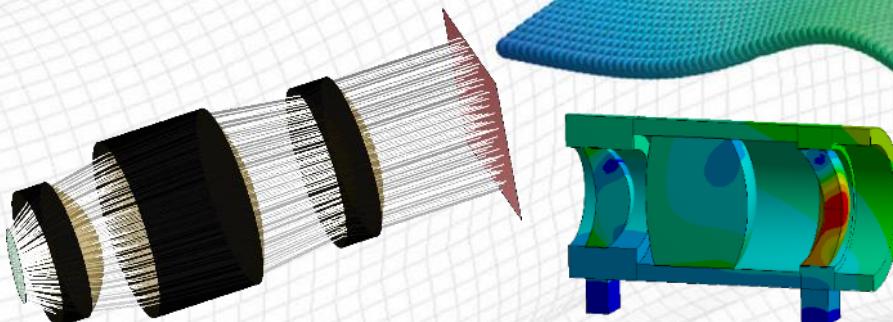


Robustheitsanalysen unter Berücksichtigung fertigungstechnischer Toleranzen für opto-mechanische Systeme

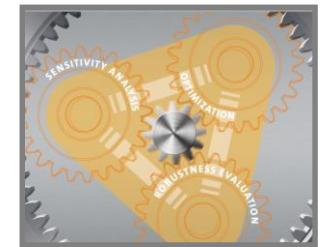
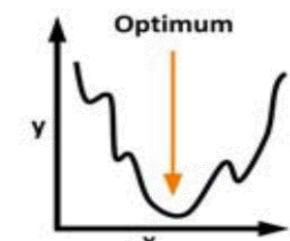
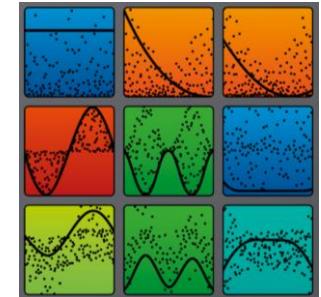
WOST Infotag:
„Fertigungsgerechtes optisches Design“

**Dr.-Ing. Bernd Büttner
Dr.-Ing. Stephanie Kunath
Dynardo GmbH, Weimar**



Motivation

- The **optimization of advanced optical designs** is very challenging due to their
 - complexity,
 - nonlinearity,
 - a huge number of input parameters and
 - interactions between them.
- The demands for the system's **performance** are
 - versatile and
 - very high and even get higher concerning optimization and robustness criteria.
- Furthermore, **totally new developments**, like
 - new materials,
 - manufacturing possibilities and
 - very short product development times,simultaneously, require advanced methodologies to develop competitive optical products.



Solution

- Dynardo supports the whole virtual product development process with software solutions including
 - Process integration
 - Building workflows
 - Automation
 - Robust Design Optimization

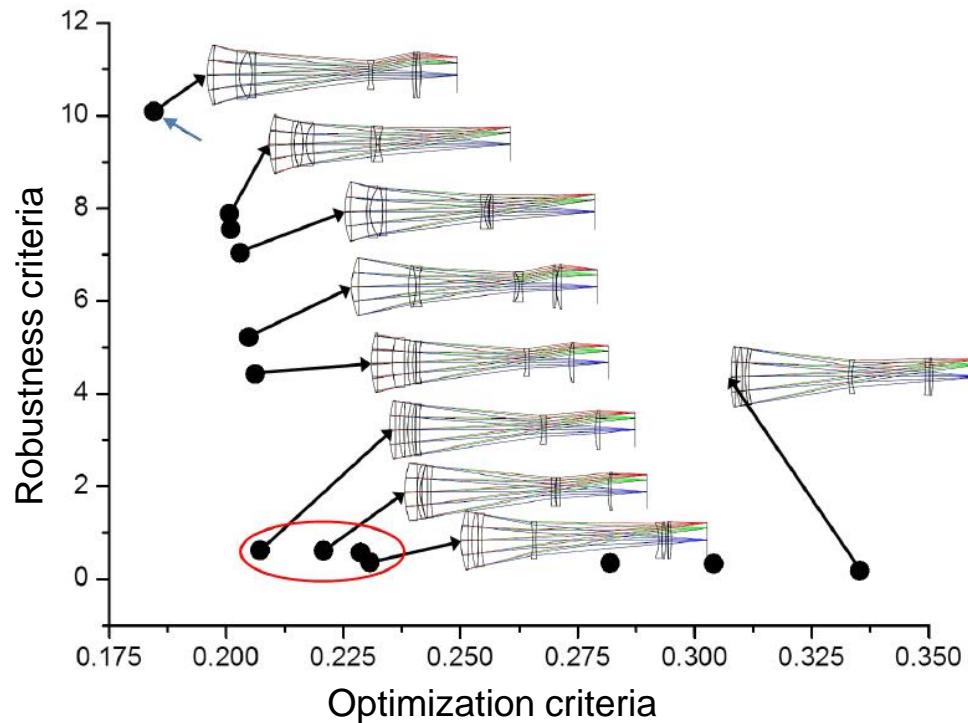


optiSLang



Robust Design Optimization of optical systems

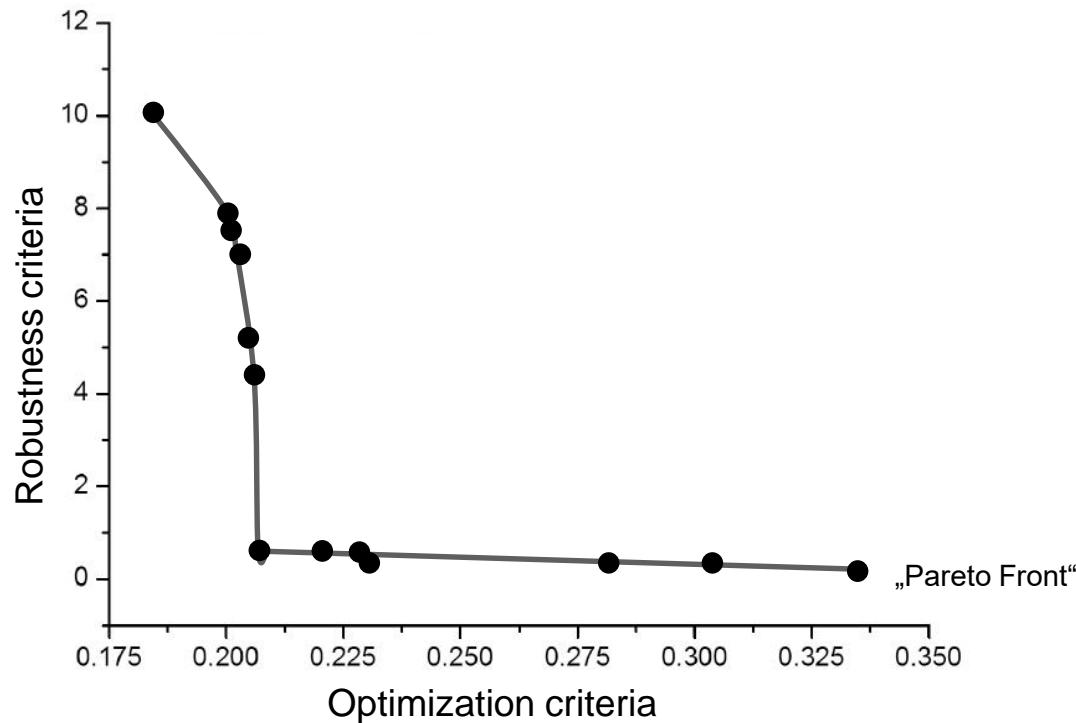
- Pareto optimization for the Cooke triplet problem
-> optimization criteria vs. robustness



B. Albuquerque, 2014, dissertation, „Multi-objective Memetic Approach for the automatic design of optical systems“

Robust Design Optimization of optical systems

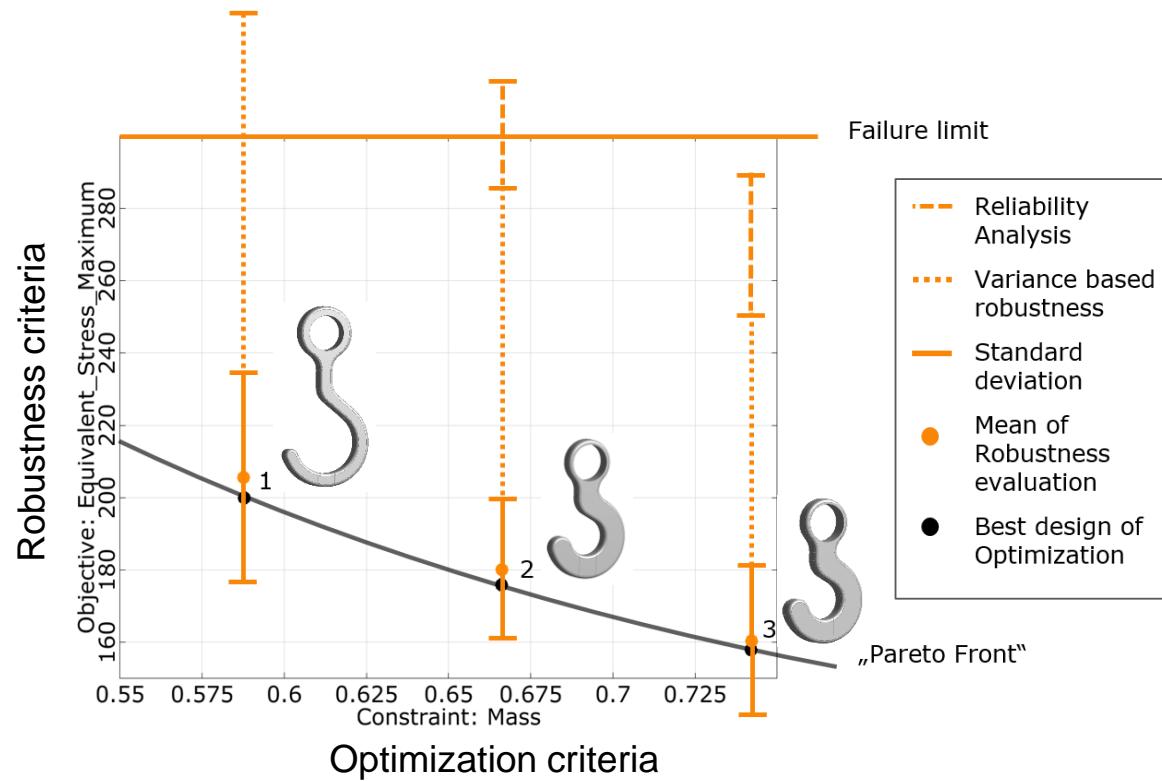
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Robust Design Optimization of mechanical systems

- “Pareto optimization” for a mechanical hook
-> optimization criteria vs. robustness

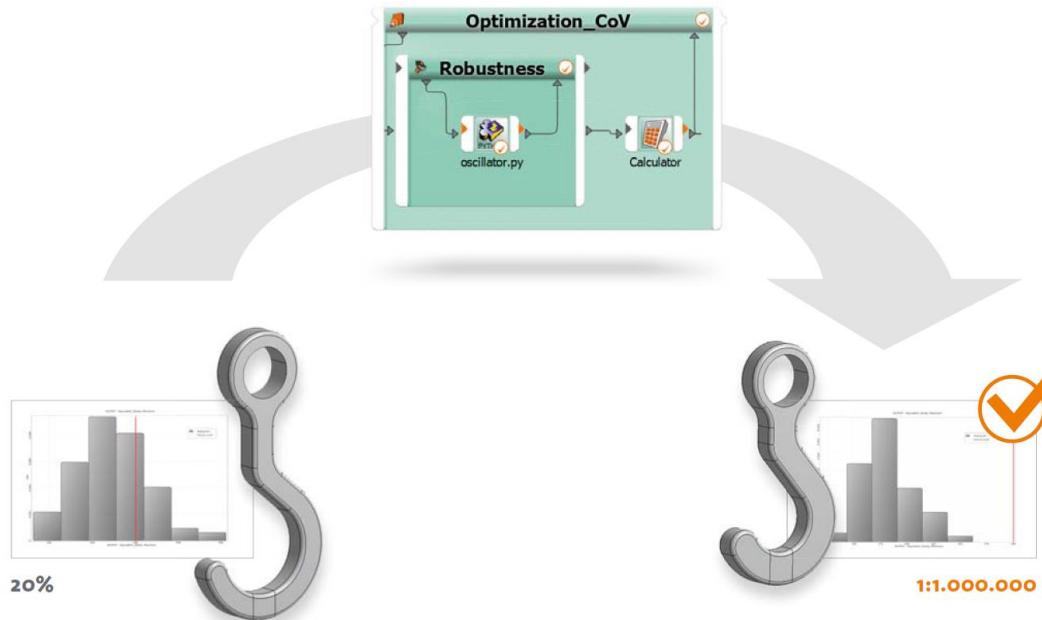


J. Will, T. Most, S. Kunath, 2014, NAFEMS, „Robust Design Optimization in Virtual Product Development“

https://www.nafems.org/publications/browse_buy/browse_by_topic/education/r0122-robust-design-optimization-in-virtual-product-development/

Robust Design Optimization of mechanical systems

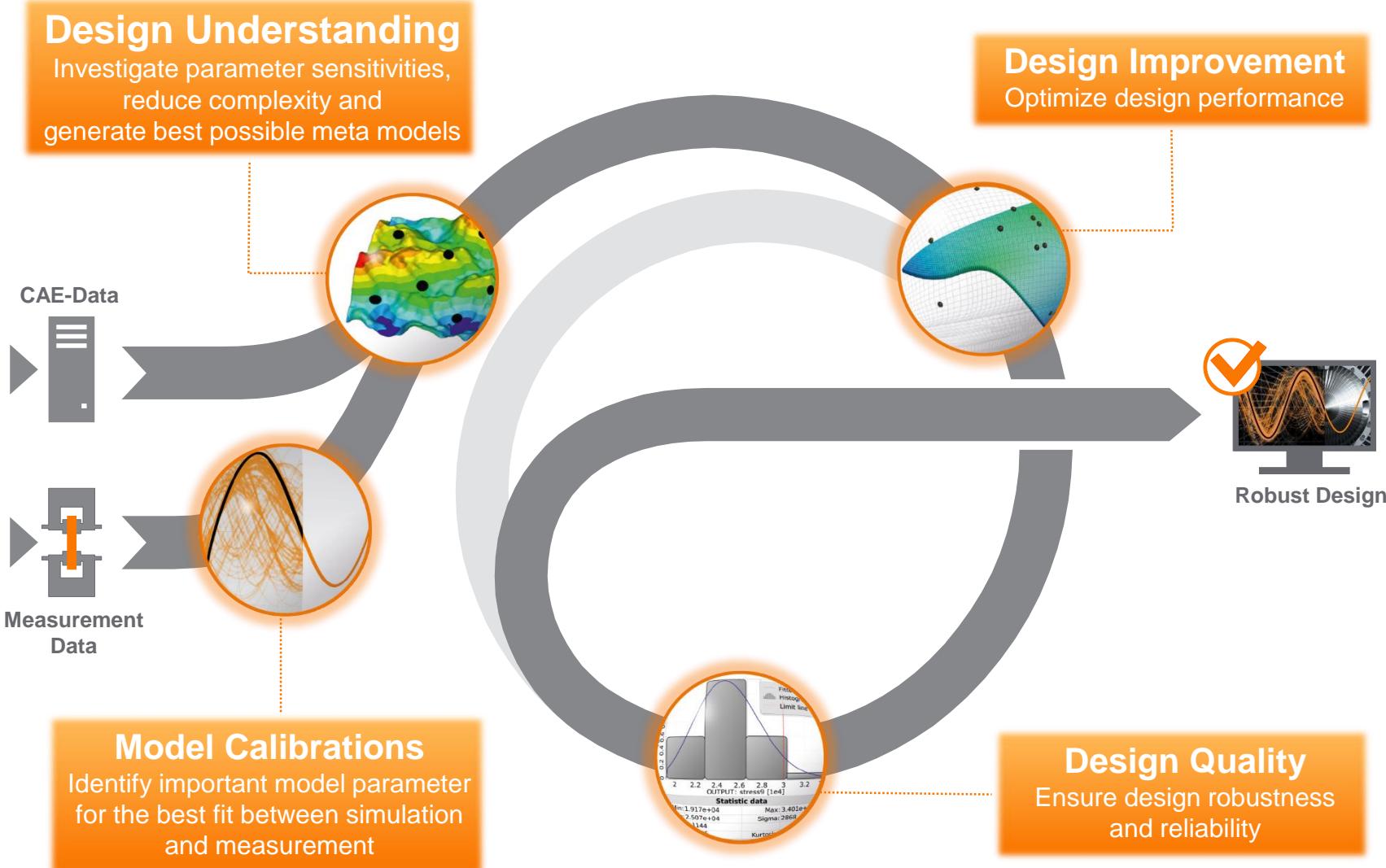
- “Pareto optimization” for a mechanical hook
 - > robustness criterium: *failure rate* was minimized from 22% to less than 1: 1.000.000
 - > optimization criterium: *mass* was minimized by 6%

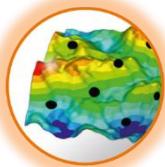


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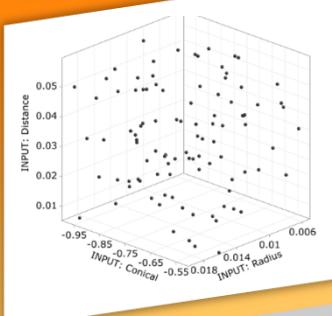




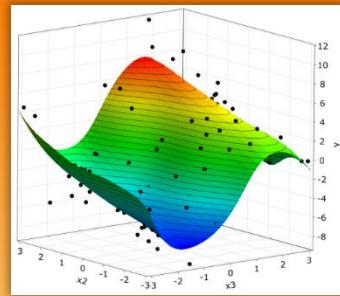
Sensitivity Analysis

Understand the most important input variables!

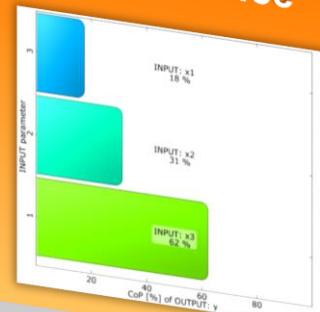
Latin Hypercube Sampling



Metamodel of Optimal Prognosis



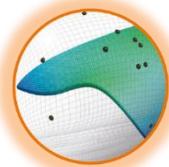
Input parameter importance



Automatic workflow

with a minimum of solver runs to:

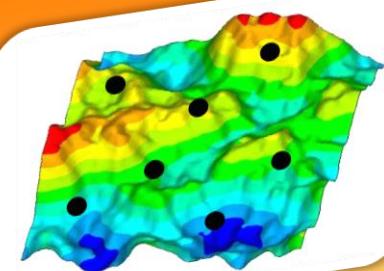
- identify the important parameters for each response
- Generate best possible metamodel (MOP) for each response
 - understand and reduce the optimization task
 - check solver and extraction noise



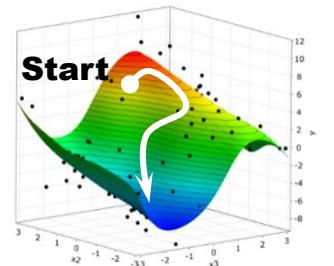
Optimization

Optimize your product design!

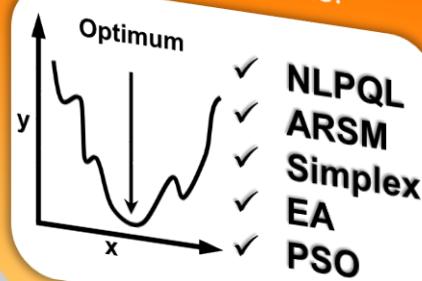
Sensitivity analysis



Optimization using MOP

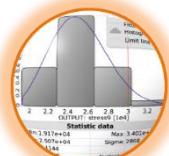


Direct Optimization with algorithms:



- work with the reduced subset
of only important parameters

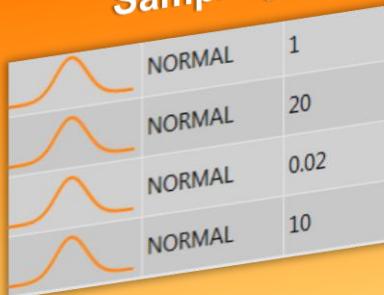
- pre-optimization on meta model (one additional solver run)
- optimization with leading edge optimization algorithms
 - decision tree for optimization algorithms



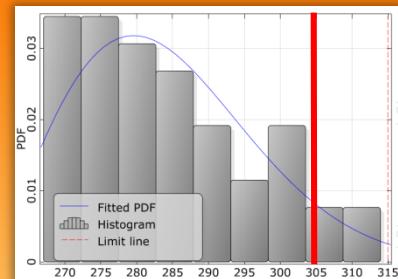
Robustness Evaluation

Ensure your product quality!

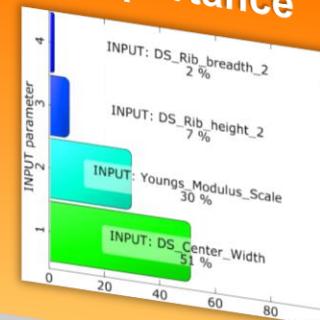
Latin Hypercube Sampling



Output parameter variation



Input parameter importance

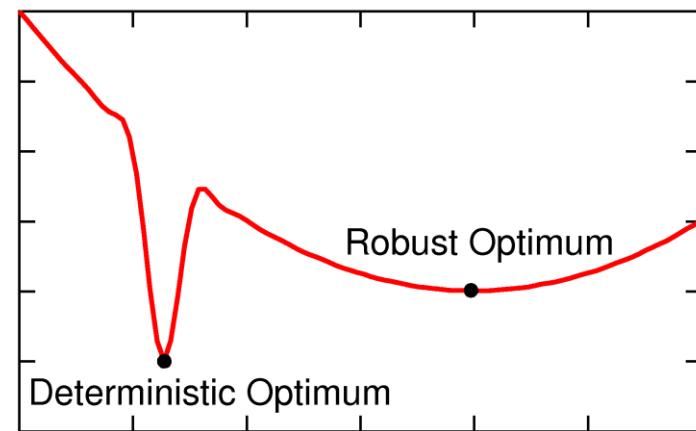
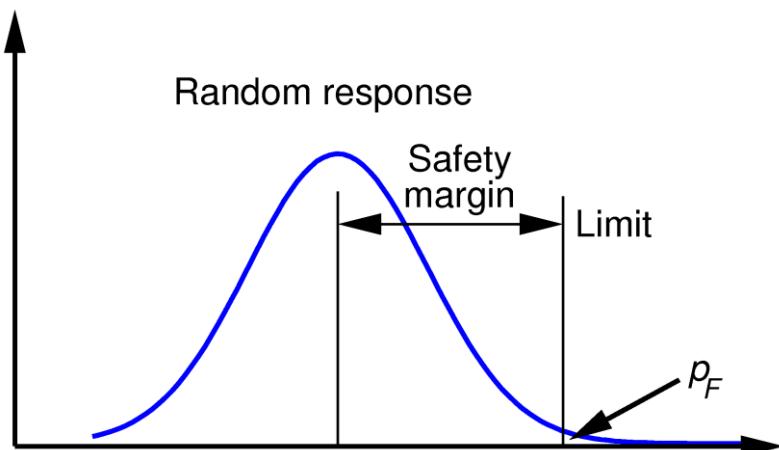


Powerful procedure to check design quality:

- LHS representing scattering variables optimally
- check variation interval limits and critical responses
- Identify the most important scattering variables

How to Define the Robustness of a Design?

- **Intuitively:** The performance of a robust design is largely unaffected by random perturbations
- **Variance indicator:** The coefficient of variation (CV) of the objective function and/or constraint values is smaller than the CV of the input variables



Robust Design Optimierung für optische Systeme



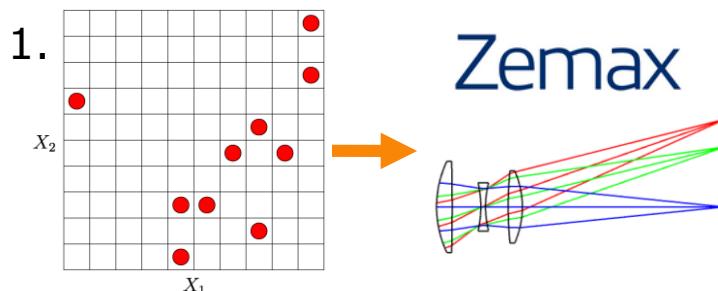
Tolerance Analysis vs. Robustness Analysis

- **Zemax Tolerance Analysis**

1. Monte Carlo (MC) analysis varies all factors at a time without sensitivity evaluation.
2. Local sensitivity analysis - „one factor at a time“
 - Assumption: all parameters are linear and independent

- **optiSLang Robustness Analysis** based on combination of MC analysis and sensitivity analysis

3. Improved MC-Sampling (Latin Hypercube Sampling based on 100 designs)
4. Calculates “global” sensitivities based on metamodels.



Tolerance Analysis vs. Robustness Analysis

- **Zemax Tolerance Analysis**

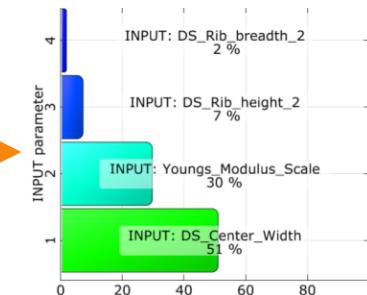
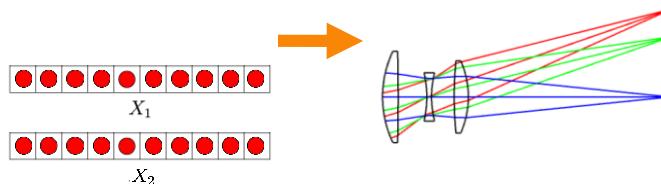
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2.

Zemax



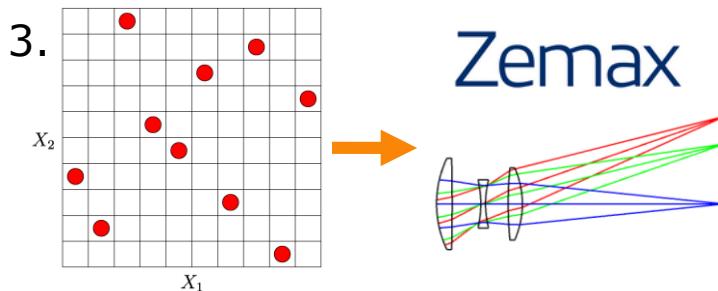
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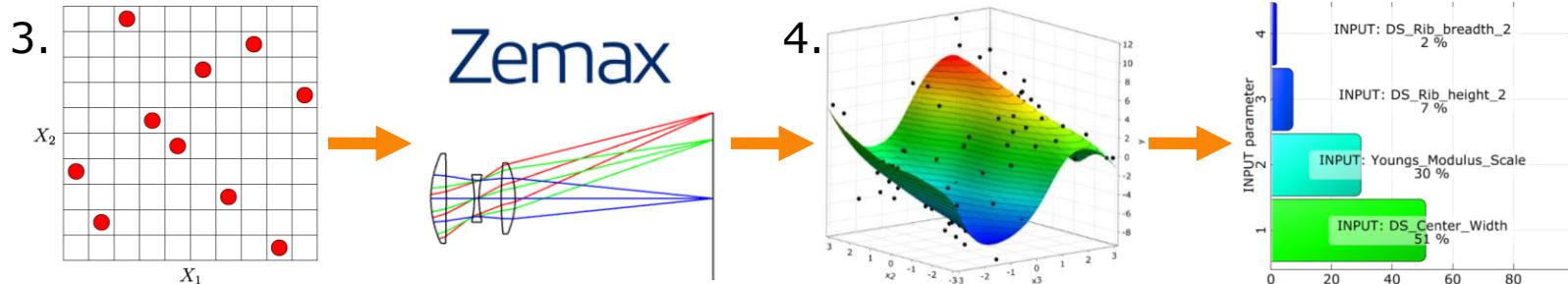
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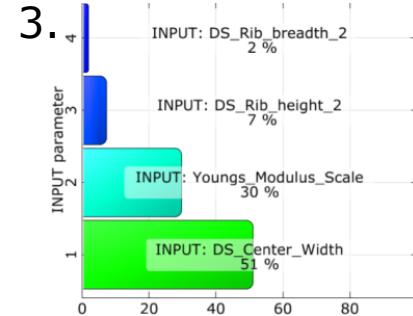
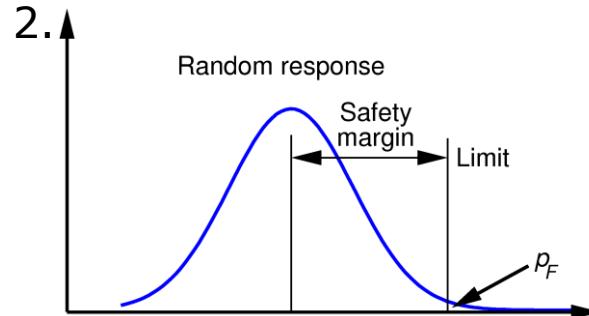
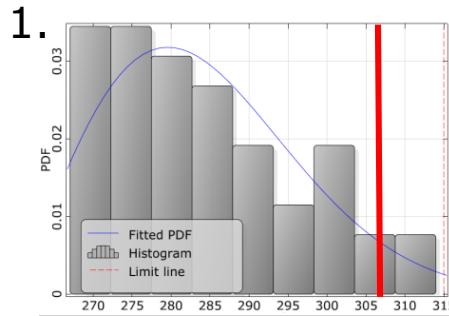
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Robustness Analysis – optISLang approach

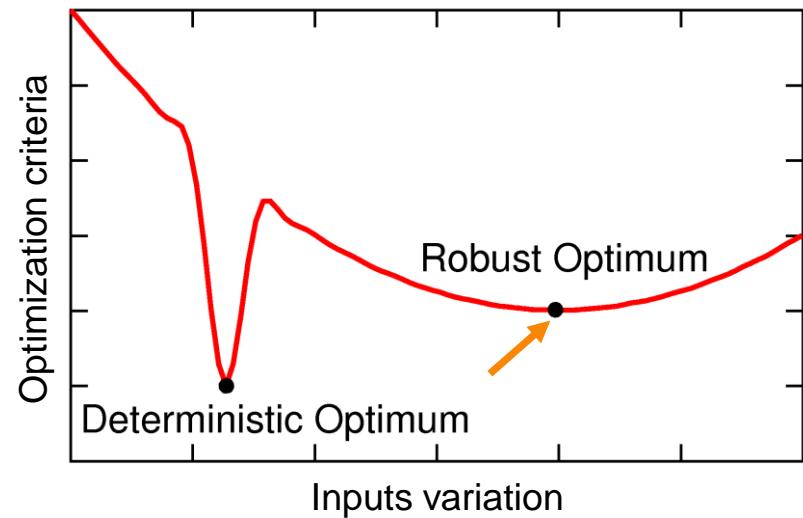
- Investment of \approx **100 designs**
- More **realistic modelling** of the scattering behavior as all possible distributions and correlations between input parameters can be modelled
- Results for each output/ merit:
 1. Observed scattering
 2. Quantify the probability of failure by defining limits based on specs
 3. Global sensitivities of inputs
 - > Detection of causes
 - > Identify critical/ non-critical inputs



Robustness Analysis with Optimization

- Strategies:

1. **Iterative RDO approach:** first Optimization, then Robustness analysis
 - a. Reduction of critical input scattering
 - b. Subsequent Optimization with changed constraints
2. **Coupled RDO approach:** Optimizer contains optimization and robustness criteria as
 - a. Constraint
 - b. Second merit function



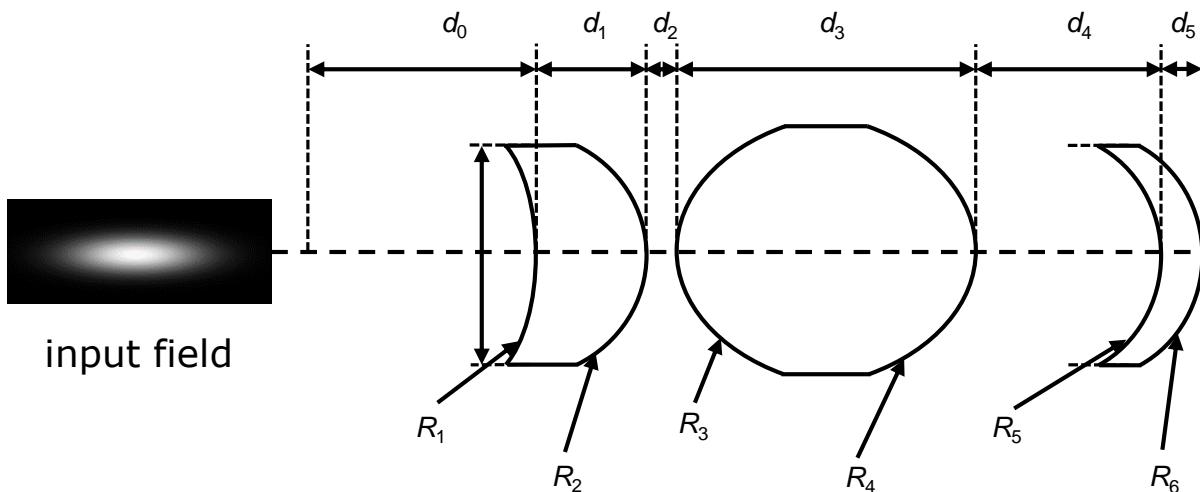
Robust Design Optimierung für optische Systeme



Beispiel

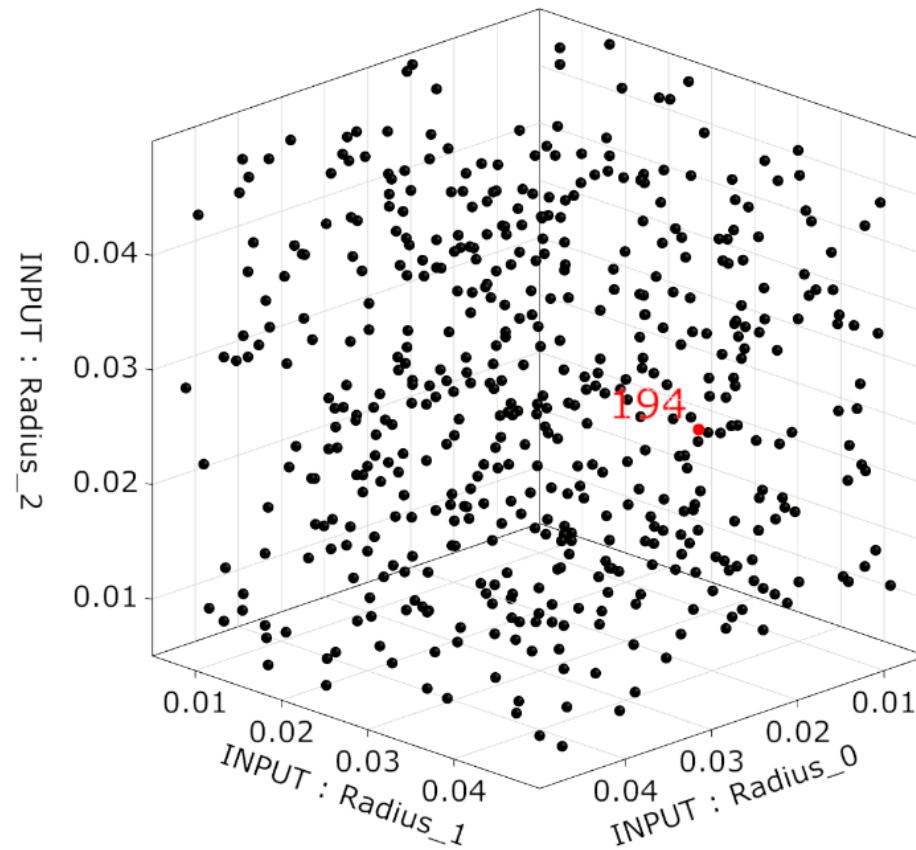
Problem Description

- Collimation of Diode Laser Beam by Objective Lens
- **Optimization objective:**
 - Minimize *divergence angle* in x and y direction
 - Minimize m^2 to be close to 1 in x and y direction
- **Robustness criteria:**
 - Coefficient of Variation (CoV) of *divergence angle* and m^2 in x and y direction should not exceed 20%



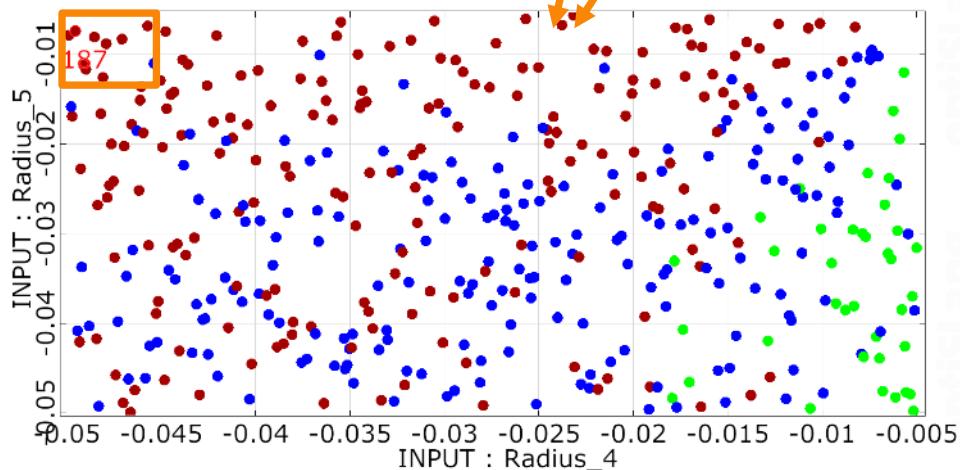
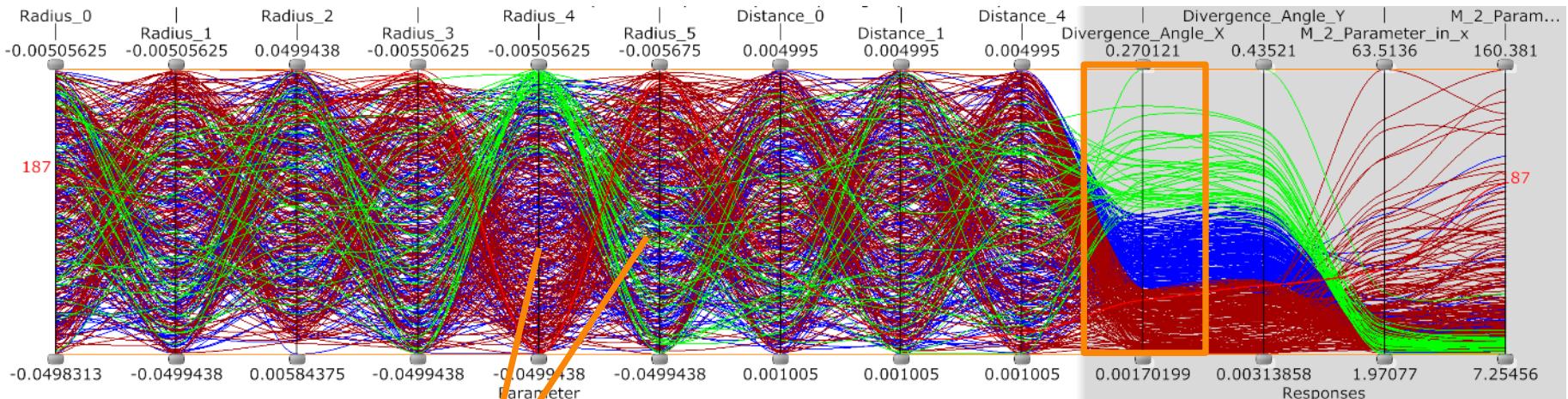
Inputs and Sampling

- 500 designs sampled with Advanced Latin Hypercube Sampling
- Inputs: 6 radii, 5 distances



Design Exploration

- Interactive Postprocessing: Cluster Analysis

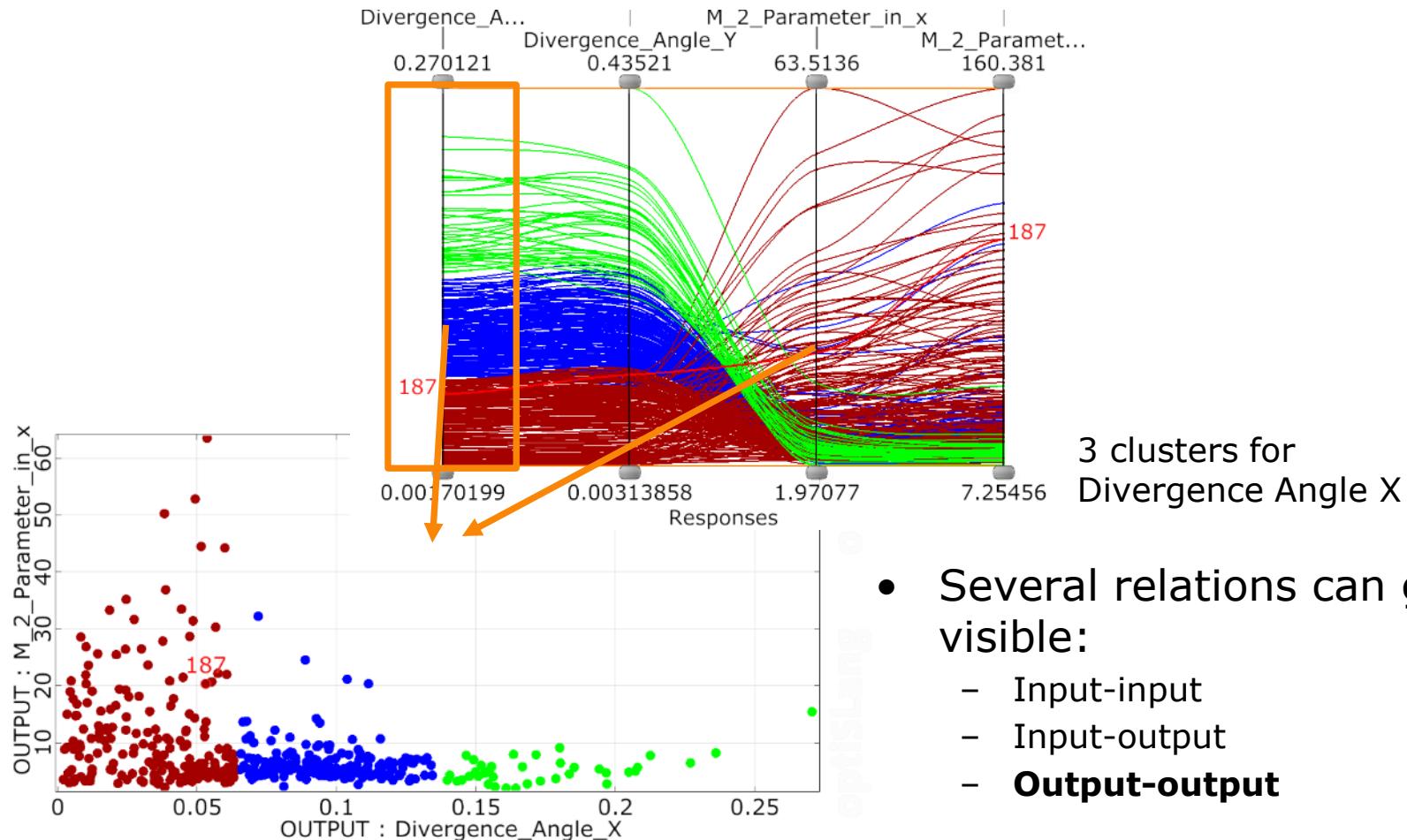


3 clusters for
Divergence Angle X

- Several relations can get visible:
 - Input-input**
 - Input-output**
 - Output-output

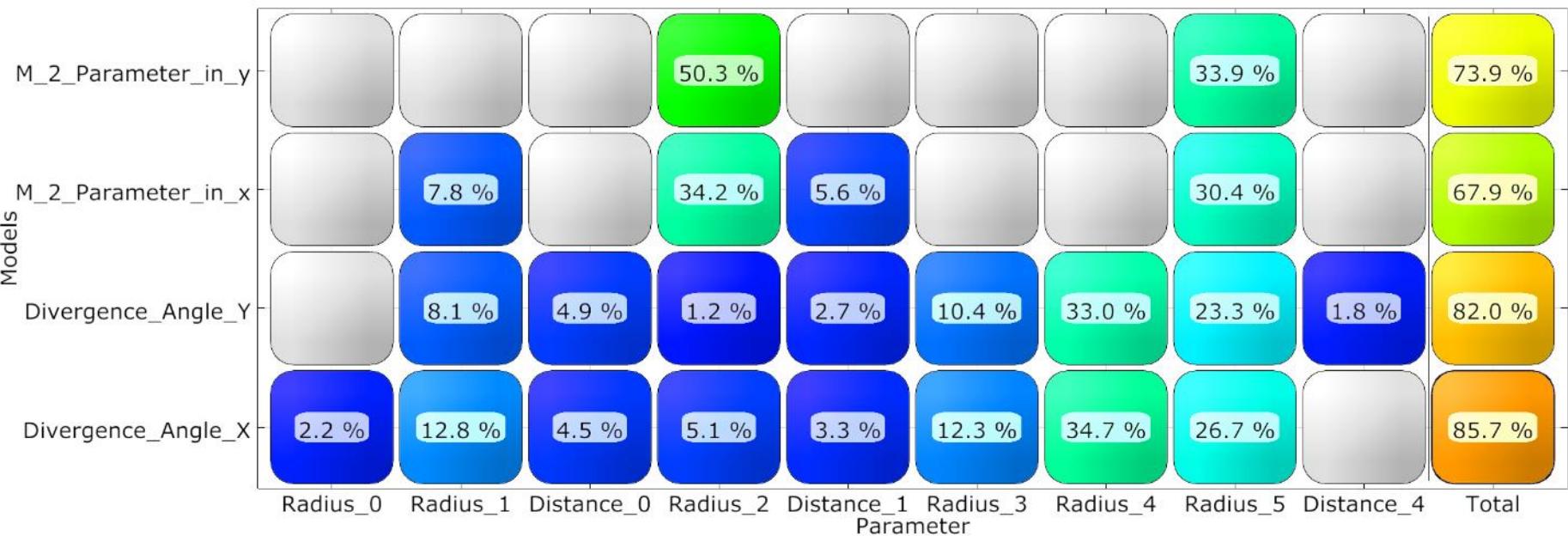
Design Exploration

- Interactive Postprocessing: Cluster Analysis



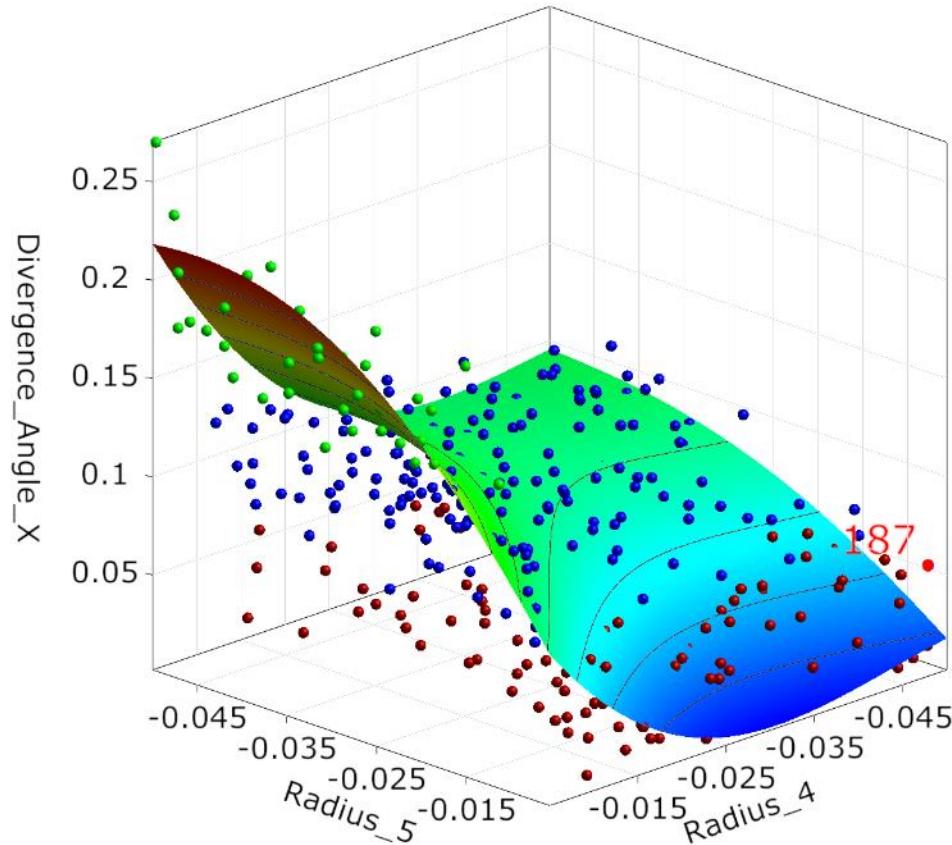
Metamodelling

- Beam parameters obtained by field tracing can be described quite well ($\text{CoP} > 70\%$), influence of radii is dominant
- **Fast pre-optimization on metamodel (MOP) is possible**



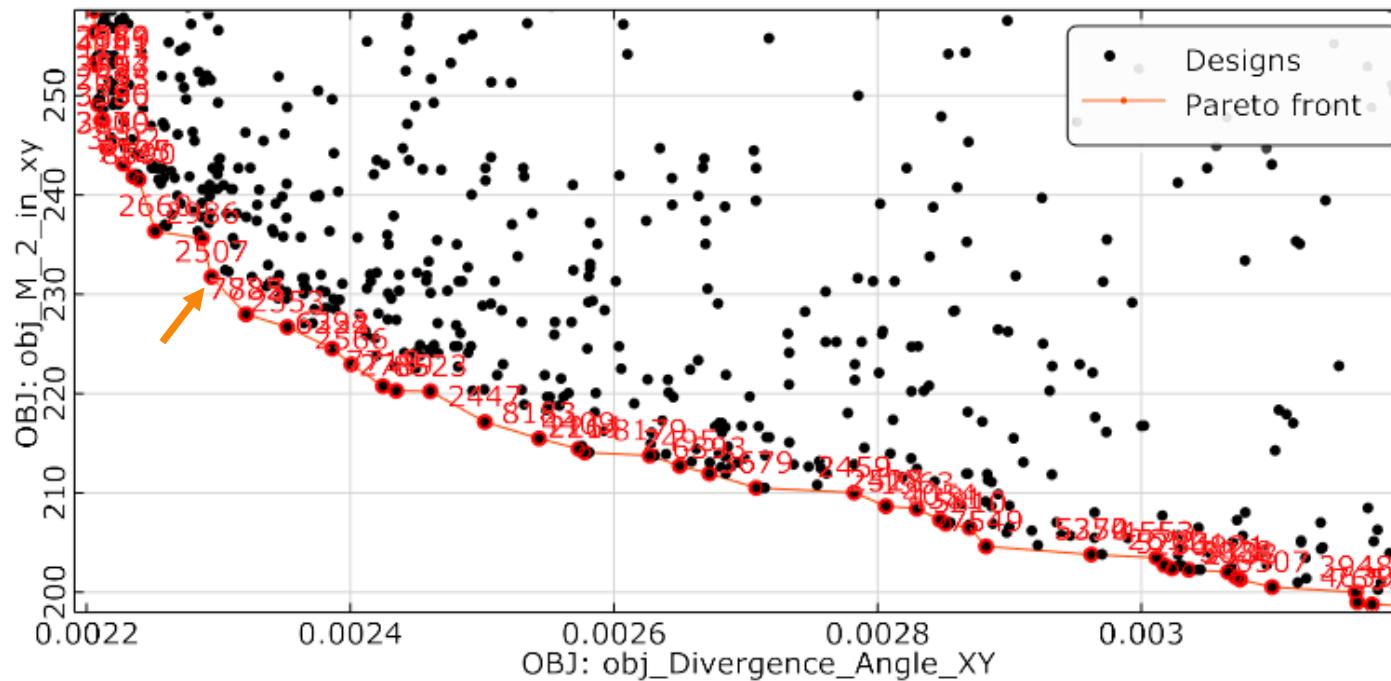
Metamodelling

- **Metamodel of Divergence Angle X:**
The lower radius 5 the lower the divergence angle!
An intermediate radius 4 leads to a low divergence angle!



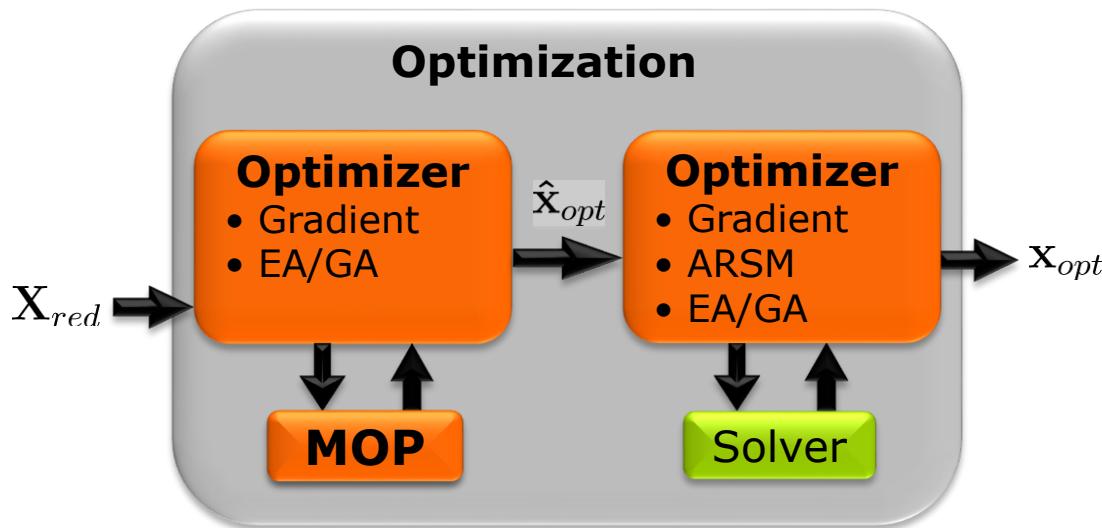
Pareto Optimization

- **Pareto optimization** on metamodel with the following objective functions:
 - Minimize $Divergence_Angle_Y+Divergence_Angle_X$
 - Minimize $(M_2_Parameter_in_x-1)^2+(M_2_Parameter_in_y-1)^2$
 - Best design can be chosen from the Pareto front and used as start design for further direct optimization



Direct Optimization

- **Direct optimization** based on best design of Pareto optimization



Optimized outputs	Value & Unit
wavefront error (RMS)	0.03λ
divergence Angle X x Y	$0.02^\circ \times 0.01^\circ$
M ² parameter in X x Y direction	1.0180×1.1802

Optimized inputs	Value & Unit
Radius 0	-0.00679898m
Radius 1	-0.00390681m
Radius 2	0.0210514m
Radius 3	-0.00873955m
Radius 4	-0.00504888m
Radius 5	-0.0070837m
Distance 0	0.00200701m
Distance 1	0.000967461m
Distance 2	0.00600046m
Distance 3	0.00448916m
Distance 4	0.00108139m

Robustness Analysis: Inputs

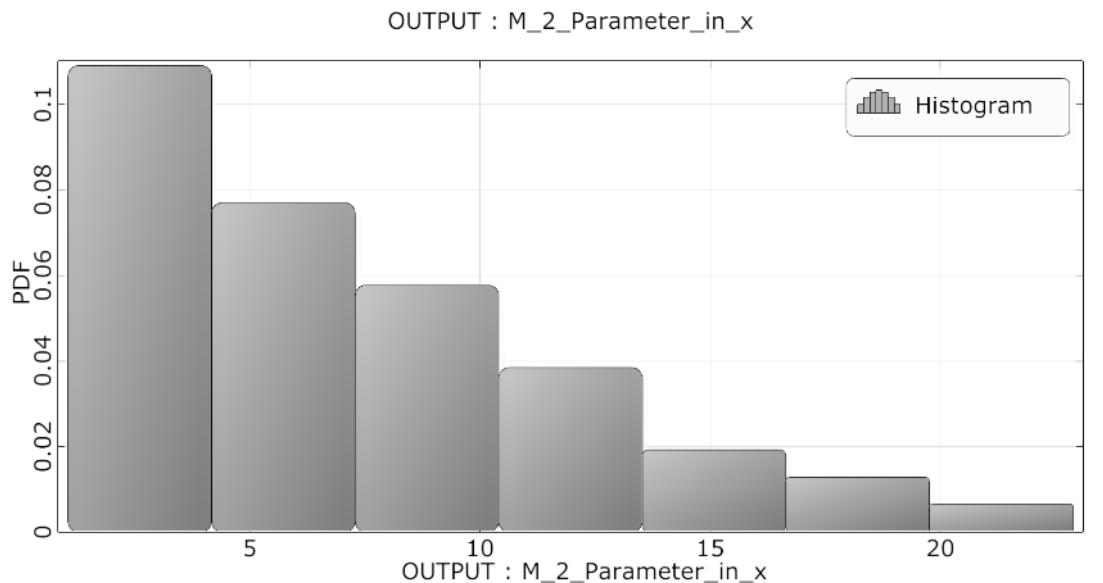
- Robustness analysis:** Definition of scattering input parameters

Name	PDF	Type	Mean	Std. Dev.	CoV
Distance_0		NORMAL	0.00200701	2.00701e-05	1 %
Distance_1		NORMAL	0.000967461	4.83731e-05	5 %
Distance_2		NORMAL	0.00600046	6.00046e-05	1 %
Distance_3		NORMAL	0.00448916	0.000224458	5 %
Distance_4		NORMAL	0.00108139	1.08139e-05	1 %
Distance_Before		NORMAL	0.0036915	0.000184575	5 %
Lateral_Shift_X		NORMAL	0	1e-05	100 %
Lateral_Shift_Y		NORMAL	0	1e-05	100 %

Name	PDF	Type	Mean	Std. Dev.	CoV
Radius_0		NORMAL	-0.00679898	3.39949e-05	0.5 %
Radius_1		NORMAL	-0.00390681	1.9534e-05	0.5 %
Radius_2		NORMAL	0.0210514	0.000105257	0.5 %
Radius_3		NORMAL	-0.00873955	4.36978e-05	0.5 %
Radius_4		NORMAL	-0.00504888	2.52444e-05	0.5 %
Radius_5		NORMAL	-0.0070837	3.54185e-05	0.5 %

Robustness Analysis: M² in x

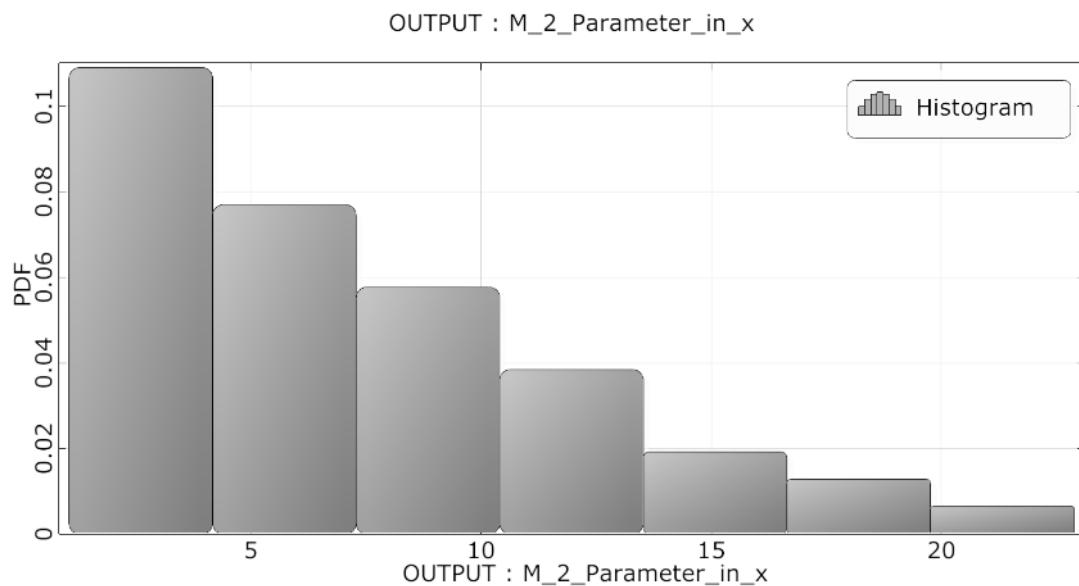
- **Optical design is not robust** in terms of M^2 ($CoV = 71\%$!) due to the variation of the lateral shift



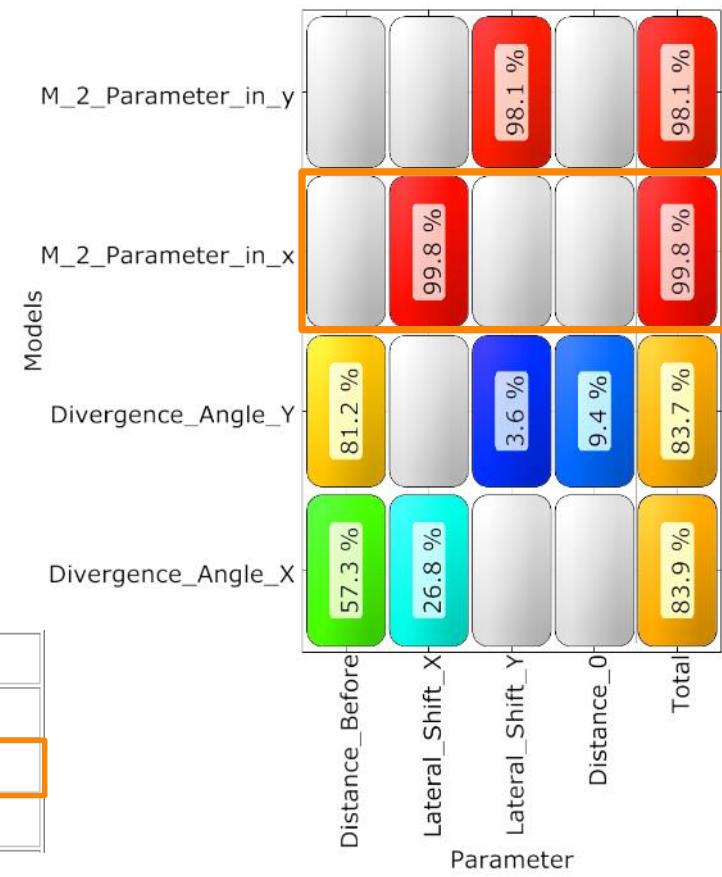
Statistical data			
Min:	1.02217		Max: 22.8507
Mean value:	7.24983	Standard deviation:	5.16479
CoV:	0.712401		

Robustness Analysis: M² in x

- Optical design is not robust** in terms of M^2 ($CoV = 71\%$!) due to the variation of the lateral shift

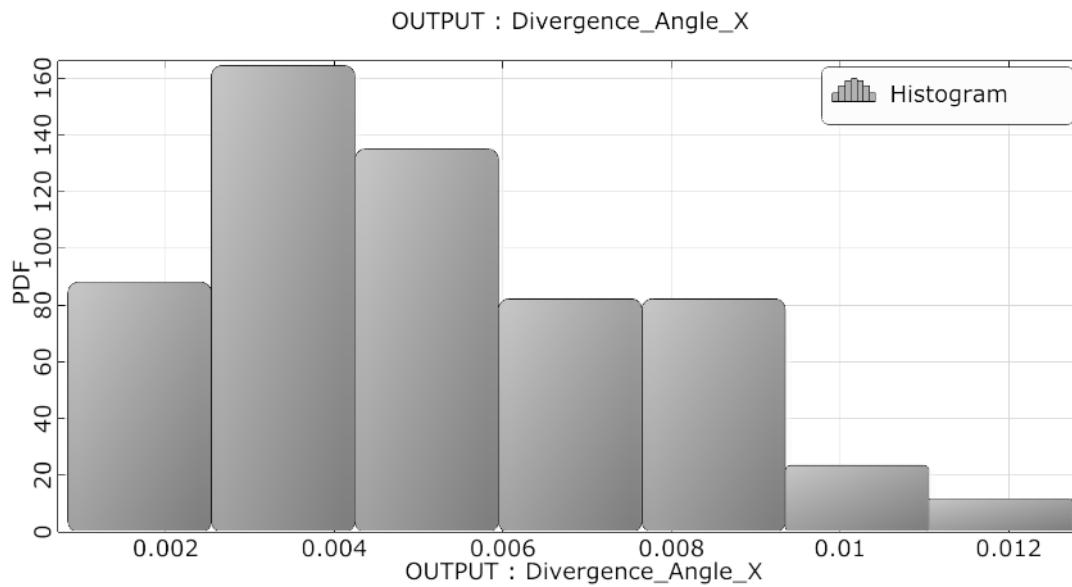


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Min:	1.02217	Max:	22.8507
Mean value:	7.24983	Standard deviation:	5.16479
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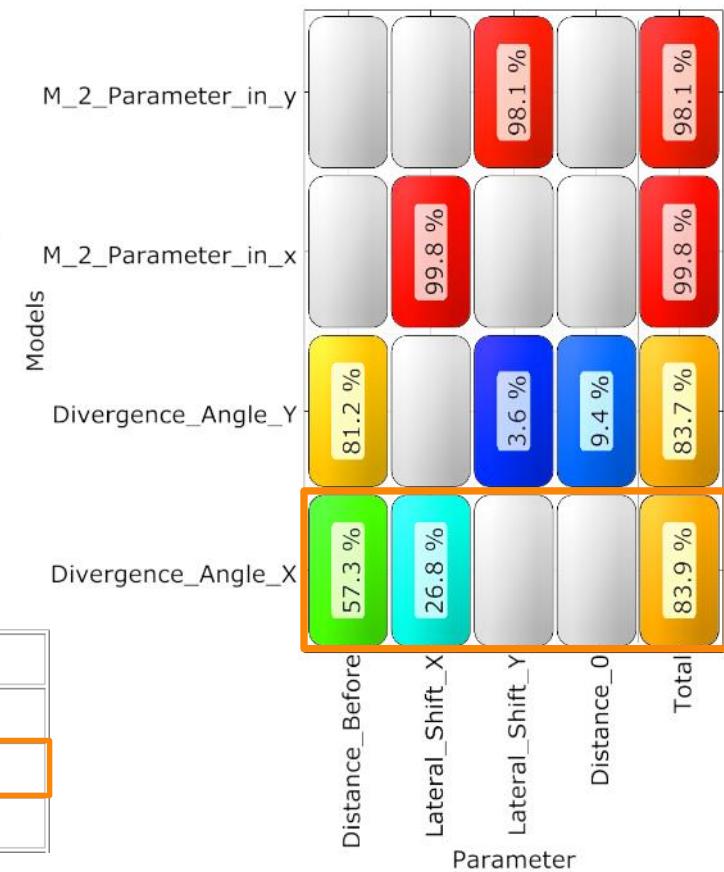


Robustness Analysis: Divergence Angle in x

- Optical design is not robust** in terms of divergence angle ($\text{CoV} = 51\%!$) due to the variation of the lateral shift and distance before lens

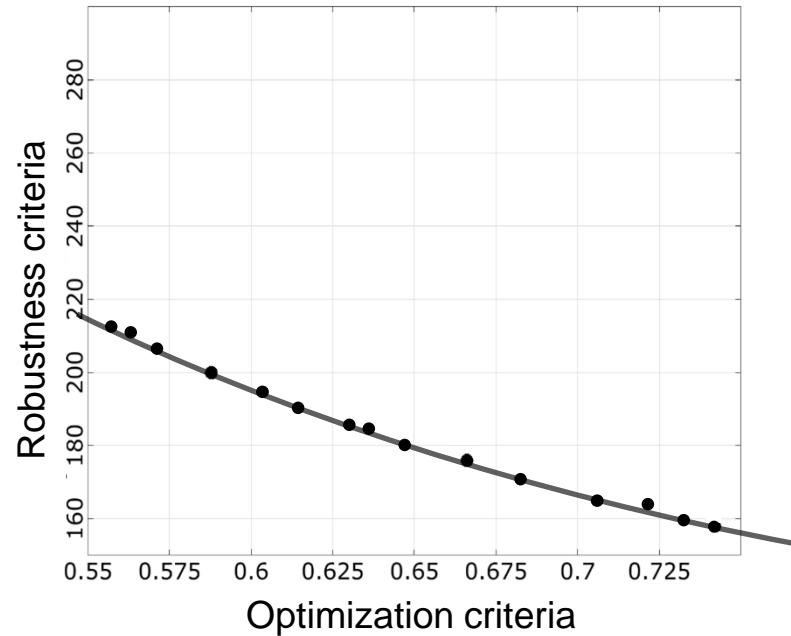


Statistical data			
Min:	0.00082438	Max:	0.0127391
Mean value:	0.00505156	Standard deviation:	0.0025927
CoV:	0.513247		



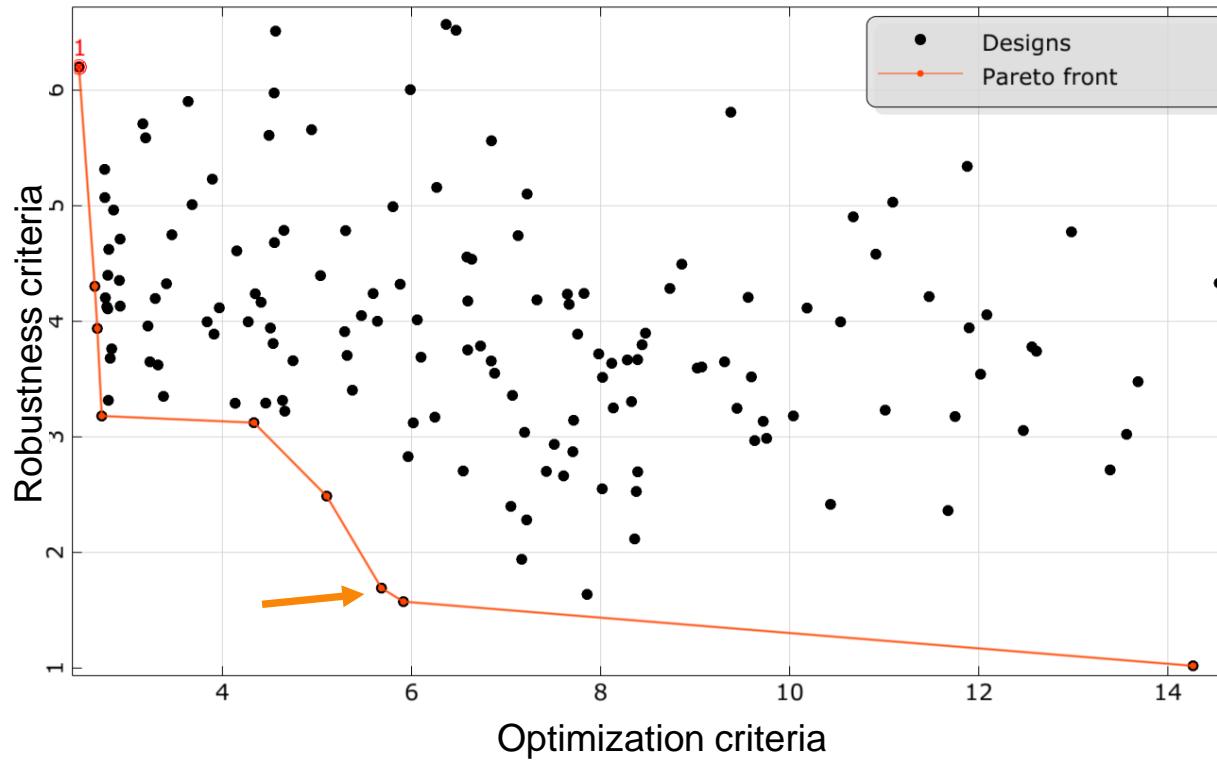
Robustness Analysis

- If design is not robust...
 1. **Iterative RDO approach:** first Optimization, then Robustness analysis
 - a. Reduction of critical input scattering
 - b. Second Optimization with changed constraints
 2. **Coupled RDO approach:** Optimizer contains optimization and robustness criteria as
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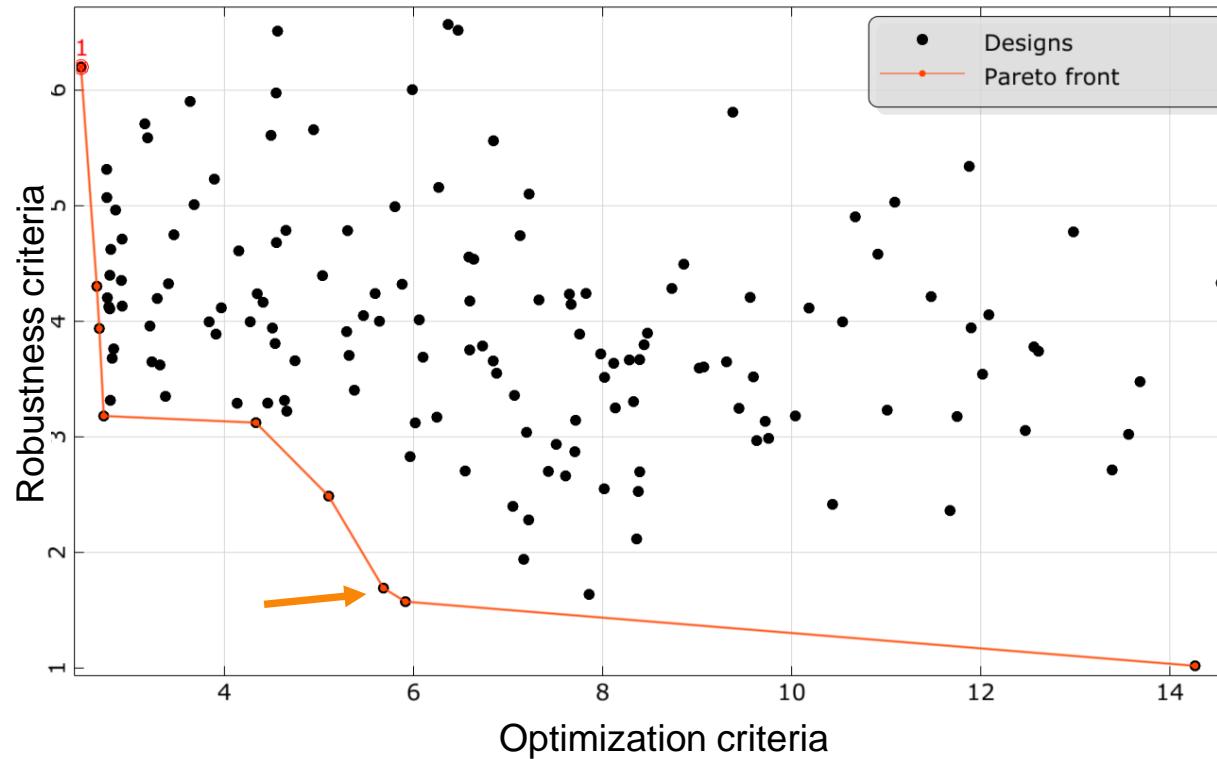
Coupled Robust Design Optimization

- **Optimization criteria:** weighted merits in one objective function
- **Robustness criteria:** weighted standard deviation of merits in second objective function



Coupled Robust Design Optimization

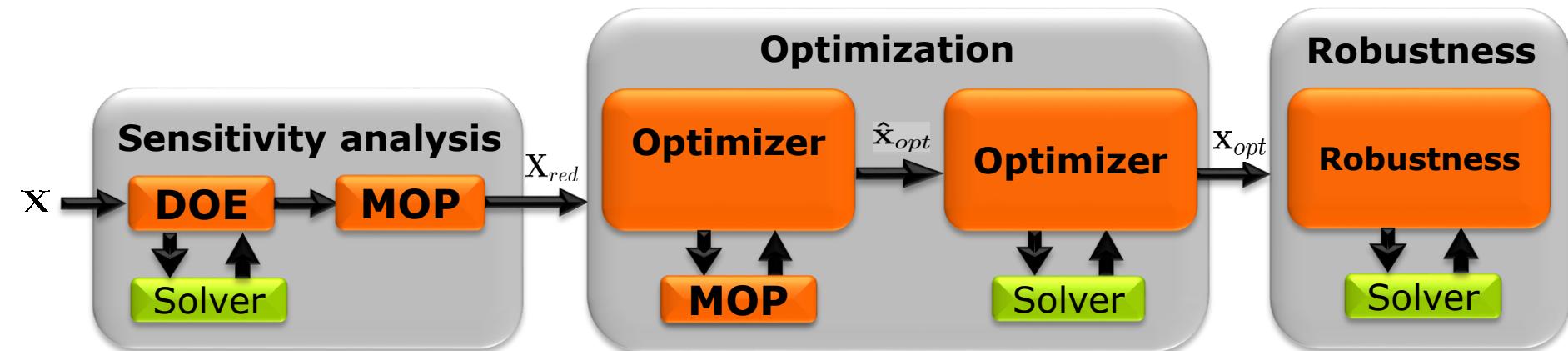
- **Further steps:**
 - Check value of inputs
 - Check performance of each output parameter



Summary: Robust Design Optimization

- **Workflow:**

1. Sensitivity analysis
 - Correlation and cluster analysis
 - MOP generation
2. Optimization on MOP using best design from sensitivity analysis
3. Optimization with direct solver calls using start design from previous optimization on MOP
4. Robustness analysis
5. Coupled or iterative Robust Design Optimization

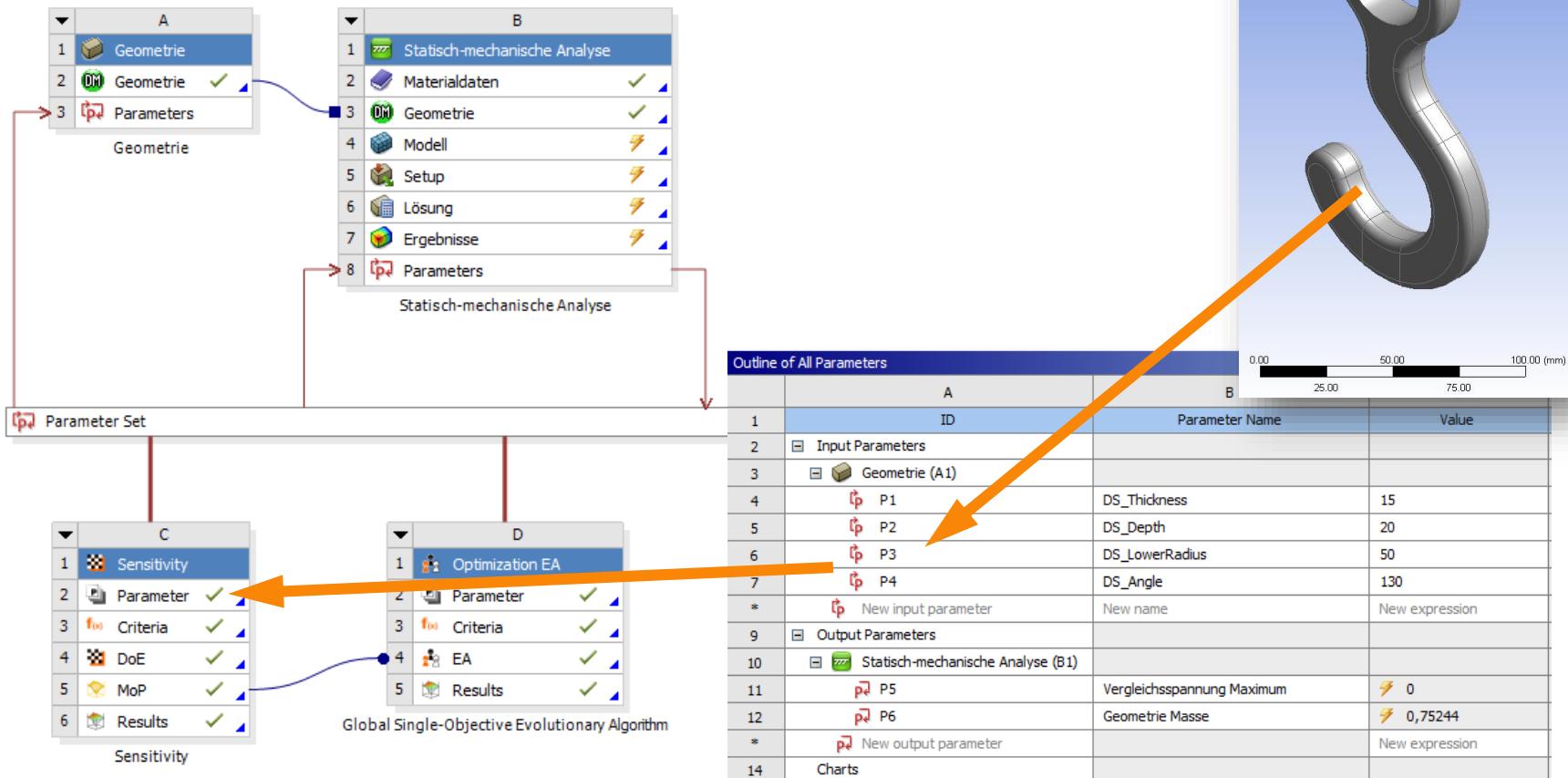


RDO für opto-thermo-mechanische Systeme



Full Integration of optiSLang in ANSYS Workbench

- optiSLang modules **Sensitivity**, **Optimization** and **Robustness** are directly available in ANSYS Workbench



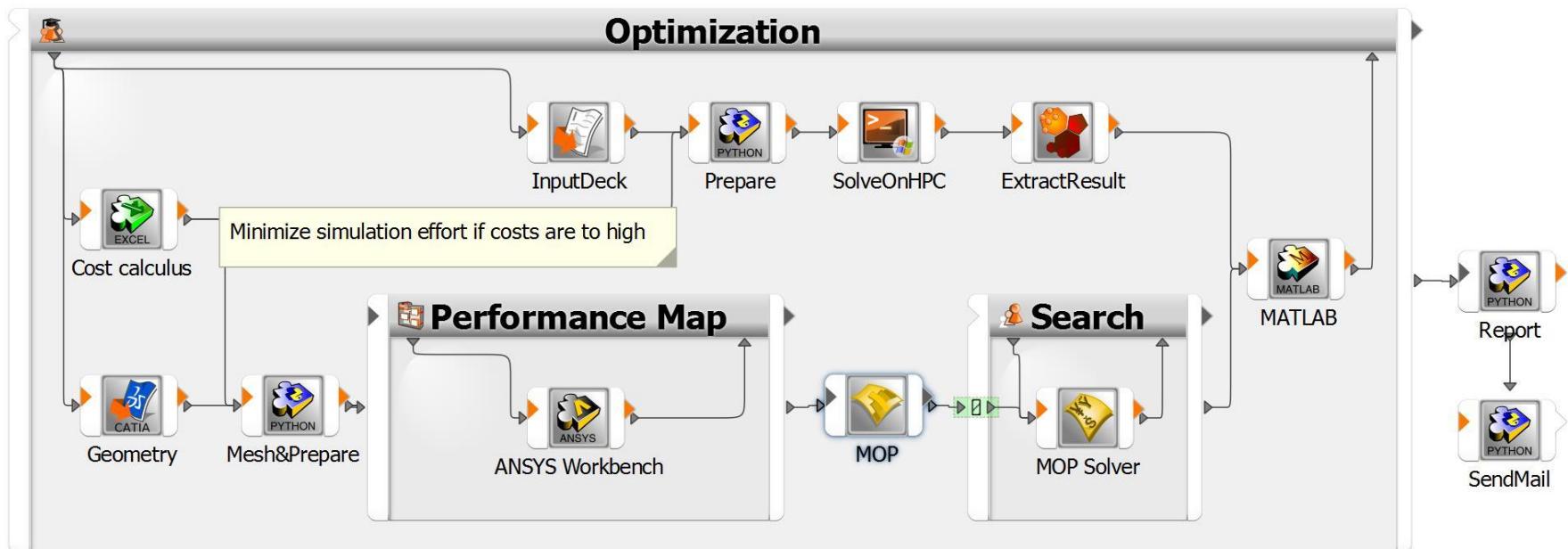
Integration of optics tools in optiSLang



Zemax

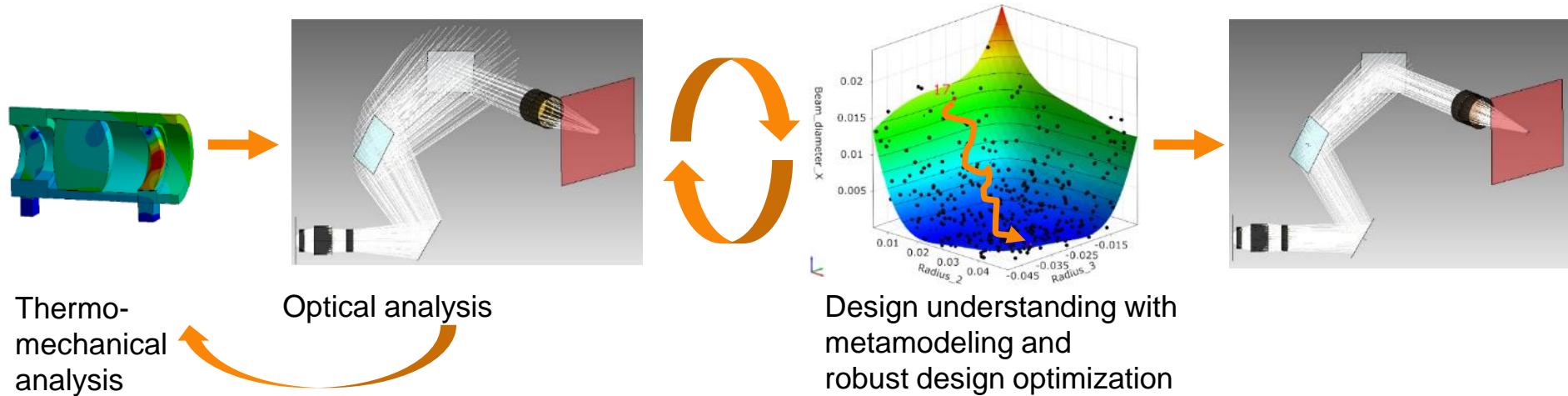
Workflow generation

- Building of complex workflows based on several simulation tools possible
- ANSYS Workbench can be coupled with different other solvers like Zemax, MATLAB or VirtualLab



Opto-Thermo-Mechanical simulation

1. Integration optical and mechanical simulation tools (e.g. Zemax, VirtualLab, ANSYS, Abaqus,...) in optiSLang
2. Built up complex workflows
3. Automation of workflows
4. Robust Design Optimization
 - Sensitivity Analysis
 - Optimization
 - Robustness Analysis



Thank you for your attention!

For more information
please visit our homepage:
www.dynardo.com



Thank you for your attention!



Bernd Büttner

Technical Engineer bei Dynardo
GmbH



Stephanie Kunath

Business Development Manager bei
Dynardo GmbH

