

New Reliability Methodologies for Driving Scenarios

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How many miles ...

Table 1. Examples of Miles and Years Needed to Demonstrate Autonomous Vehicle Reliability

Statistical Question	Benchmark Failure Rate			
	How many miles (years ^a) would autonomous vehicles have to be driven...	(A) 1.09 fatalities per 100 million miles?	(B) 77 reported injuries per 100 million miles?	(C) 190 reported crashes per 100 million miles?
	(1) without failure to demonstrate with 95% confidence that their failure rate is at most...	275 million miles (12.5 years)	3.9 million miles (2 months)	1.6 million miles (1 month)
	(2) to demonstrate with 95% confidence their failure rate to within 20% of the true rate of...	8.8 billion miles (400 years)	125 million miles (5.7 years)	51 million miles (2.3 years)
	(3) to demonstrate with 95% confidence and 80% power that their failure rate is 20% better than the human driver failure rate of...	11 billion miles (500 years)	161 million miles (7.3 years)	65 million miles (3 years)

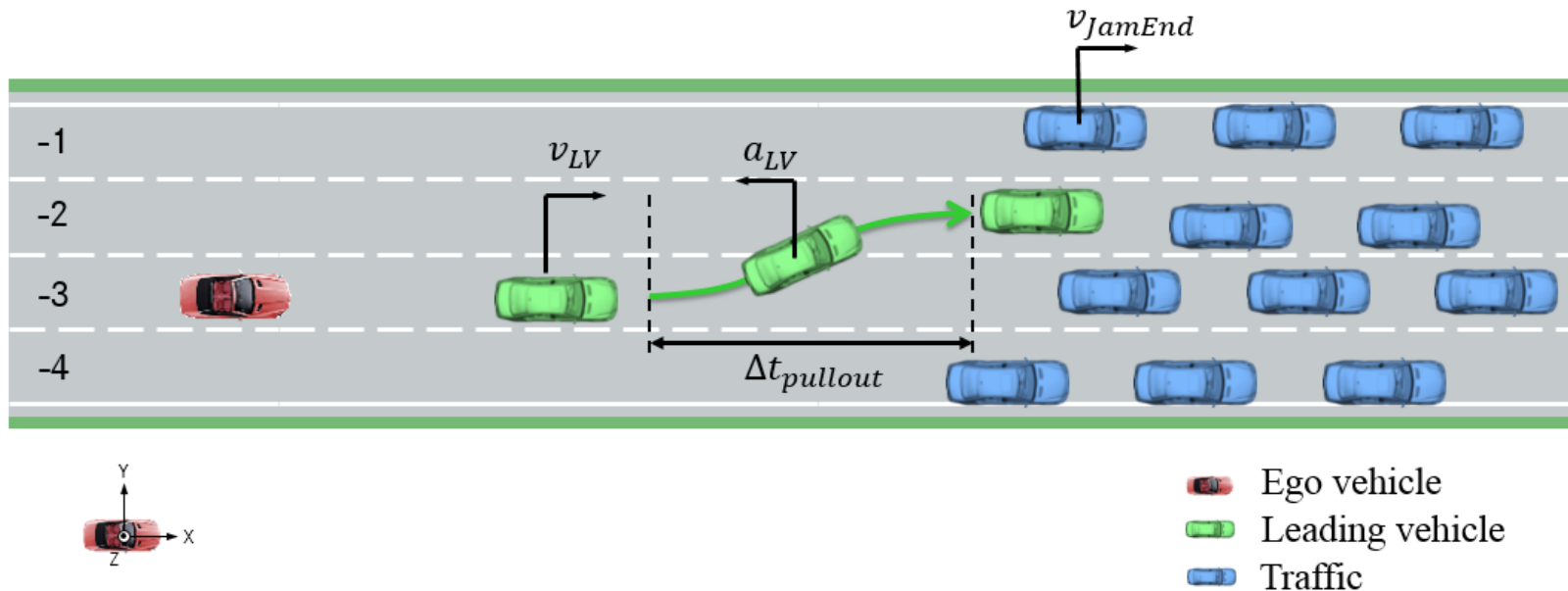
^a We assess the time it would take to complete the requisite miles with a fleet of 100 autonomous vehicles (larger than any known existing fleet) driving 24 hours a day, 365 days a year, at an average speed of 25 miles per hour.

Source: Nidhi Kalra, Susan M. Paddock: Driving to Safety, www.rand.org



There is a crucial Need for Smart Reliability Methods for Driving Scenarios

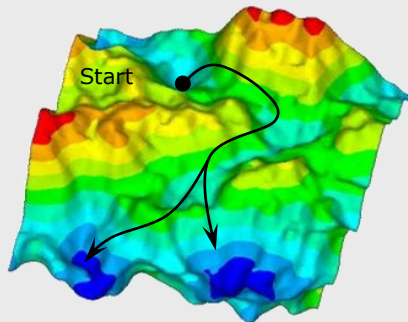
A typical driving scenario: approaching a jam tail with a lane change of the vehicle in front of the driver



Robust Design Optimization

Optimization

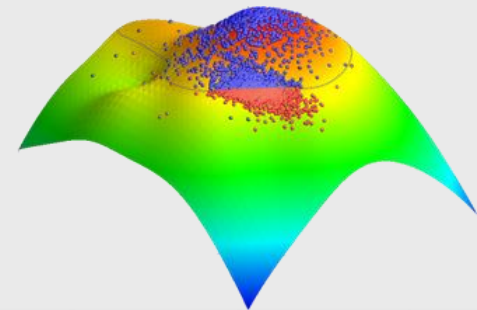
Sensitivity Analysis
Single- & Multi-Objective
(Pareto) Optimization



Robust Design

Variance-Based
Robustness Evaluation

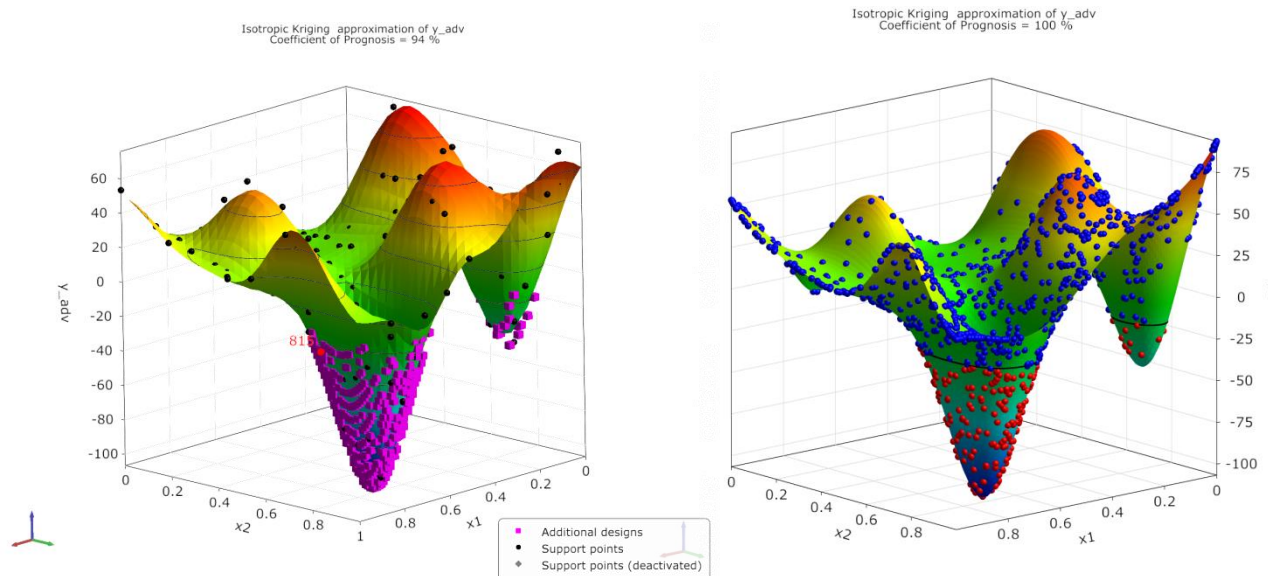
Probability-Based
Reliability Analysis



CAE process (FEM, CFD, MBD, Excel, Matlab, etc.)

Mishra's Bird Function

Test function used for events in advanced driver assistance systems



Method : Adaptive Sampling (AS)

Complete iterations : 3 / 3
Selected data : All designs

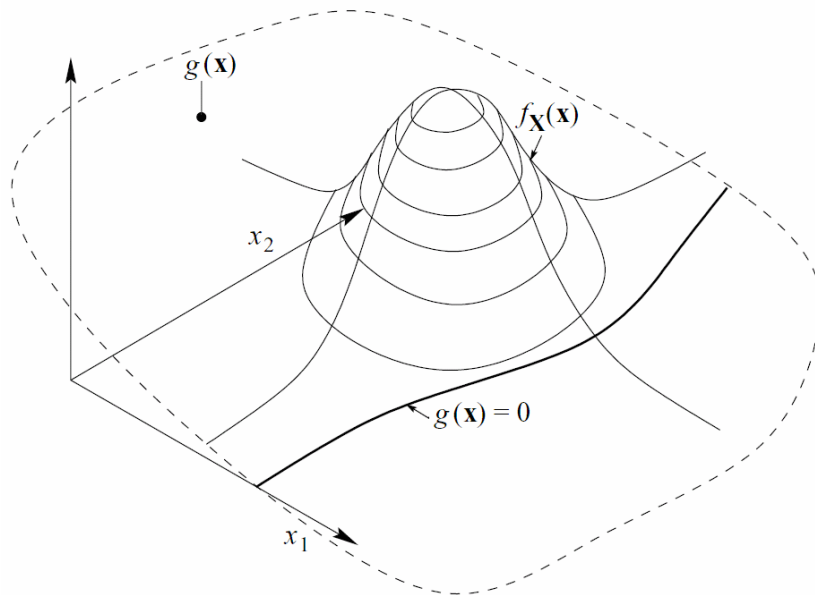
Probability of Failure : 0.110101
Standard deviation error : 0.0102236
Reliability Index : 1.22599

Number of designs

Total : 1200
Safe domain : 953
Unsafe domain : 247
Failure strings : 0
Failed : 0

Comparison of Monte Carlo based Failure Probability calculation with Adaptive Sampling method helped to reduce simulations runs from about 500.000 to 3.000

Failure Probability



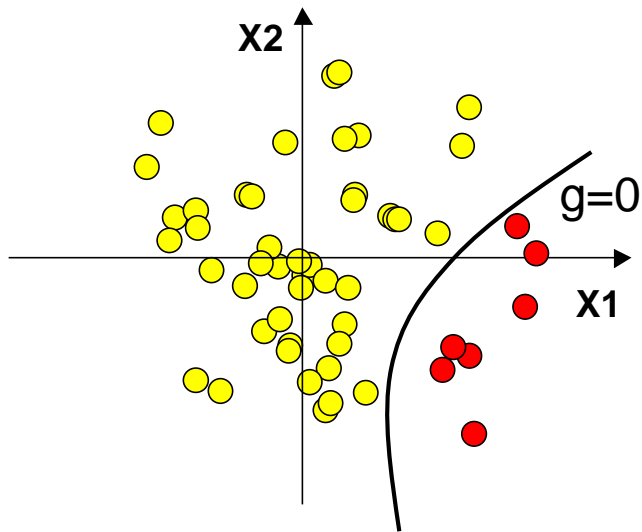
$$\begin{aligned} P_F &= P[\mathbf{X} : g(\mathbf{X}) \leq 0] \\ &= \int \cdots \int_{g(\mathbf{x}) \leq 0} f_{\mathbf{X}}(\mathbf{x}) d\mathbf{x} \\ &= \int_{-\infty}^{\infty} \cdots \int_{-\infty}^{\infty} I(g(\mathbf{x})) f_{\mathbf{X}}(\mathbf{x}) d\mathbf{x} \end{aligned}$$

- The probability of failure is the integral of the joint probability density function over the failure domain
- By introducing an indicator function

$$I(g(\mathbf{x})) = 1 \text{ if } (g(\mathbf{x})) < 0, \quad I(g(\mathbf{x})) = 0 \text{ else}$$

this can be computed as the expected value of I

Monte Carlo Simulation



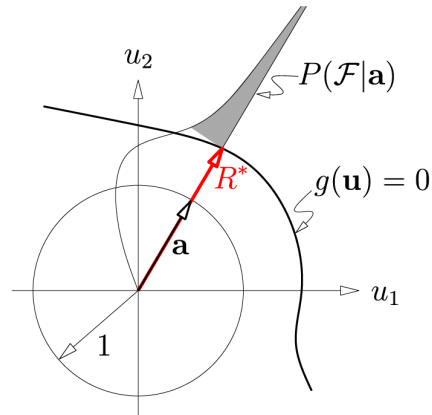
Sigma level	P_F	N for $\text{cov}(P_F) = 10\%$
2	2.3E-2	4 400
3	1.3E-3	74 000
4.5	3.4E-6	29 500 000

$$\hat{P}_F = \frac{1}{N} \sum_{i=1}^N I(g(\mathbf{x}_i)) \quad \hat{\sigma}_{P_F} = \sqrt{\frac{\hat{P}_F}{N}}$$

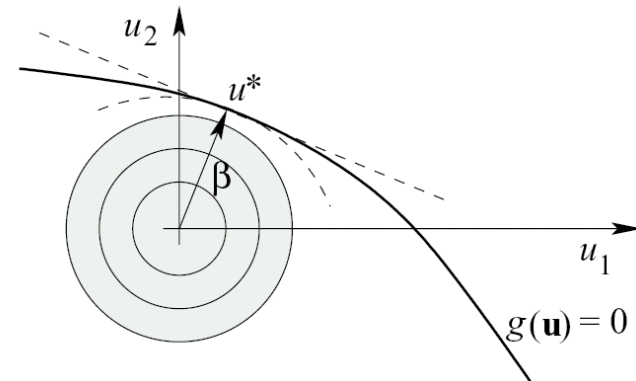
- Robust for arbitrary limit state functions
- Confidence of the estimate is very low for small failure probabilities
- Sigma level ≤ 2
- Independent of number of random variables

Some advanced methods for reliability analysis

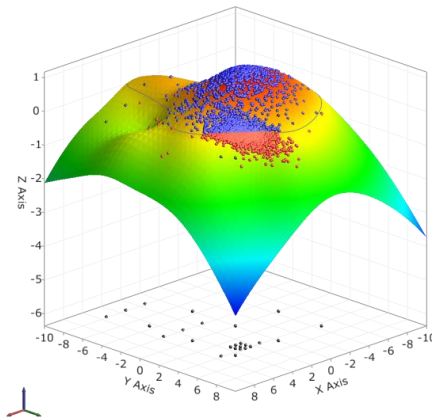
Directional Sampling



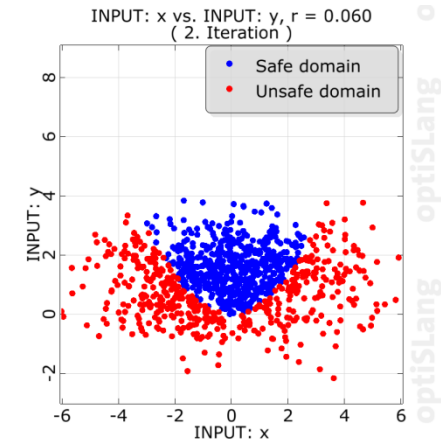
First Order Reliability Method



Adaptive RSM



Adaptive Importance Sampling



Define Limit State in optiSLang

Parameter


Name	Value
D	0.02
Ekin	10

Responses





Name	Value
x_max	0.623417
omega_damped	4.47124

- The “positive”, i.e. non-failed case is expressed
- Several criteria are automatically interpreted as series system

Criteria

Name	Type	Expression	Criterion	Limit	Evaluated expression
 lim_st_omega_damped	Limit state	omega_damped	\leq	8.5	4.47124 \leq 8.5
new					

☐ Create new

 Variable
 Objective
 Constraint
 Limit state

☐ Prefer criteria from slot
☐ Instant visualization

Robustness & Reliability – Decision Tree

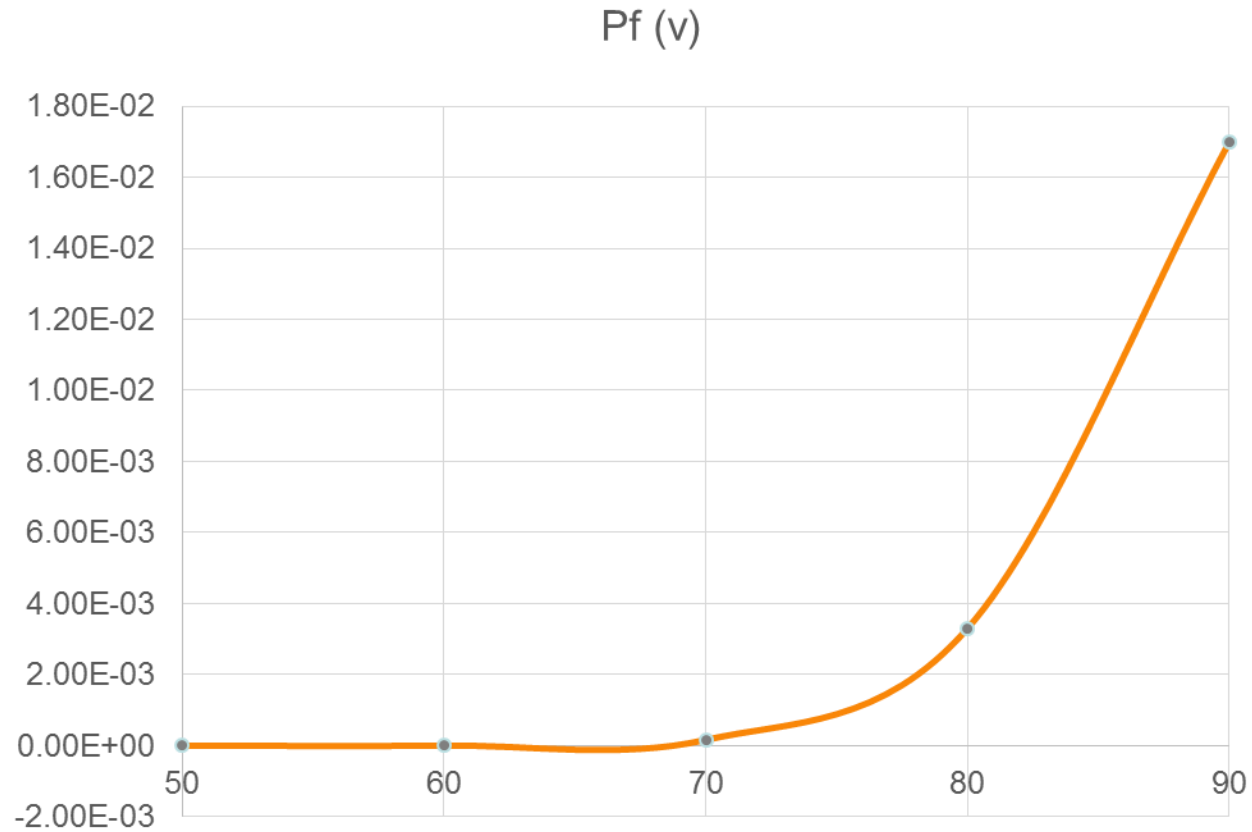
- optiSLang automatically suggests a robustness approach depending on the parameter properties, the defined criteria and user specified settings

The screenshot shows the 'Robustness / Reliability method' settings dialog in optiSLang. The interface is divided into several sections:

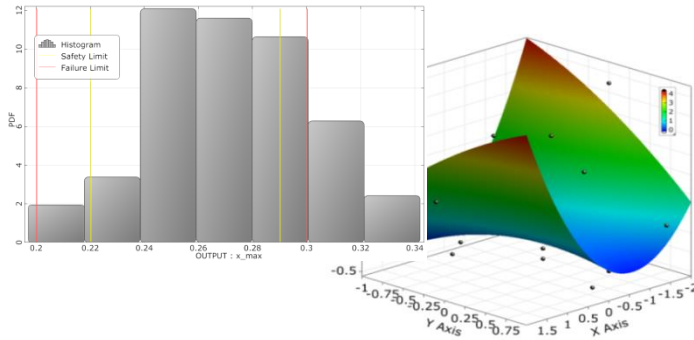
- Analysis status:** A dropdown menu set to 'Not set'.
- Constraints violations:** A dropdown menu set to 'None'.
- Failed designs:** A dropdown menu set to 'Not set'.
- Solver noise:** A dropdown menu set to 'Not set'.
- Sigma level:** A slider ranging from 2σ to 6σ , currently positioned at 2σ .
- Complexity evaluation:** A section with four input fields: 'Number of designs' (1), 'Maximum in parallel' (1), 'Runtime per design' (infinite), and 'Maximum runtime' (infinite).
- Robustness / Reliability method:** A section with two sub-sections:
 - Varianced based:** Contains a radio button for 'Robustness' (selected).
 - Probability based:** Contains several radio buttons: 'Adaptive Sampling (AS)' (selected), 'ARSM - Directional Sampling' (selected), 'Directional Sampling (DS)' (selected), 'FORM' (selected), 'ISPUD' (selected), and 'Monte Carlo Simulation (MCS)' (selected).
- Starting Point(s):** A section with two radio buttons: 'Don't using starting points' (selected) and 'Use start-design-table' (selected).

At the bottom left, there is a button labeled 'Show additional settings'.

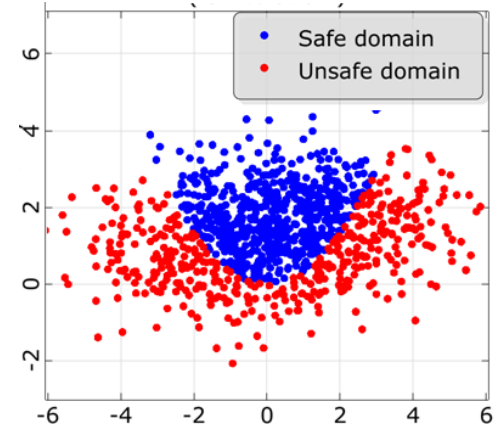
Probability of Failures and Fragility Curves



Recommended Workflow



Robustness Sampling/MOP



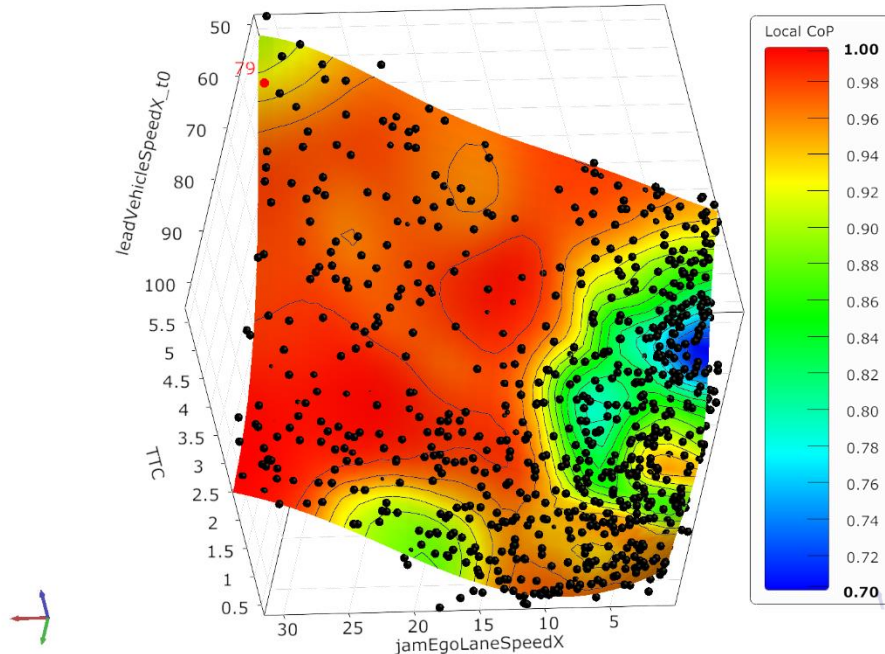
Reliability Analysis

- Check variation of inputs & responses
 - Check plausibility in MOP to proof simulation model
 - Eventually reduce parameter number
 - 200 – 500 samples
 - Check different safety limits
 - Stop if failure probability is larger as 10%
- Perform reliability analysis (e.g. Adaptive Sampling) until defined standard error (e.g. 10%) is reached
 - 2000 – 5000 samples
 - In case of fulfilled safety requirement: proof the result with different approach (e.g. Directional Sampling)

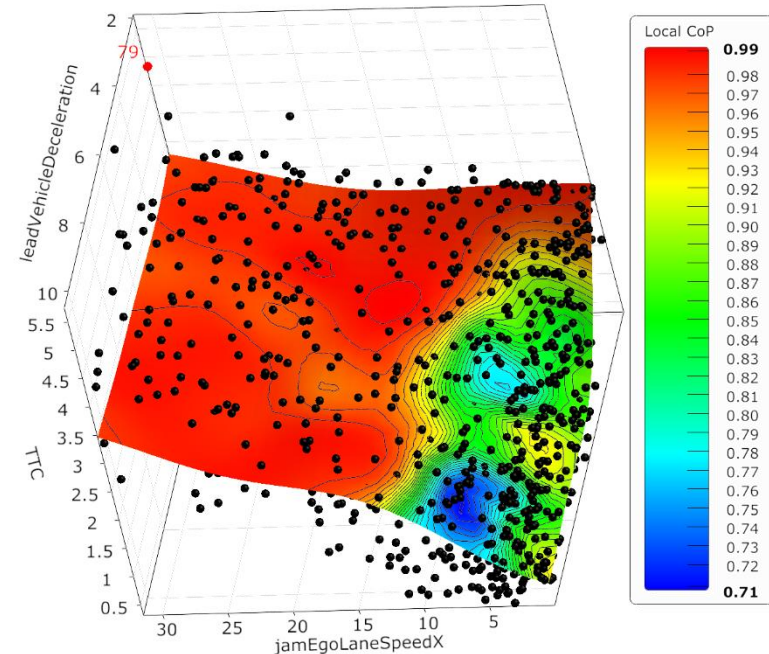
Analysis based on MOP (Metamodel of Optimal Prognosis)

- Partially low local CoPs (CoP – Coefficient of Prognosis)
- Assumption special physical and control mechanisms in these regions

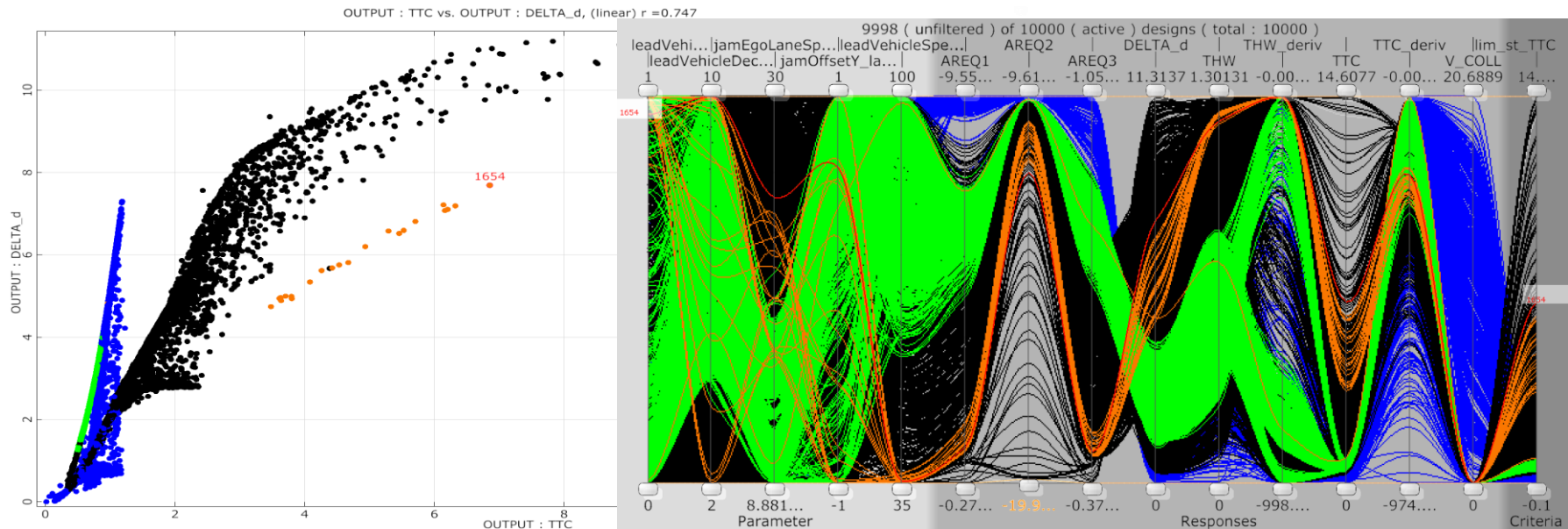
Isotropic Kriging approximation of TTC
Coefficient of Prognosis = 92 %



Isotropic Kriging approximation of TTC
Coefficient of Prognosis = 92 %



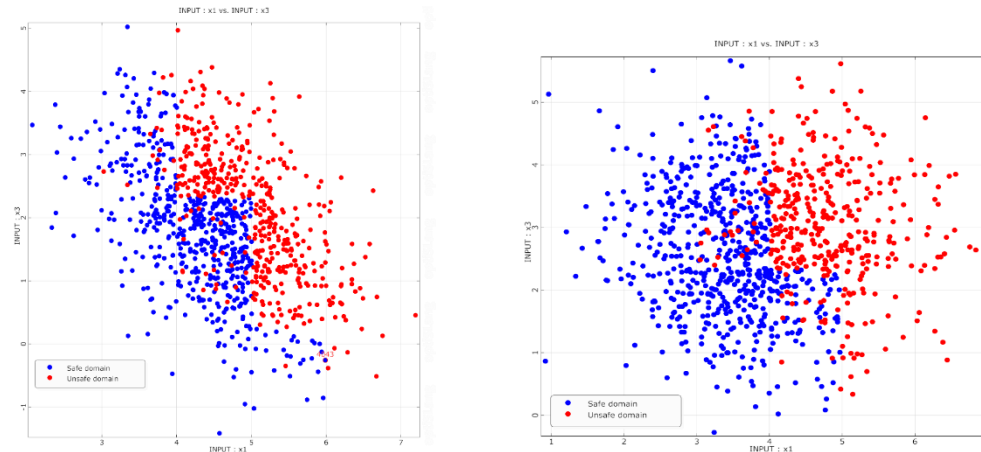
Analysis with Anthill and Parallel Coordinates Plots



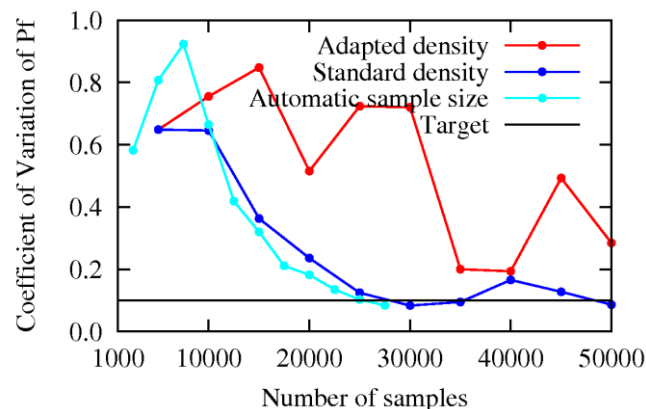
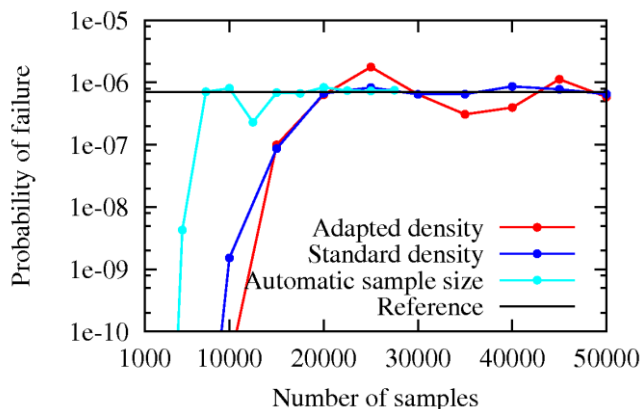
- Some output parameters are used for the steering and therefore have impact on other output parameters
- Analysis provided excellent indication which parameters are used for steering

Enhanced Adaptive Sampling

- Adaptation of mean values only, unity covariance matrix in Normal space



- Given a budget (no. of samples), the sample size per iteration is adapted to reach target standard error of results



20 variables,
max. 5000 samples/iteration

Comparision using the Enhanced Adaptive Sampling

- A factor of 1000 proved to be realistic for the reduction of the necessary simulation runs if using the enhanced adaptive sampling !*

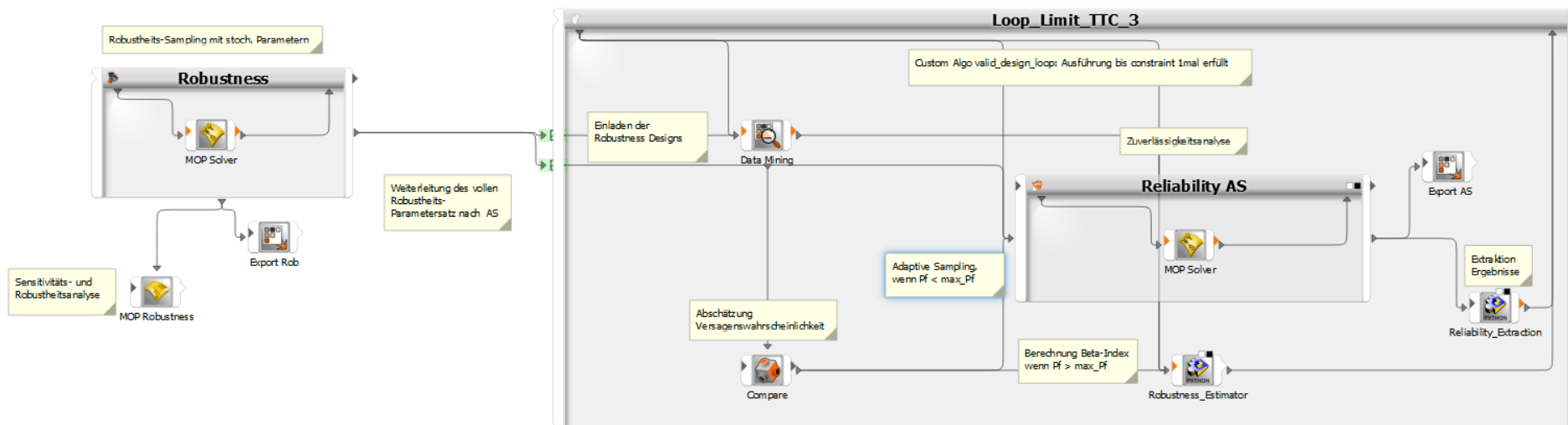
TTC = 1.0	Samples	Pf	CoV	Beta
MCS	30.000	$1.61 \cdot 10^{-2}$	4.5%	2.14
AS Standard	20.000	$1.55 \cdot 10^{-2}$	3.2%	2.16
AS Enhanced	8.000	$1.30 \cdot 10^{-2}$	5.8%	2.22

TTC = 0.5	Samples	Pf	CoV	Beta
MCS	14.010.000	$2.86 \cdot 10^{-5}$	5.0%	4.02
AS Standard	20.000	$2.55 \cdot 10^{-5}$	5.1%	4.05
AS Enhanced	16.000	$2.85 \cdot 10^{-5}$	8.4%	4.05

TTC = 0.4	Samples	Pf	CoV	Beta
MCS	39.420.000	$2.54 \cdot 10^{-6}$	10.0%	4.56
AS Standard	20.000	$3.68 \cdot 10^{-6}$	23.0%	4.48
AS Enhanced	16.000	$2.81 \cdot 10^{-6}$	9.1%	4.54

Automated Process

- Loop over threshold values (fragility curve) by custom algorithm
- Robustness sampling (before the loop)
- Estimate failure probability from robustness sample
- Start reliability analysis only for small probability
- Loop until minimal (target) probability is reached



- *Note: MOP on robustness samples should not be used here for parameter reduction*

**Thank you for
your attention!**

