

# Shape Optimisation for Crashworthiness

F. Duddeck<sup>1</sup>, S. Hunkeler<sup>1,2</sup>, H. Zimmer<sup>3</sup>,  
L. Rota<sup>4</sup>, M. Zarroug<sup>4</sup>

# Shape Optimisation for Crashworthiness

## Content

- Motivation
- SFE CONCEPT for geometrical variations
- Test examples for validation (front rail)
- Industrial examples (front rail)
- Optimisation results and recommendations
- Conclusions and outlook

# Motivation

## State-of-the-Art in Shape Optimisation

Example:

7th Europ. LS-DYNA Conf. 2009

Multi-Disciplinary Design Optimization exploiting the efficiency of ANSA-LSOPT-META coupling

Korbetis Georgios, Siskos Dimitrios,

BETA CAE Systems S.A.

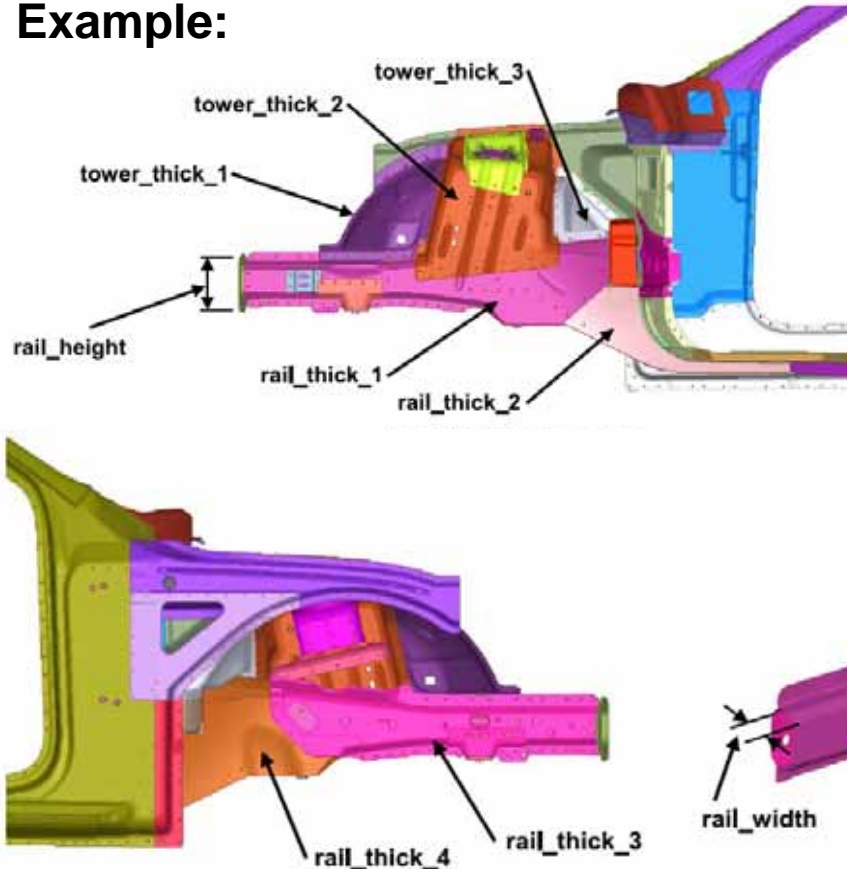


Figure 3: Design variables

Design Variable	Type	Initial Value [mm]	Lower Bound [mm]	Upper Bound [mm]
Rail_thick_1	Discrete	1.6	1.2	2
Rail_thick_2	Discrete	1.8	1.4	2.6
Rail_thick_3	Discrete	1.6	1.2	2
Rail_thick_4	Discrete	2.0	1.6	2.8
Tower_thick_1	Discrete	1.4	1	2
Tower_thick_2	Discrete	2.	1.6	3
Tower_thick_3	Discrete	0.8	0.6	1
Rail_height	Continuous	160	140	180
Rail_width	Continuous	64	60	68
Bead_depth	Continuous	0	0	6

# Motivation

## State-of-the-Art in Shape Optimisation



Figure 6: Rail initial shape

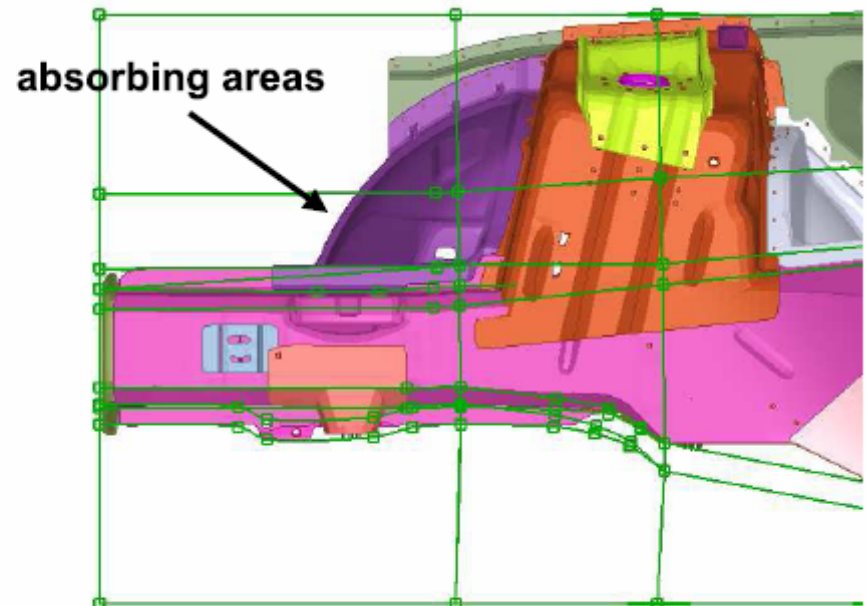


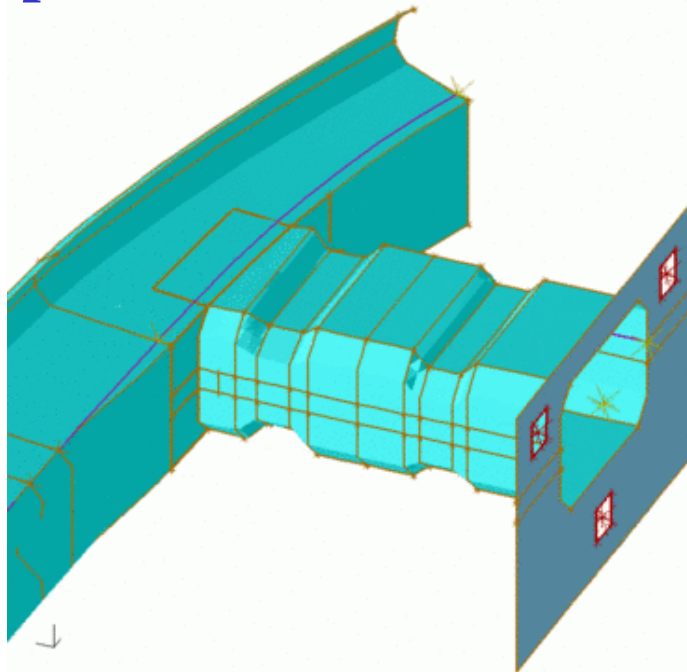
Figure 7: Rail modified shape

**Morphing can only realise small geometrical modifications**  
⇒ **Truly shape optimisation methods required**

Automated  
Variation  
of  
Geometries  
for  
Shape  
Optimisation

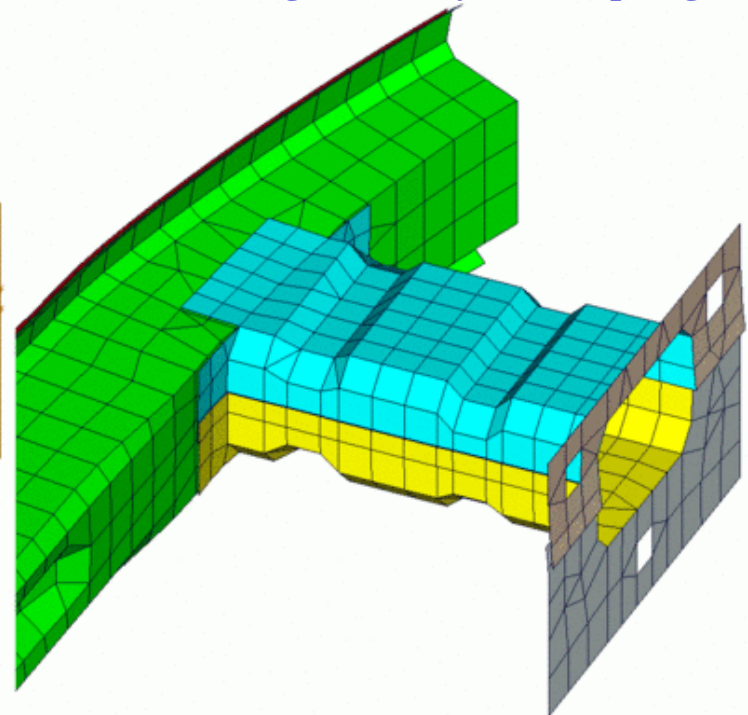
SFE CONCEPT Model

**Fully parametric  
model for shape  
optimisation**



SFE CONCEPT FE Mesh

**Parametric geometry change  
Automatic mesh adaptation**  
includes the capability of morphing  
and goes far beyond morphing

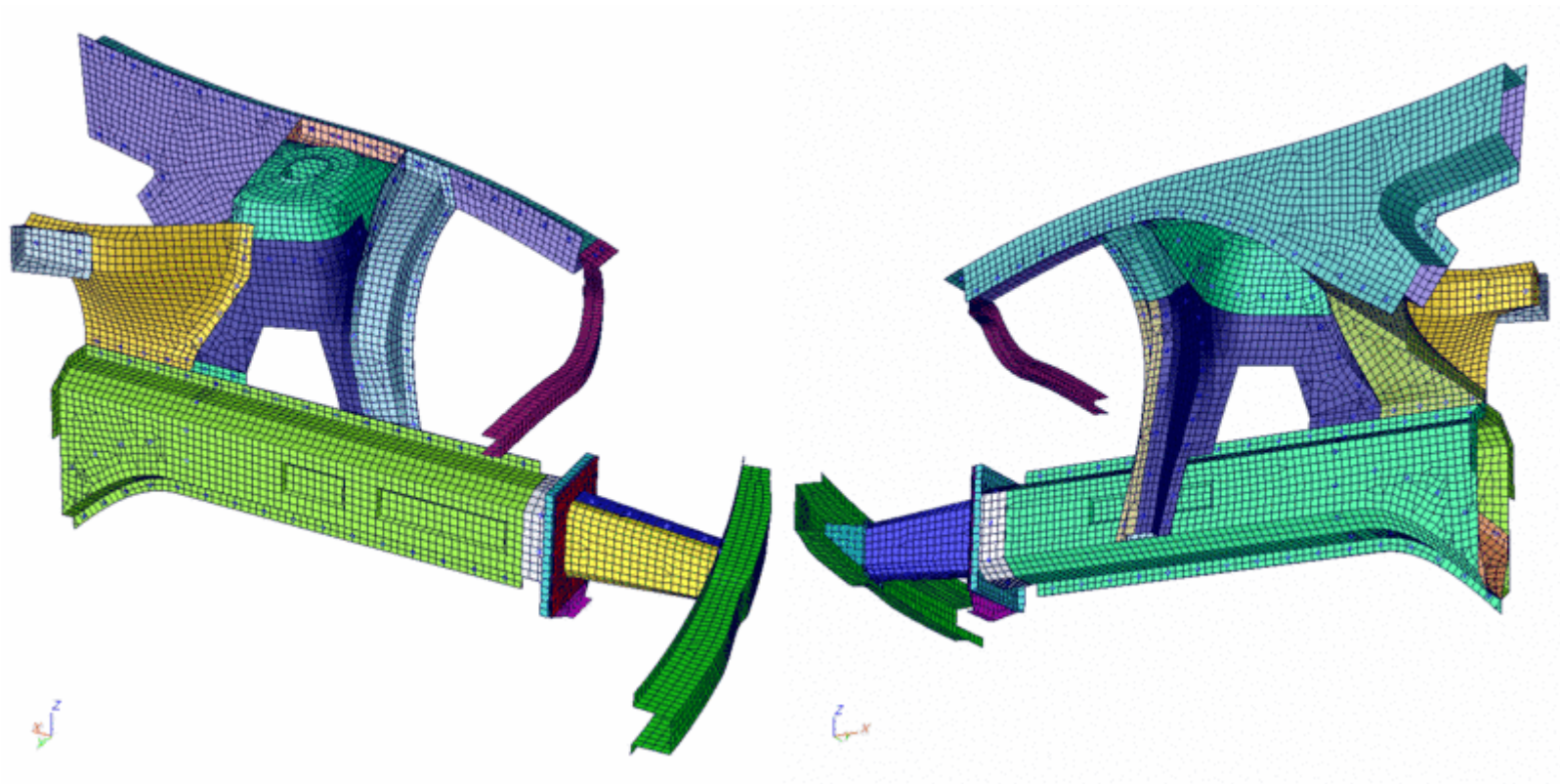


October 2009

Hans Zimmer  
President & CEO  
h.zimmer@sfe-berlin.de  
SFE GmbH, Berlin  
<http://www.sfe-berlin.de>

Automated  
Variation  
of  
Geometries  
for  
Shape  
Optimisation

## Complex geometries in complex environments



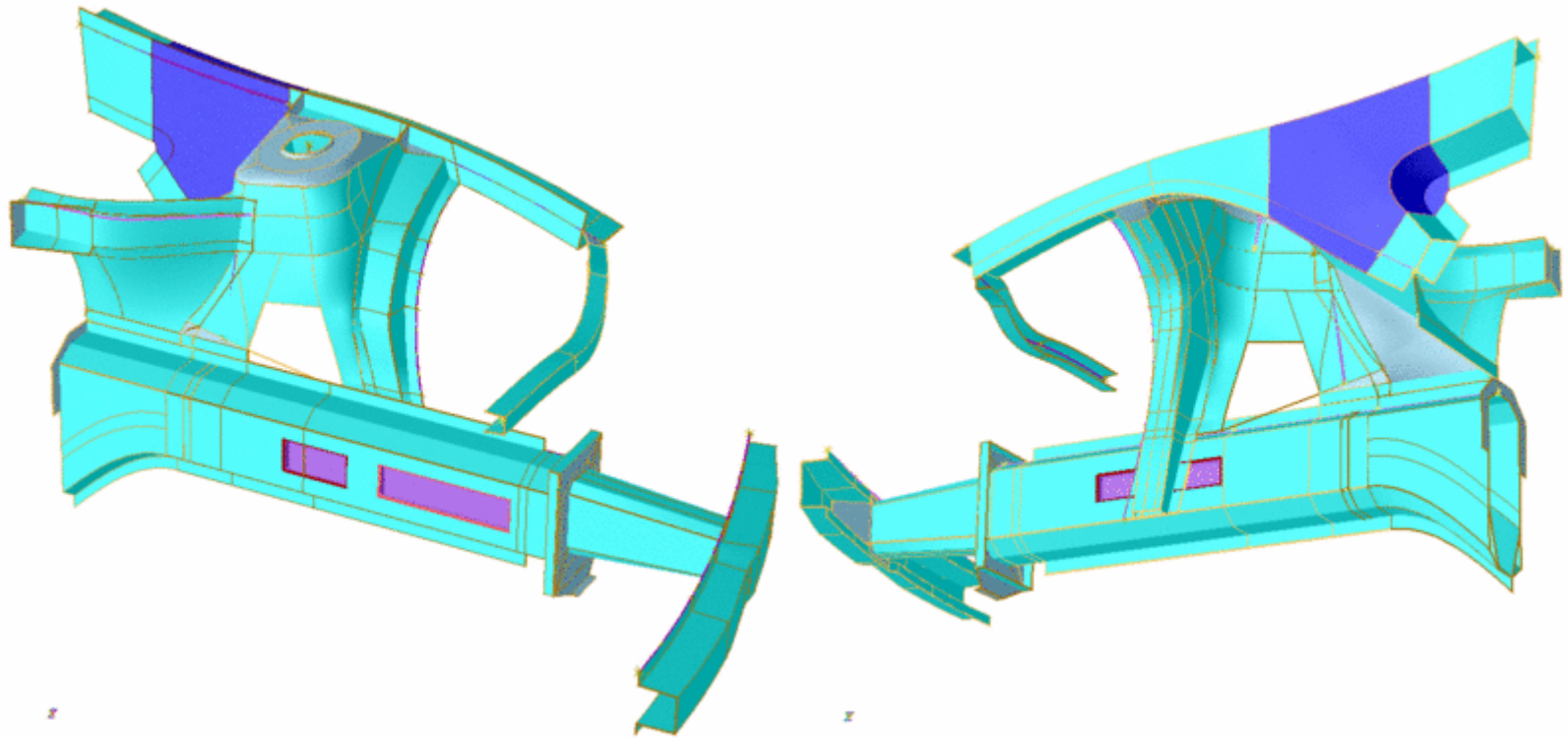
October 2009

Hans Zimmer  
President & CEO  
h.zimmer@sfe-berlin.de  
SFE GmbH, Berlin  
<http://www.sfe-berlin.de>



Automated  
Variation  
of  
Geometries  
for  
Shape  
Optimisation

## Complex geometries in complex environments

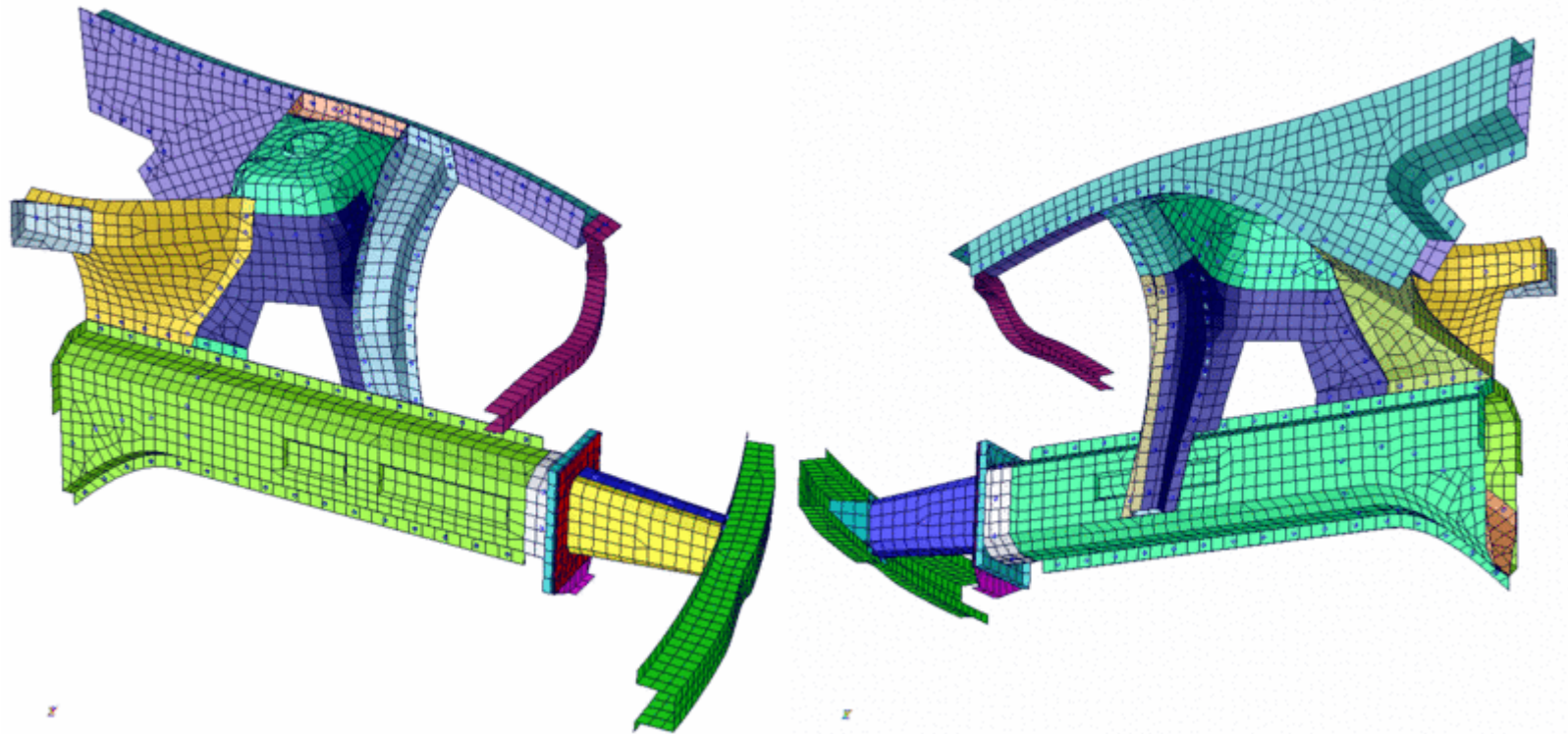


October 2009

Hans Zimmer  
President & CEO  
h.zimmer@sfe-berlin.de  
SFE GmbH, Berlin  
<http://www.sfe-berlin.de>

Automated  
Variation  
of  
Geometries  
for  
Shape  
Optimisation

## Complex geometries in complex environments



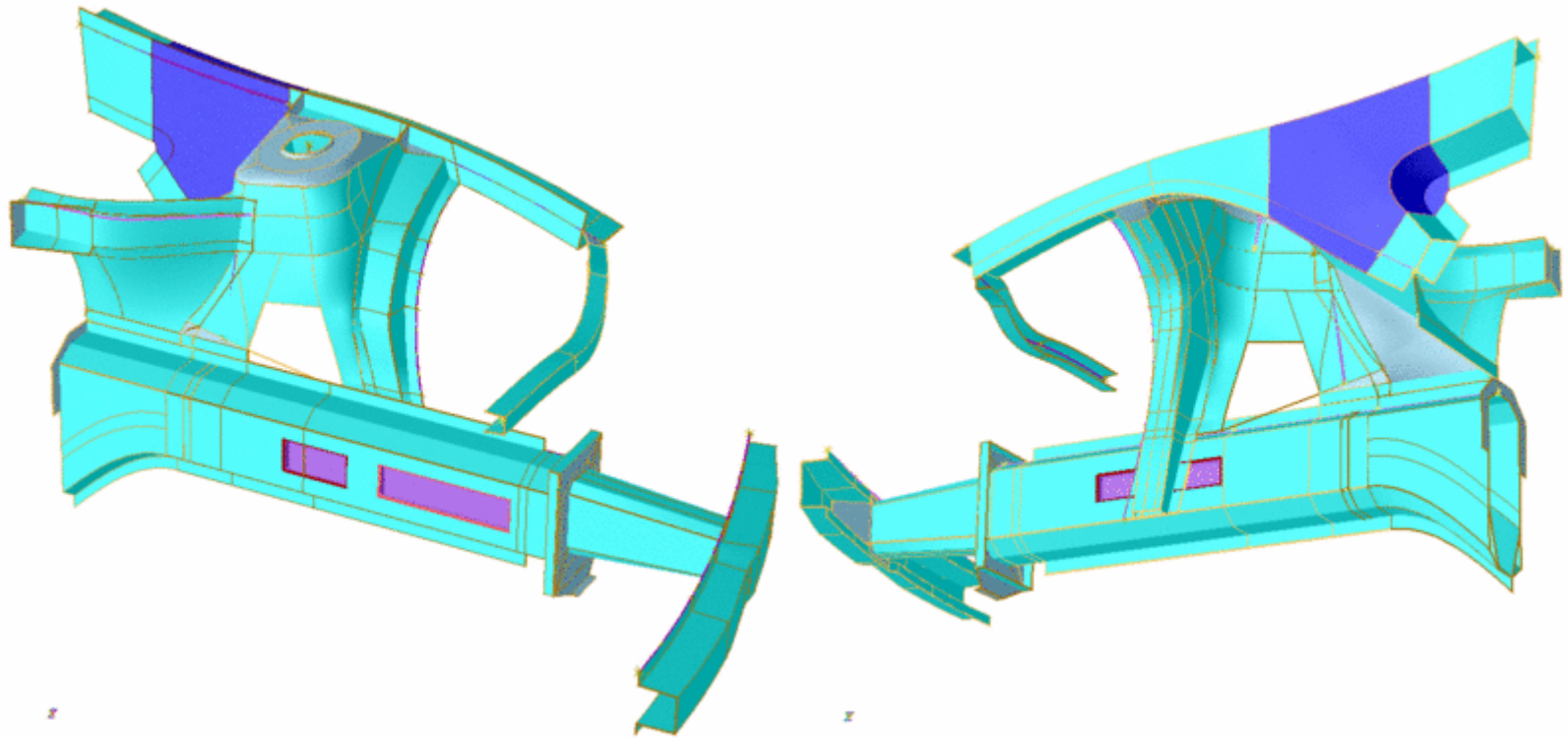
October 2009

Hans Zimmer  
President & CEO  
h.zimmer@sfe-berlin.de  
SFE GmbH, Berlin  
<http://www.sfe-berlin.de>



Automated  
Variation  
of  
Geometries  
for  
Shape  
Optimisation

## Complex geometries in complex environments

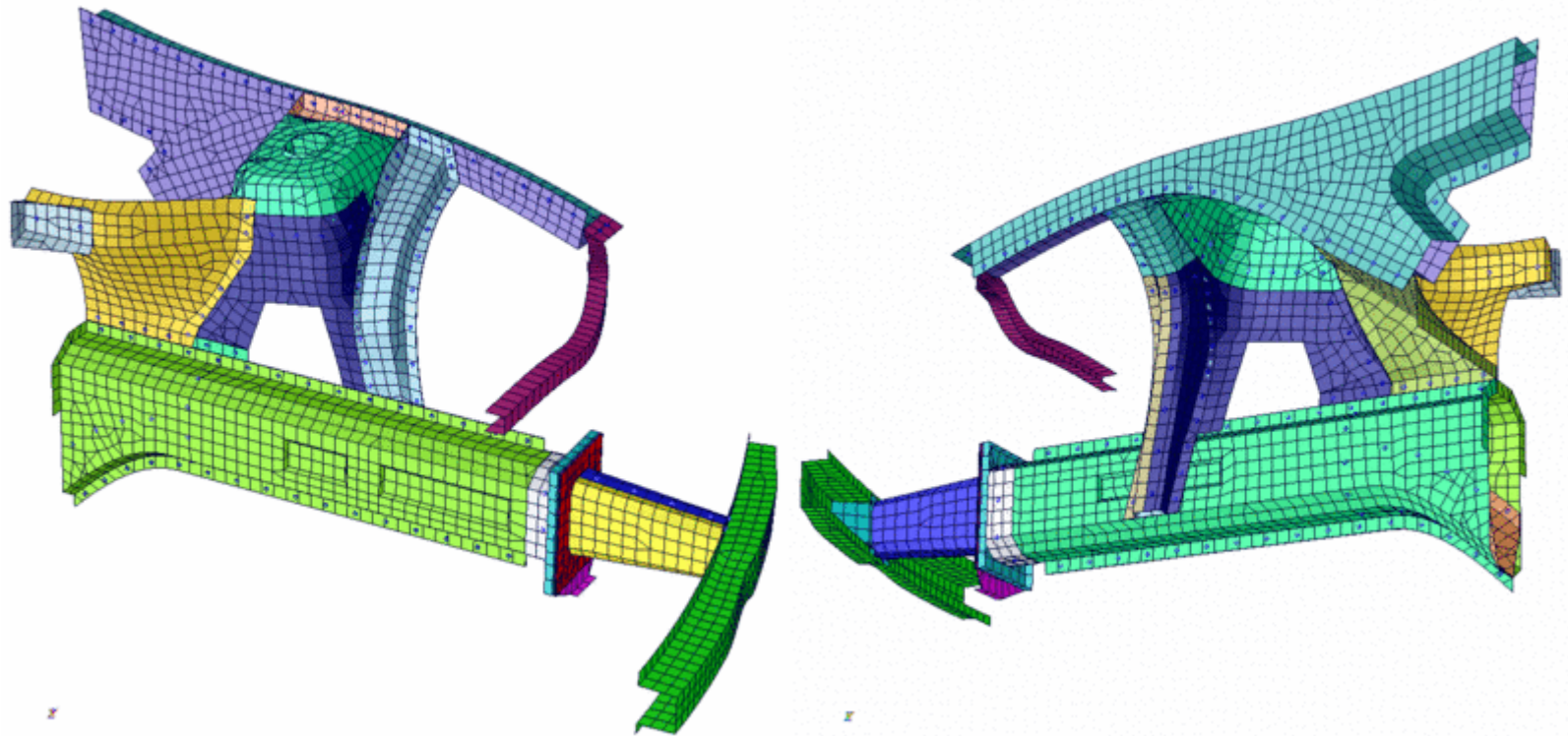


October 2009

Hans Zimmer  
President & CEO  
h.zimmer@sfe-berlin.de  
SFE GmbH, Berlin  
<http://www.sfe-berlin.de>

Automated  
Variation  
of  
Geometries  
for  
Shape  
Optimisation

## Complex geometries in complex environments

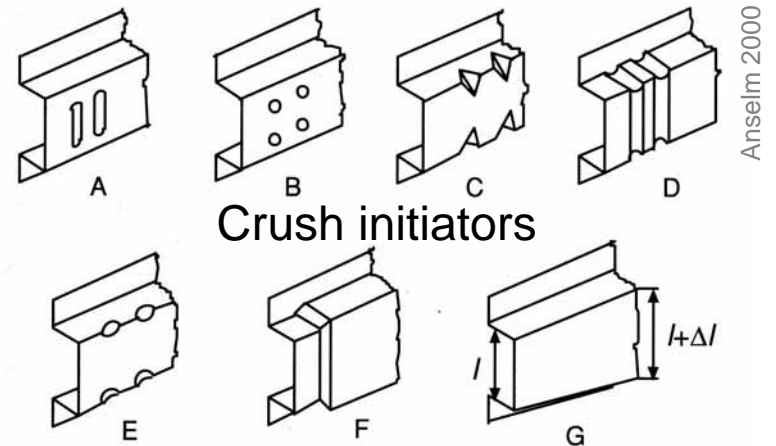


October 2009

Hans Zimmer  
President & CEO  
h.zimmer@sfe-berlin.de  
SFE GmbH, Berlin  
<http://www.sfe-berlin.de>

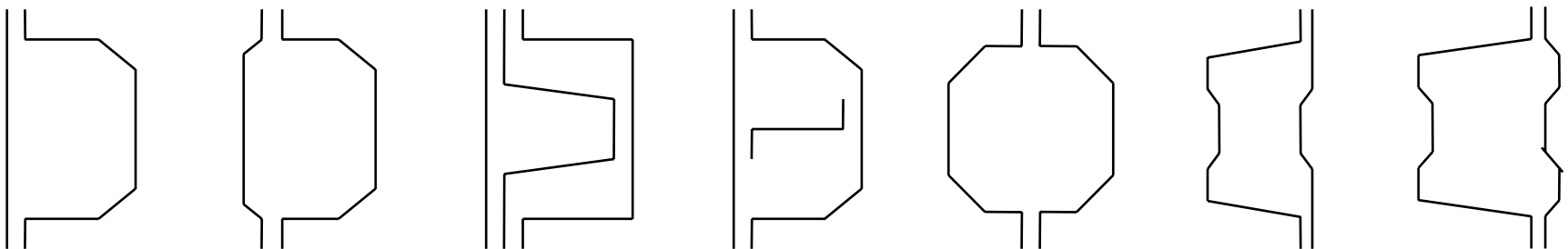
# Example: Crash Boxes

- Simplest example
- But already a high number of design variables;
- High sensitivity to fluctuations in load configurations & other factors;
- Non-repetitive FEM computations if computed in parallel;



# Example: Frontal Rail

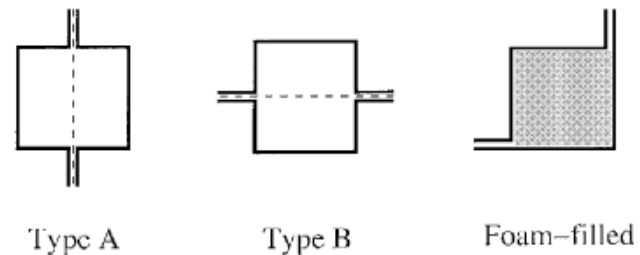
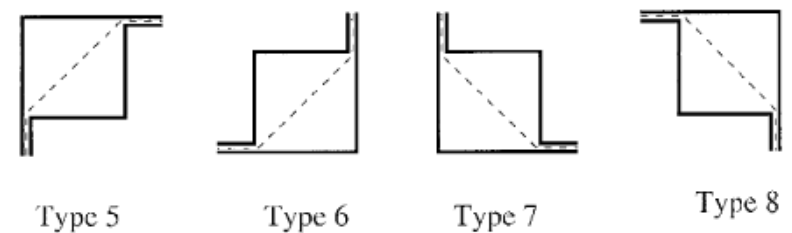
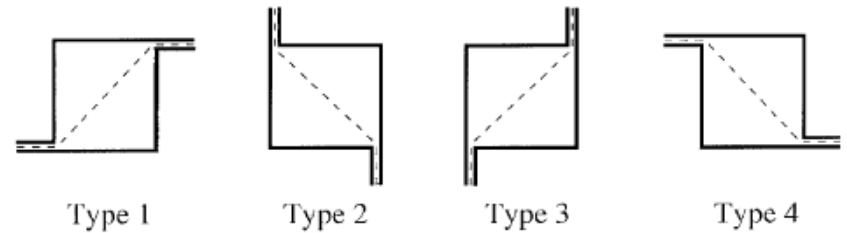
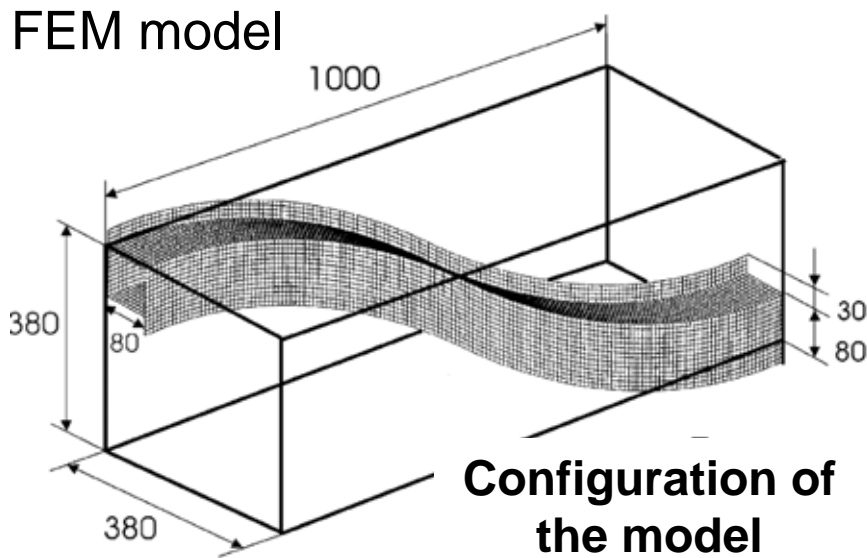
- Very high number of design variables
- Complex geometrical situation
- High importance for crash



Industrial examples (cross-sections)

# Example: Frontal Rail

Study by Wierzbicki et al. (MIT 2001)



**Various cross-sectional shapes considered**

Kim & Wierzbicki (2001)

## Not considered:

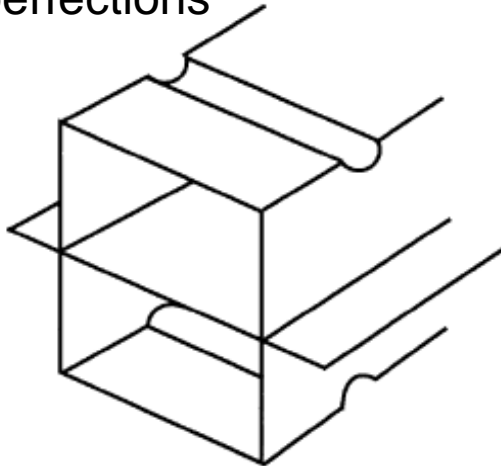
- Failure, strain rate dependency
- Real geometry variation
- Changes in longitudinal direction
- Other modes (global buckling)



# Example: Frontal Rail

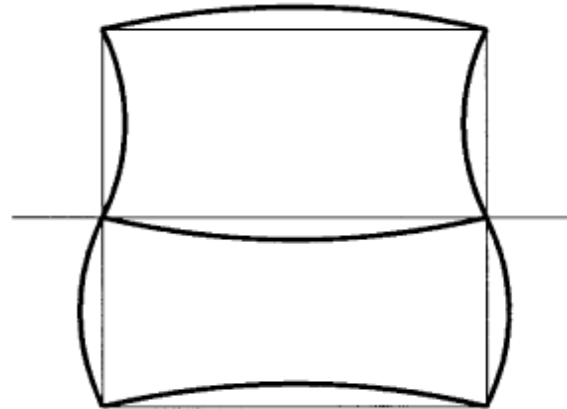
## Geometrical Imperfections

Local imperfections



Geometrical imperfection (type 1)

Global imperfections



Geometrical imperfection (type 2)

### For real robustness analysis:

- Small local geometrical variations at arbitrary locations
- More general approach covering local and global imperfections
- Thickness fluctuations should be taken into account
- Global parameters (angle, position, location of other adjacent objects)

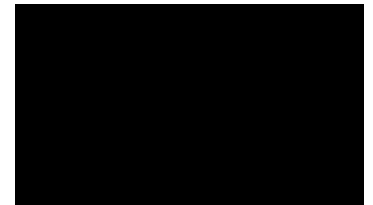
# Example: Frontal Rail

## Changes in Longitudinal Direction

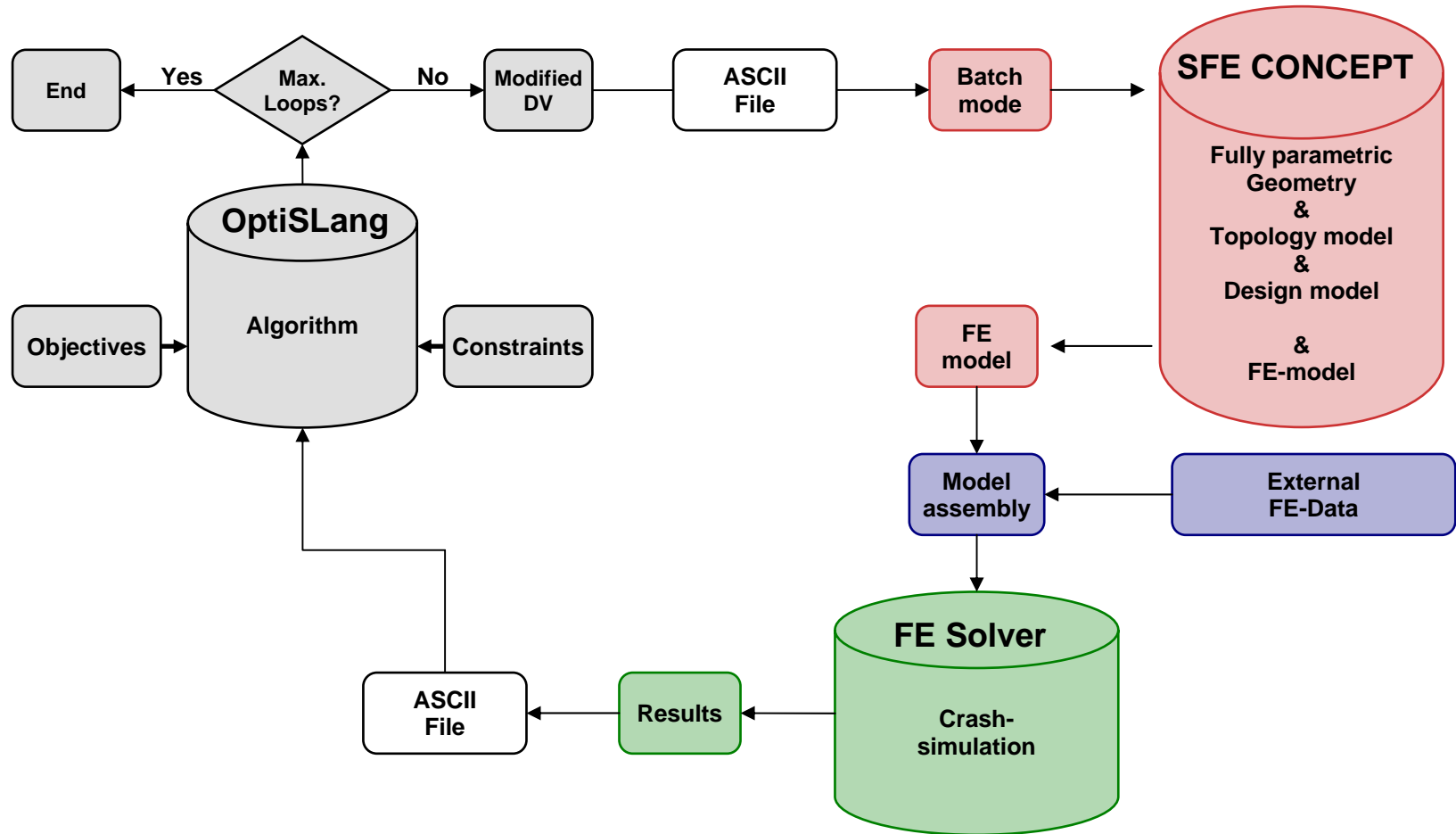


### For real shape optimisation:

- Different zones: folding at the beginning, buckling in the engine area;
- No constant cross-sectional area in longitudinal direction
- Thickness variations in axial direction
- Reinforcements and crush initiators, connection points etc.

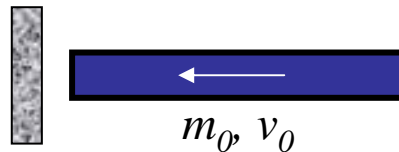


# Optimisation Loop



# Simplified Test Problem

- **First study to evaluate optimisation methods and investigate practical parameterisations**

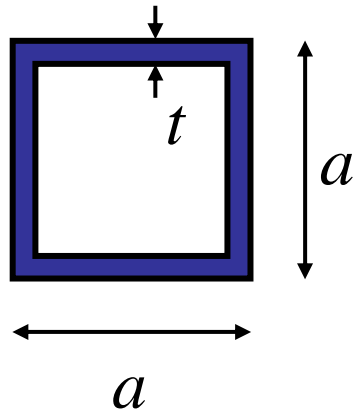


- Transverse crash on a beam encastred at one extremity ( $m_0 = 500$  kg ,  $v_0 = 10$  m/s);
- **Objective:** maximise SEA (= specific energy absorption, i.e. internal energy / mass) during the first 20 ms;
- **Constraint:** maximal transverse force should remain lower than 70 kN;

# Simplified Test Problem

## Four Test Cases

**Case A**

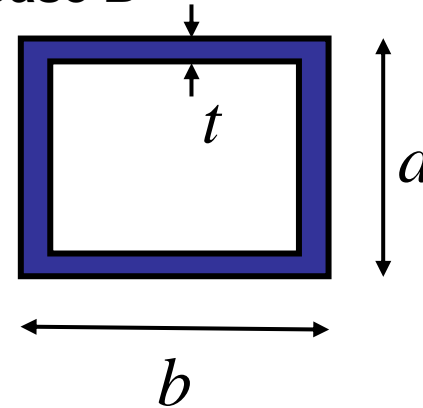


2 parameters

$$60 \leq a < 100$$

$$1.4 \leq t < 3.0$$

**Case B**



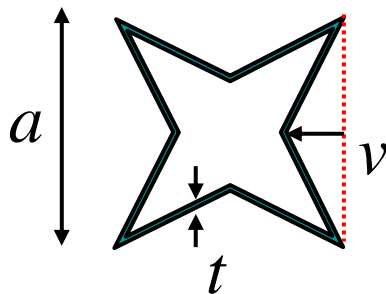
3 parameters

$$60 \leq a < 100$$

$$60 \leq b < 100$$

$$1.4 \leq t < 3.0$$

**Case C**



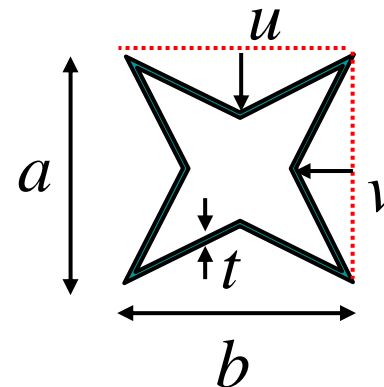
3 parameters

$$60 \leq a < 100$$

$$-20 \leq v < 20$$

$$1.4 \leq t < 3.0$$

**Case D**



5 parameters

$$60 \leq a < 100$$

$$60 \leq b < 100$$

$$-20 \leq v < 20$$

$$-20 \leq u < 20$$

$$1.4 \leq t < 3.0$$

All dimensions in mm

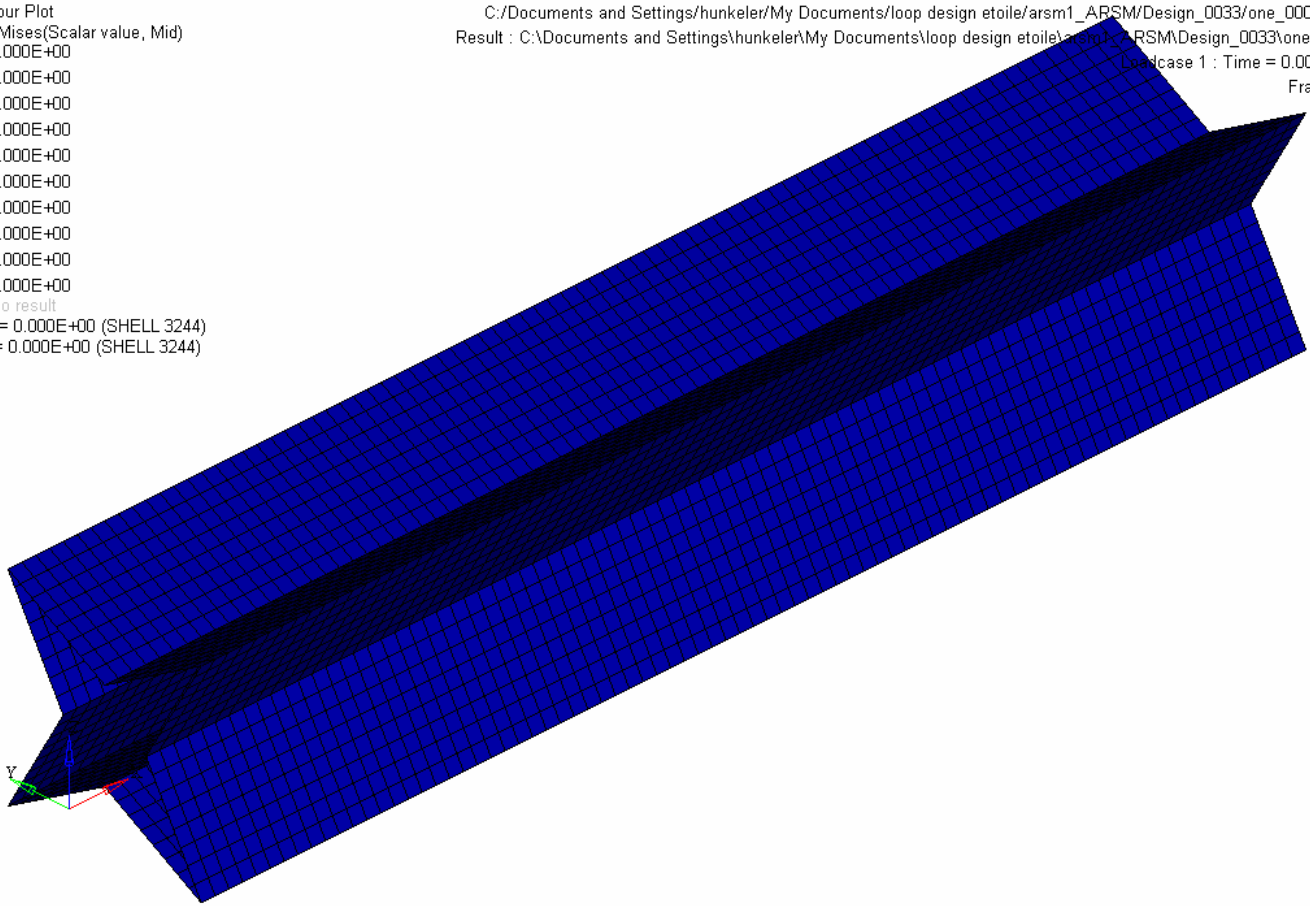


# Simplified Test Problem

## Initial Model

Contour Plot  
Von Mises(Scalar value, Mid)  
0.000E+00  
0.000E+00  
0.000E+00  
0.000E+00  
0.000E+00  
0.000E+00  
0.000E+00  
0.000E+00  
0.000E+00  
0.000E+00  
No result  
Max = 0.000E+00 (SHELL 3244)  
Min = 0.000E+00 (SHELL 3244)

C:/Documents and Settings/hunkeler/My Documents/loop design etoile/arsm1\_ARSM/Design\_0033/one\_0000.rad  
Result : C:\Documents and Settings\hunkeler\My Documents\loop design etoile\arsm1\_ARSM\Design\_0033\oneA001  
Loadcase 1 : Time = 0.000000  
Frame 1



Initial model

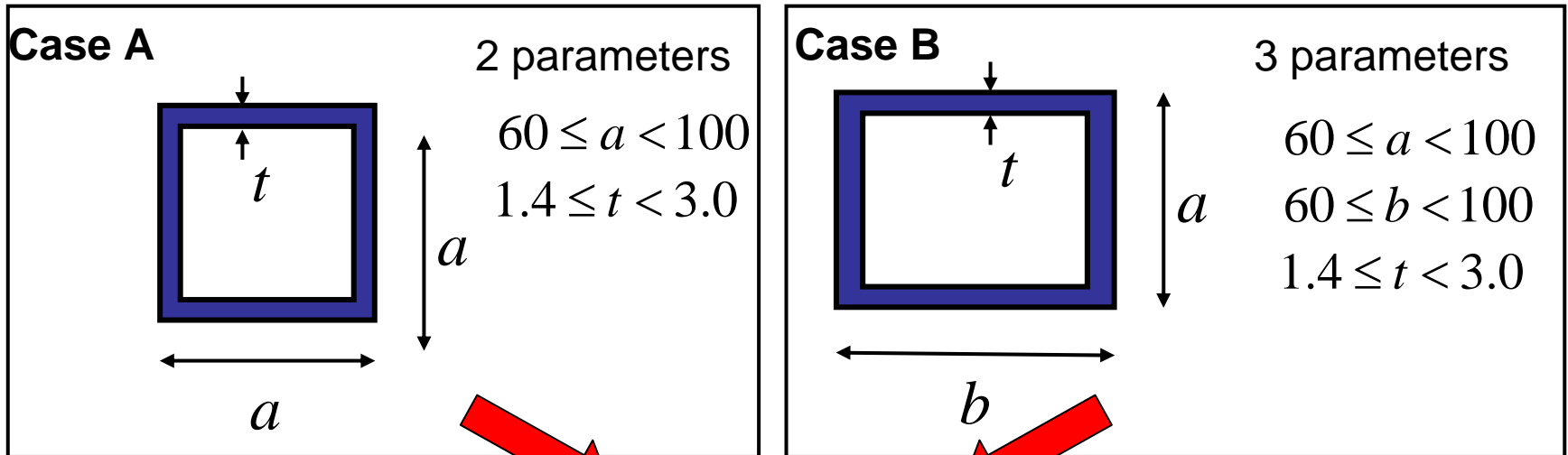
# Simplified Test Problem

## Optimisation methods

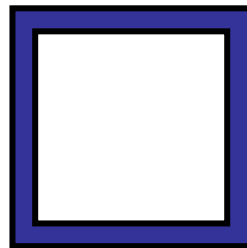
- Optimisation with adaptive response surface methods (ARSM) or evolutionary/genetic algorithms (optiSLang)
- There is no unique algorithm for all cases, hence an automated decision should be implemented and a hybrid approach realised;
- For ARSM, linear approximation and D-optimal sampling are acceptable to avoid high numerical effort
- RSM should be adaptive or successive;
- Evolutionary algorithms (EA) are in most cases better than genetic algorithms (GA).

# Simplified Test Problem

## Results (1)



**ARSM**  
**(39 shapes computed):**  
Opt energy absorption  
SEA: 10.24 kJ/kg

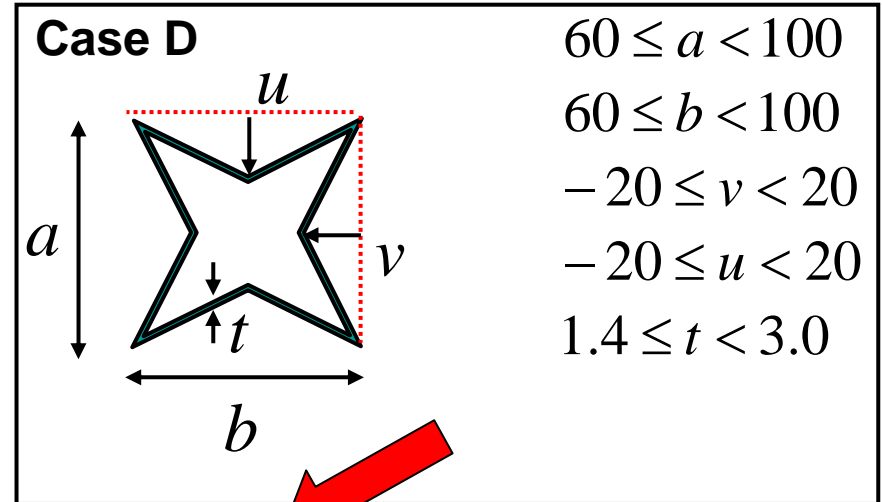
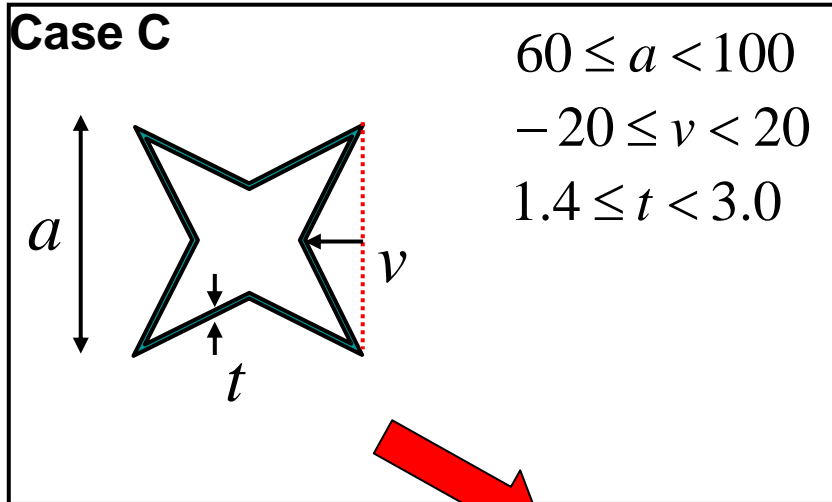


**ARSM (111 shapes):**  
Opt SEA: 10.18 kJ/kg  
**EA (368 shapes):**  
Opt SEA: 9.39 kJ/kg

**Square is the ideal rectangular shape**

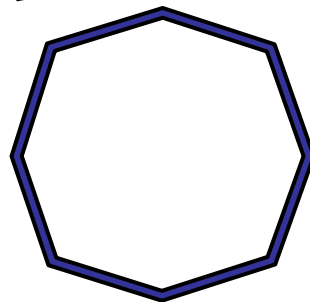
# Simplified Test Problem

## Results (2)

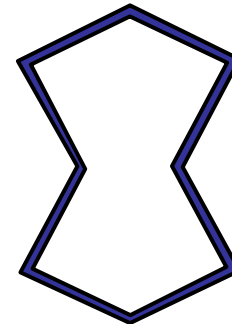


**ARSM (80 shapes)**

Opt. SEA:  
10.31 kJ/kg



**Octagon as ideal symmetric shape**



**ARSM (139 shapes)**

Opt SEA: 11.36 kJ/kg

**EA (292 shapes)**

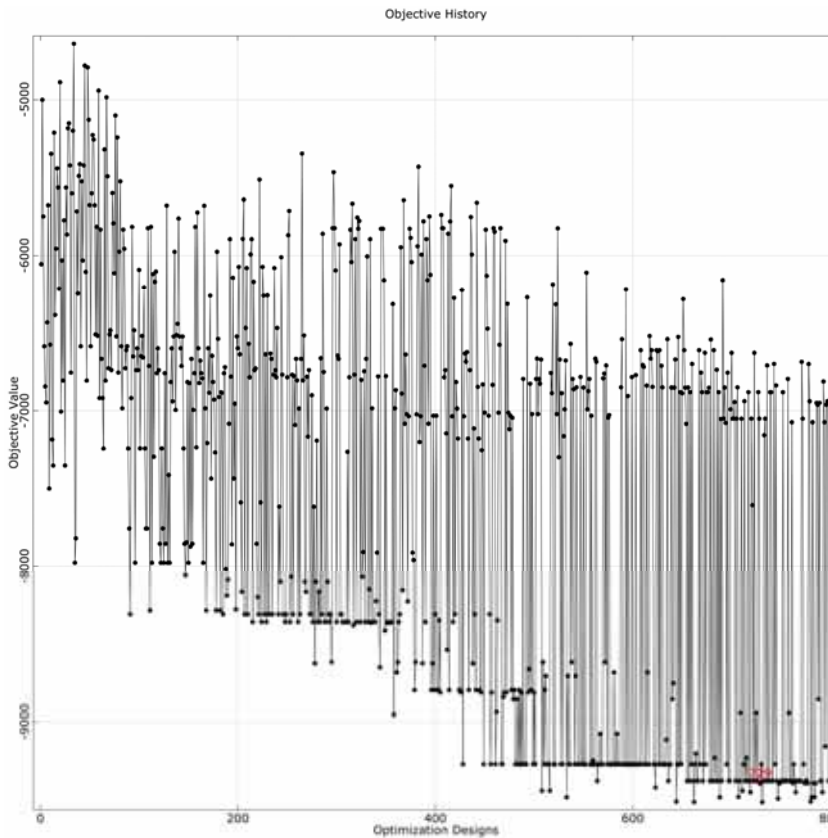
Opt SEA: 11.35 kJ/kg

**Non-symmetric octagon is better**

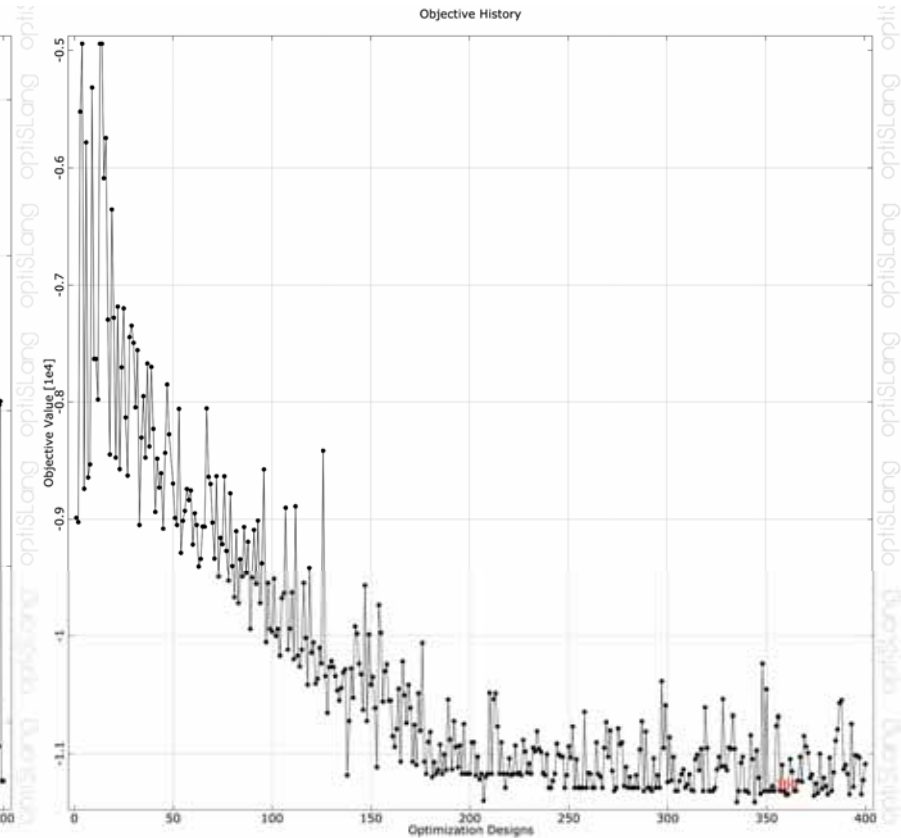
# Simplified Test Problem

## Results (3)

Convergence EA



Convergence ARSM





# Simplified Test Problem

## Summary of Results

- Parameterisations 1 and 2 present almost identical optima
- Slight improvement on parameterisation 3
- Significant improvement on parameterisation 4
- ARSM faster and reaching better results than EA
- Still true with more parameters ?

# Real Evaluation Problem

## (inspired from industry)

- Crash case slightly different  
( $m_0 = 460$  kg,  $v_0 = 12$  m/s, duration 50 ms)
- Objective: minimise the mass of the front rail
- Constraints:
  - Final internal energy higher than 30 kJ
  - Highest axial displacement lower than 300 mm
  - Fit into the allocated space
  - Highest transverse displacement lower than 15 mm  
(no buckling mode)

# Real Evaluation Problem

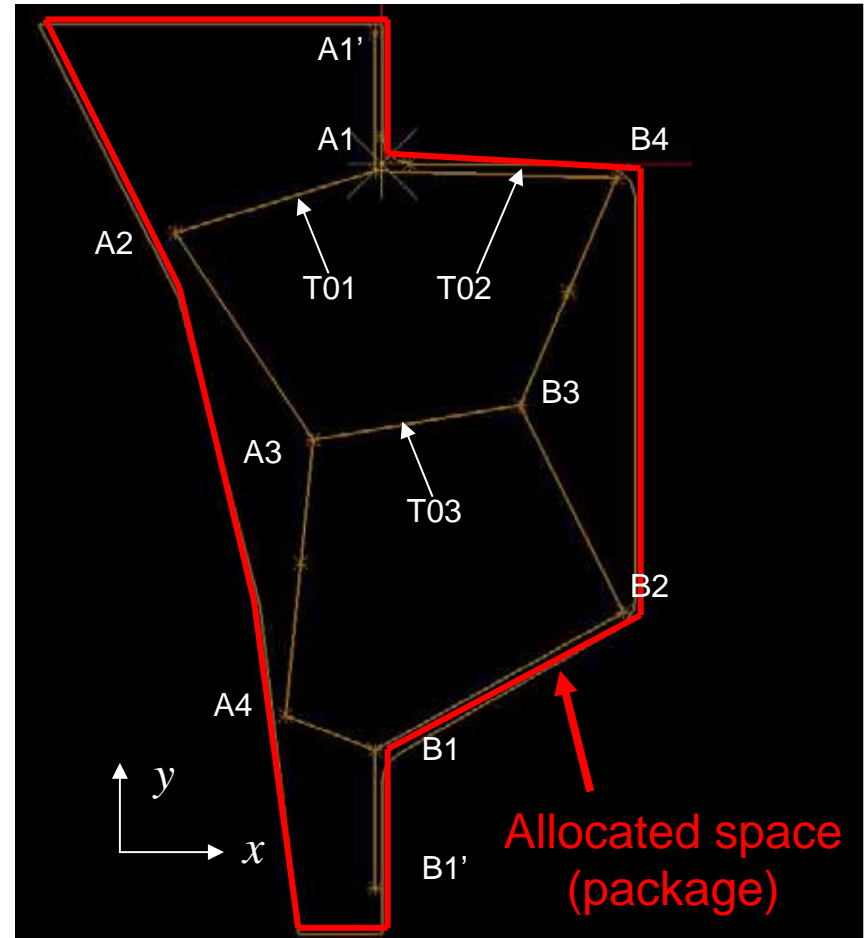
## Natural Parameterisation

- 3 thickness parameters

Left: T01	Middle: T03	Right: T02
-----------	-------------	------------

- 14 geometrical parameters

XA1	
XA2	YA2
XA3	YA3
XA4	YA4
XB1	
XB2	YB2
XB3	YB3
XB4	YB4



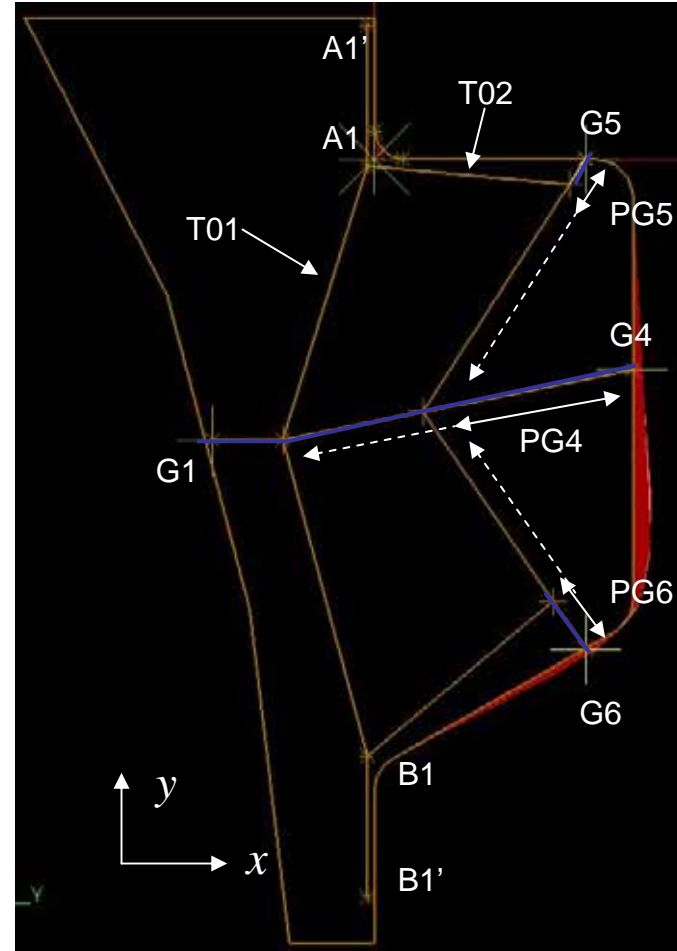
# Advanced Parameterisation Offset Mapping (SFE)

- 2 thickness parameters

Left: T01	Right: T02
-----------	------------

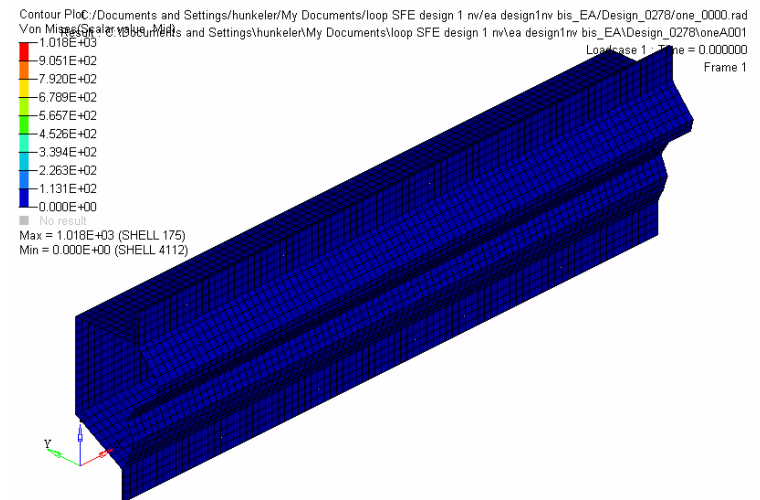
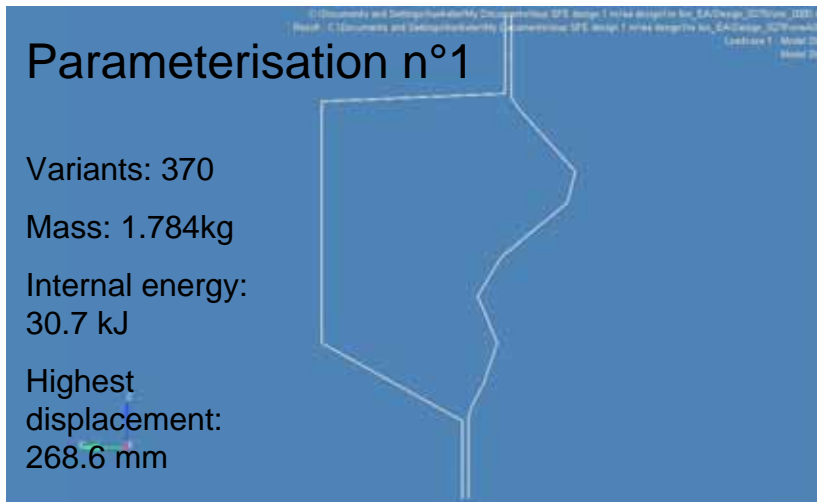
- 10 geometrical parameters

XA1	
LG1	YG1
XB1	
PG4	YG4
PG5	XG5
PG6	XG6



# Real Evaluation Problem Optimisation

- Ran exclusively with Evolutionary Algorithms
- Stochastically generated starting population (but inside the constrained design space)
- Several parameterisations tested





# Real Evaluation Problem

## Optimisation Results

- Results and number of designs computed are highly dependant on starting population;
- Difficulties to ponder between improving the objective function and reaching the output constraints;
- Though, good results for a few parameterisations (work in progress);

# Further Developments

- Combination of ARSM on coarse parameterisation and EA on a complex parameterisation based on previous optimum
- Better way of dealing with the allocated space using « offset mapping »
- Combination with simplified crash models (VCS or similar)

# Functions we could have used

- For response surface generation, an option to prioritise sample points
- For EA, population generation taking into account the input constraints (and correctly distributed in the design space)
- Post-treatment, check the accuracy of consecutive hyper-surfaces in ARSM methods

# Conclusions

- Morphing approach should be complemented by true shape alterations via SFE CONCEPT
- High number of variables
- Good parameterisations required
- Good optimisation algorithms required (combination ARSM & EA)
- Further work necessary ...

# Acknowledgements

I would like to thank all people involved in the project

- Hans Zimmer and the collaborators of SFE GmbH
- Johannes Will and the team of Dynardo
- Laurent Rota / Malek Zarroug for industrial aspects
- Prof Ehrlacher and all people involved at the Ecole des Ponts ParisTech
- The friendly licensing by Altair/UK
  
- And especially: Stephan Hunkeler for his great work.

F. Duddeck, WOST 2009