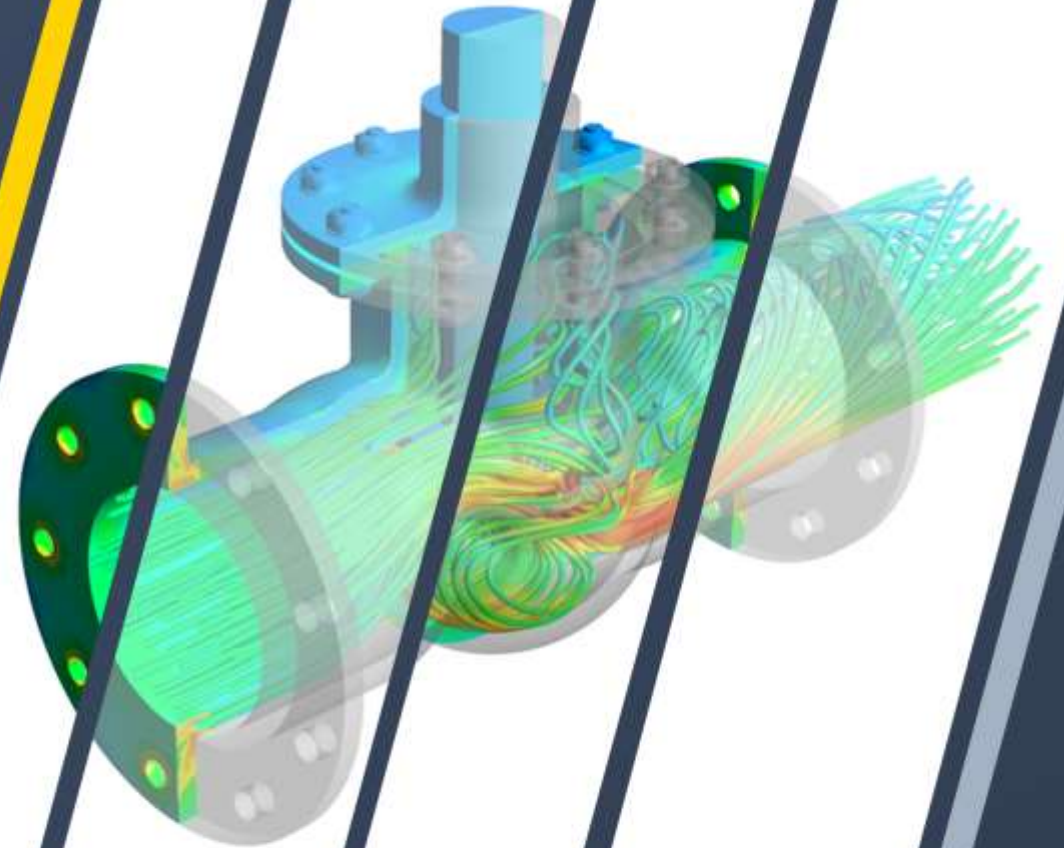




Calibration of the GEKO-Turbulence-Model Parameter with optiSLang

Johannes Einzinger



Agenda

Turbulence Modelling at a Glance

Generalized k-Omega Model (GEKO)

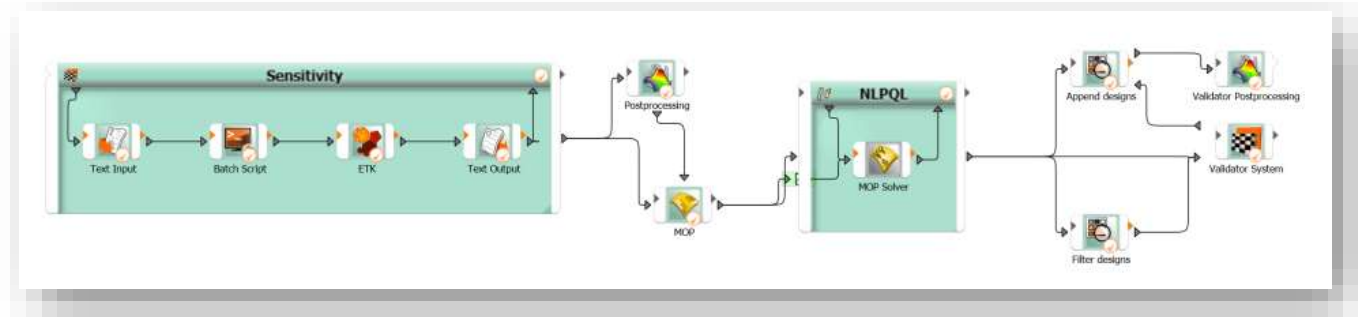
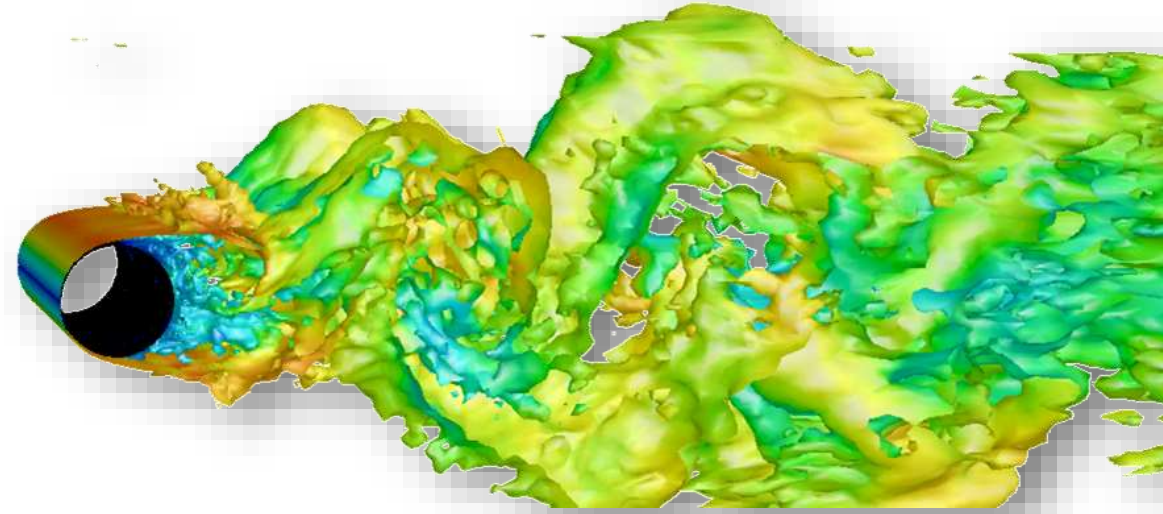
Parameter Calibration with optiSLang

- Workflow Template for CFX Simulation

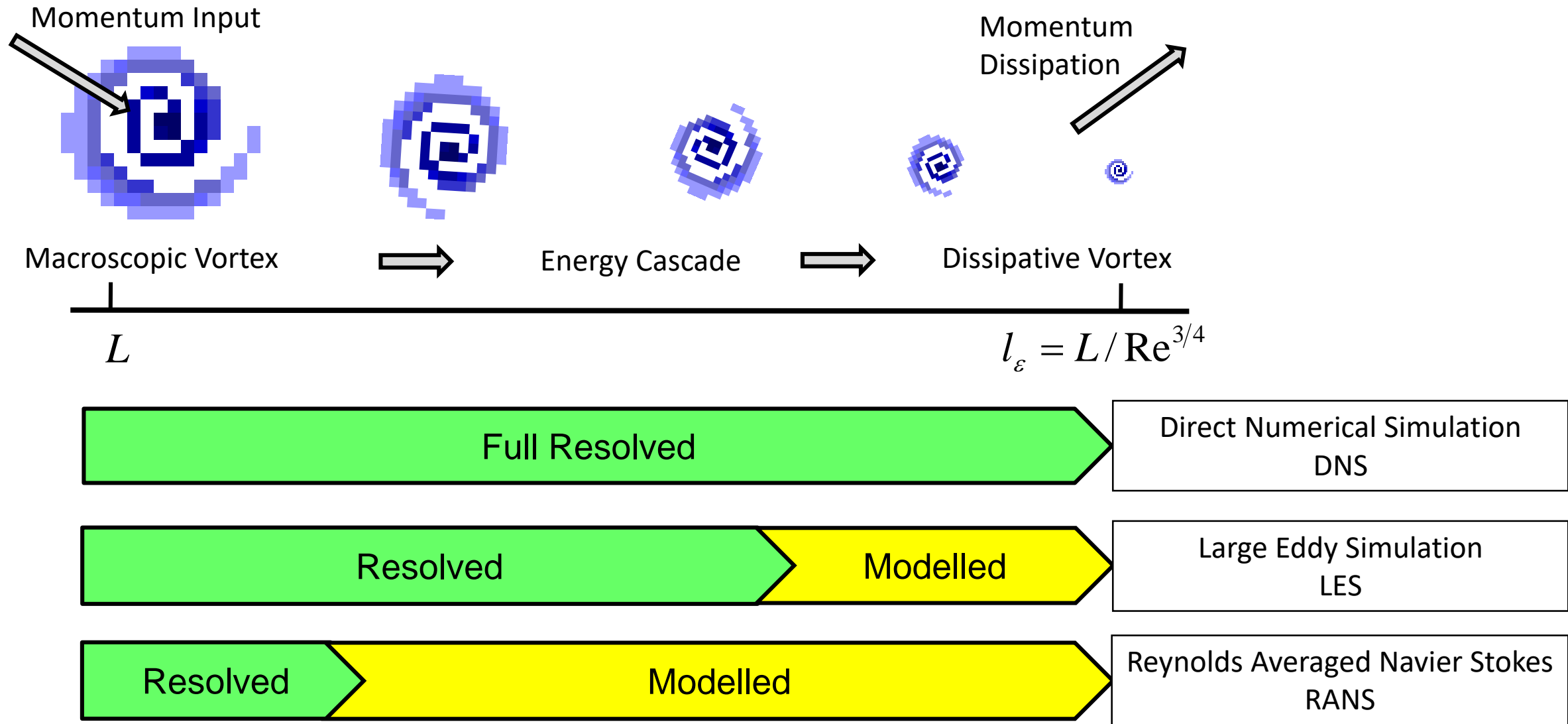
Application Example

- Backward Facing Step
- ...

Summary



Turbulence Modelling at a Glance



Turbulence

Properties:

- three dimensional
- transient
- multi scale

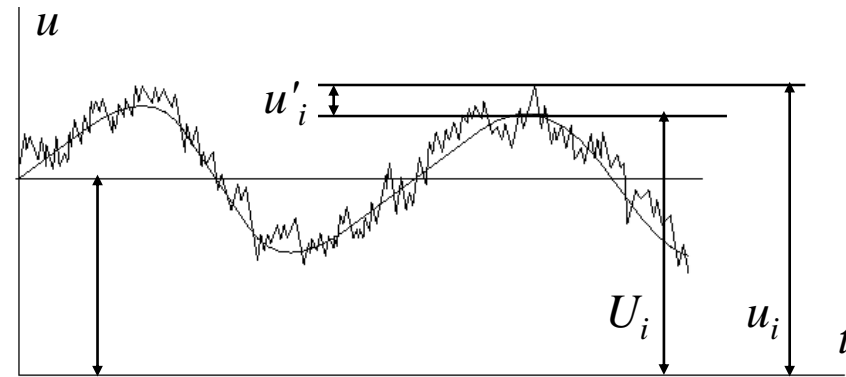
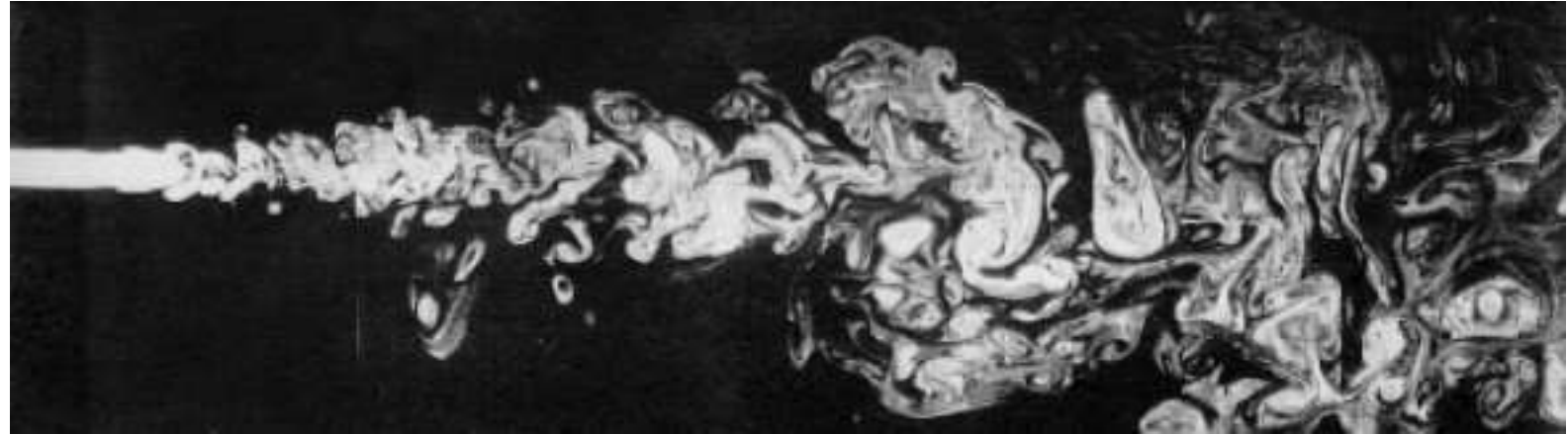
Macroscopic Effect:

- increased Friction
- increased Heat Transfer
- increased Mixing
- ...

Objective:

Model Macroscopic Effects
by RANS

fast! robust! accurate?



$$u_i(\vec{x}, t) = \underbrace{U_i(\vec{x}, t)}_{\text{Average}} + \underbrace{u_i'(\vec{x}, t)}_{\text{Fluctuation}}$$

Turbulence - Eddy Viscosity Models

Reynolds Averaged Navier-Stokes (RANS) Equations:

$$\frac{\partial(\bar{U}_i)}{\partial t} + \frac{\partial(\bar{U}_j \bar{U}_i)}{\partial x_j} = -\frac{1}{\rho} \frac{\partial \bar{P}}{\partial x_i} + \frac{\partial}{\partial x_j} [\tau_{ij}^{mol} + \tau_{ij}^{turb}]$$

Stokes Stress Tensor:

$$\tau_{ij}^{mol} = \nu \left(\frac{\partial \bar{U}_i}{\partial x_j} + \frac{\partial \bar{U}_j}{\partial x_i} \right)$$

Reynolds Stress Tensor:

$$\tau_{ij}^{turb} \approx \nu_t \left(\frac{\partial \bar{U}_i}{\partial x_j} + \frac{\partial \bar{U}_j}{\partial x_i} \right)$$

Eddy Viscosity:

Model Equations are required for k and ω

a huge number of Models has been developed... ***which one is the best?***

$$\nu_t = const \cdot \frac{k}{\omega}$$

Turbulence - Wall Treatment

The Formulation of a Turbulence Model

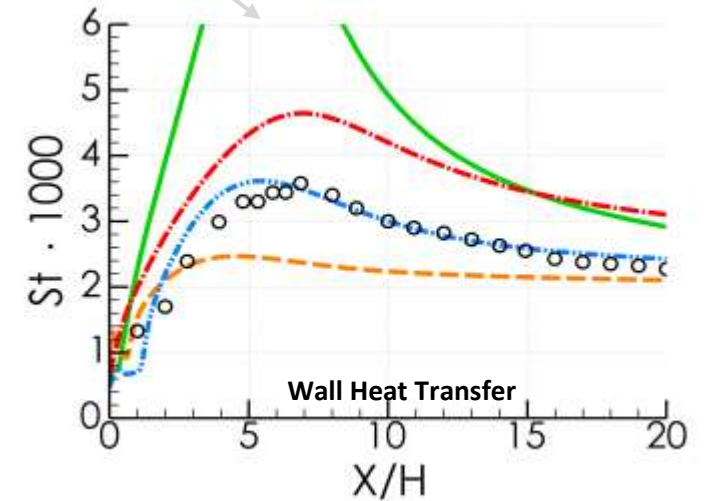
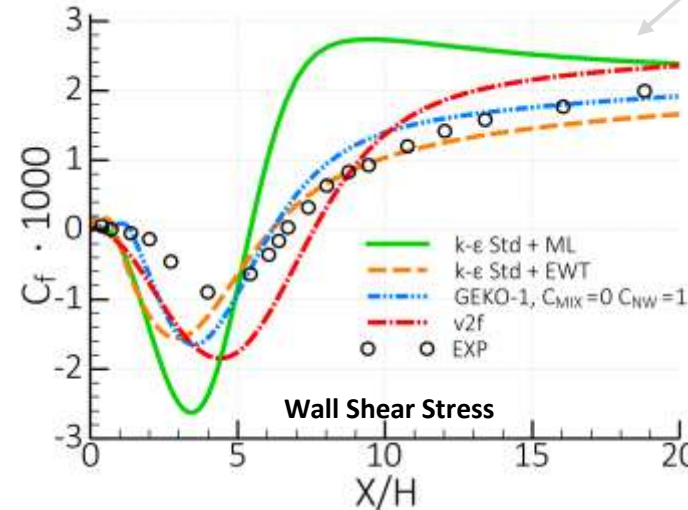
when integrated through the viscous sublayer is a key aspect of turbulence modelling

defines robustness

defines accuracy

can cause undesired pseudo-transition

makes or breaks a Turbulence Model



- 4x the same $k-\varepsilon$ model with different near wall treatment
 - ML – Menter-Lechner low-Re model
 - EWT – Enhanced wall treatment built on 2-Layer formulation
 - GEKO-1 exact transformation of $k-\varepsilon$ to $k-\omega$ with $k-\omega$ wall treatment
 - V2F - $k-\varepsilon$ model with V2F 'elliptic blending' wall treatment
- Results are vastly different

Motivation GEKO Model

Two-Equation Models are the Work-Horse in industrial CFD

They have typically 5 Coefficients which can be calibrated to match Physics

They are calibrated for

- Flat Plate Boundary Layers (log-Layer)
- Selected free Shear Flows (plane Mixing Layer, Plane Jet)
- Decaying Turbulence in Freestream



Central Question: Can we do such a simulation with one set of global constants?

Probably not ...

GEKO Model: Introducing Free Coefficients

Model Equations for Turbulent Kinetic Energy k and Dissipation ω :

$$\frac{\partial(\rho k)}{\partial t} + \frac{\partial(\rho U_j k)}{\partial x_j} = P_k - \rho C_\mu k \omega + \frac{\partial}{\partial x_j} \left[\left(\mu + \frac{\mu_t}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right] \quad \nu_t = \frac{k}{\max(\omega, S/C_{Real})}$$

$$\frac{\partial(\rho \omega)}{\partial t} + \frac{\partial(\rho U_j \omega)}{\partial x_j} = C_{\omega 1} F_1 \frac{\omega}{k} P_k - C_{\omega 2} F_2 \rho \omega^2 + F_3 \frac{2}{\sigma_\omega} \frac{\rho}{\omega} \frac{\partial k}{\partial x_j} \frac{\partial \omega}{\partial x_j} + \frac{\partial}{\partial x_j} \left[\left(\mu + \frac{\mu_t}{\sigma_\omega} \right) \frac{\partial \omega}{\partial x_j} \right]$$

The functions F_1 , F_2 , and F_3 are not constant for GEKO Model, they contain free Coefficients:

C_{SEP} – changes separation behavior

C_{MIX} – changes spreading rates of free shear flows

C_{NW} – changes near-wall behavior

C_{JET} – optimizes free jet flows

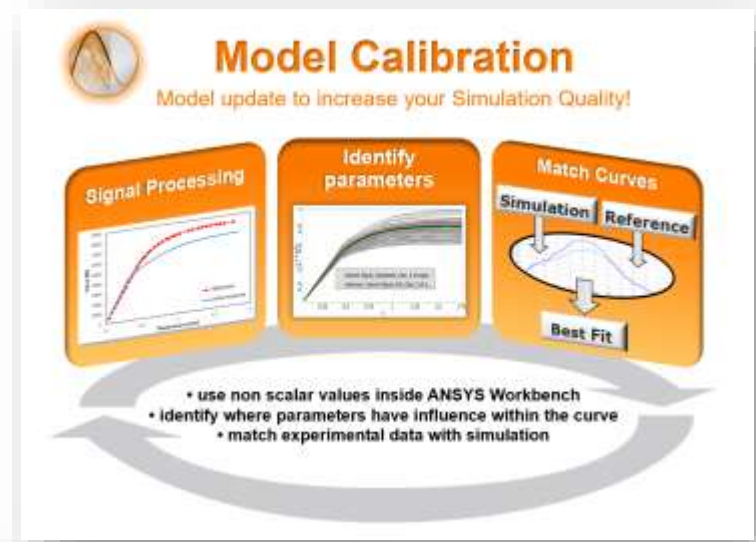
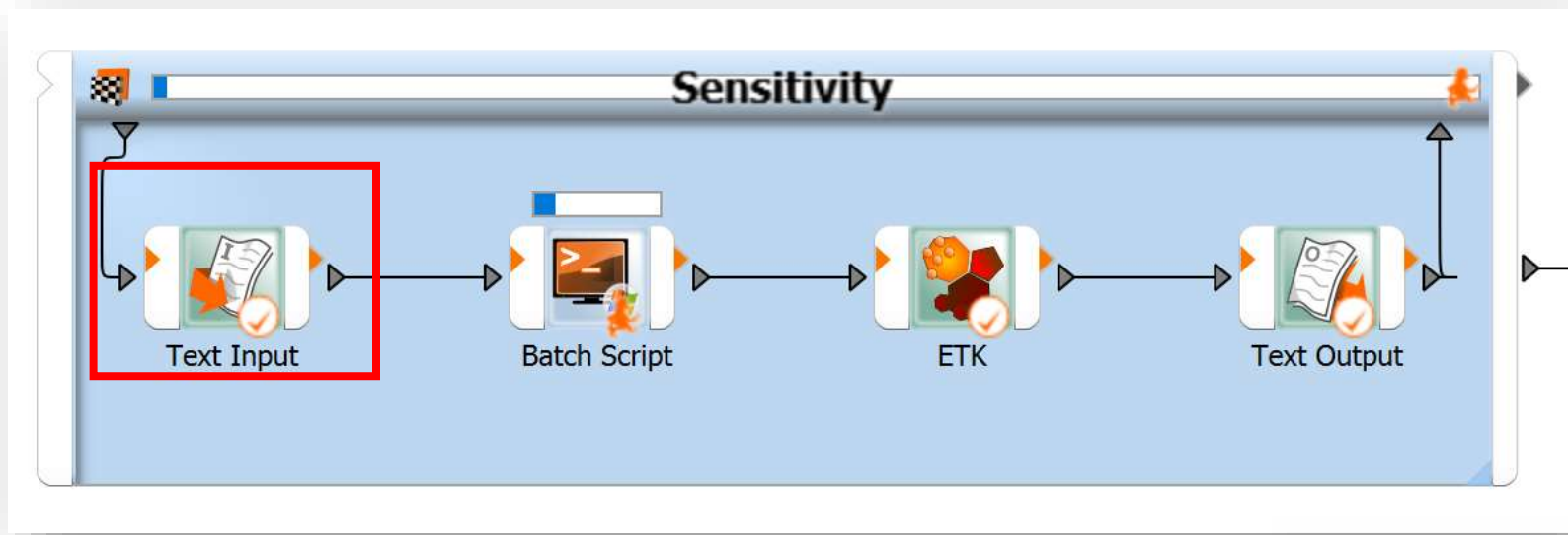
C_{CORNER} – affects corner flows



GEKO Coefficients can be varied without losing the fundamental Correlations!

→ Model Calibration wrt to Experiment possible

Workflow optiSLang CFX – Template – Input



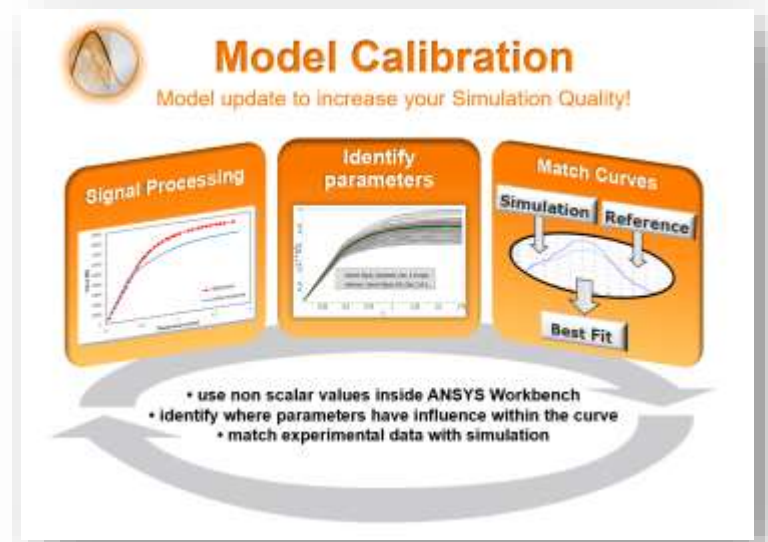
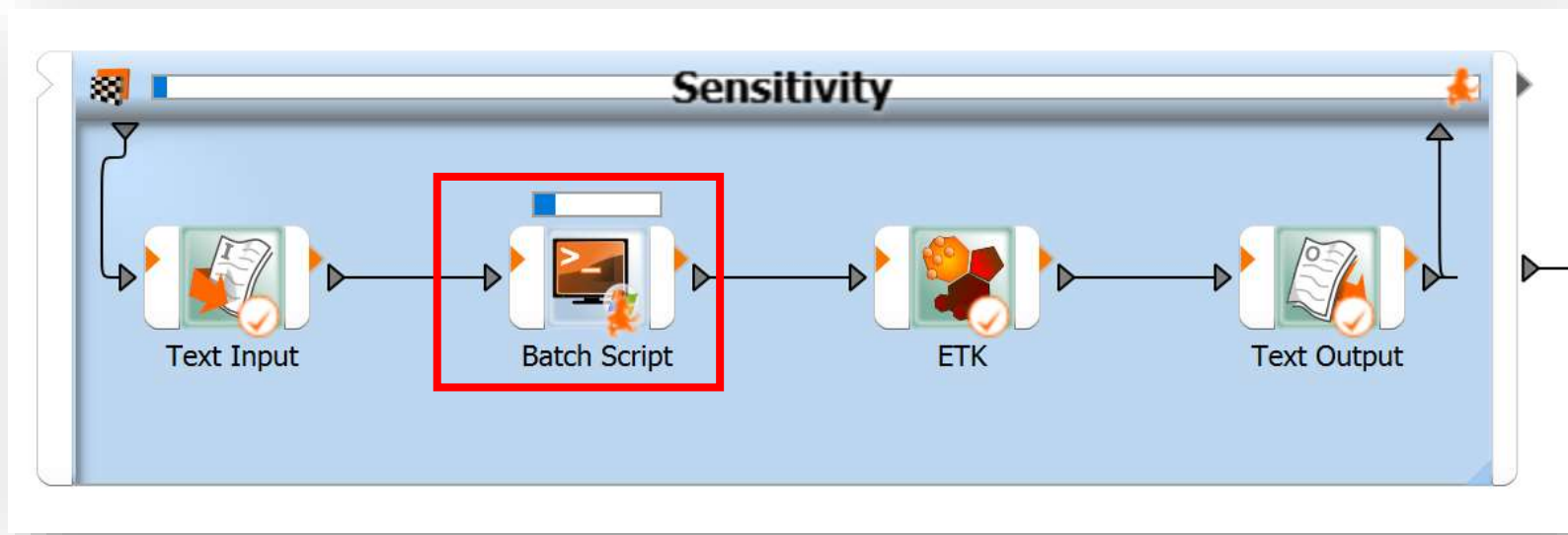
**CFX-CCL File,
parsed for GEKO
Parameter**

```

1 FLOW: Flow Analysis
2 DOMAIN: fluid
3 FLUID MODELS:
4 TURBULENCE MODEL:
5 Option = GEKO
6 Separation Coefficient = 1.75
7 Mixing Coefficient = 0.3
8 #
9 Near Wall Coefficient = 0.5
10 Jet Coefficient = 0.9
11 Corner Coefficient = 0.0
12 END
13 END
14 END
15 END
    
```

**CFX-CCL-Snippet
Linked to Solver at Start**

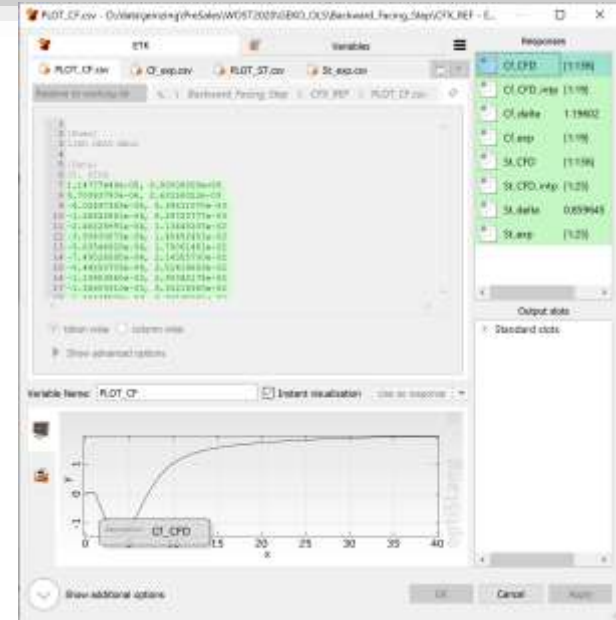
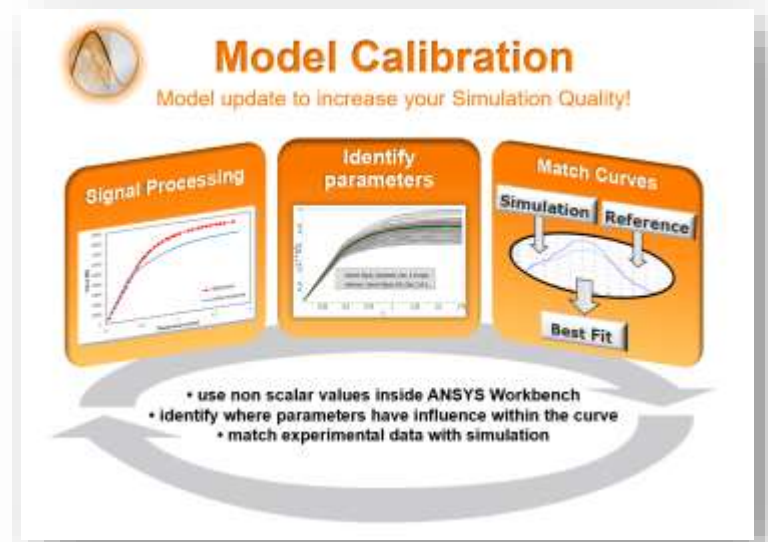
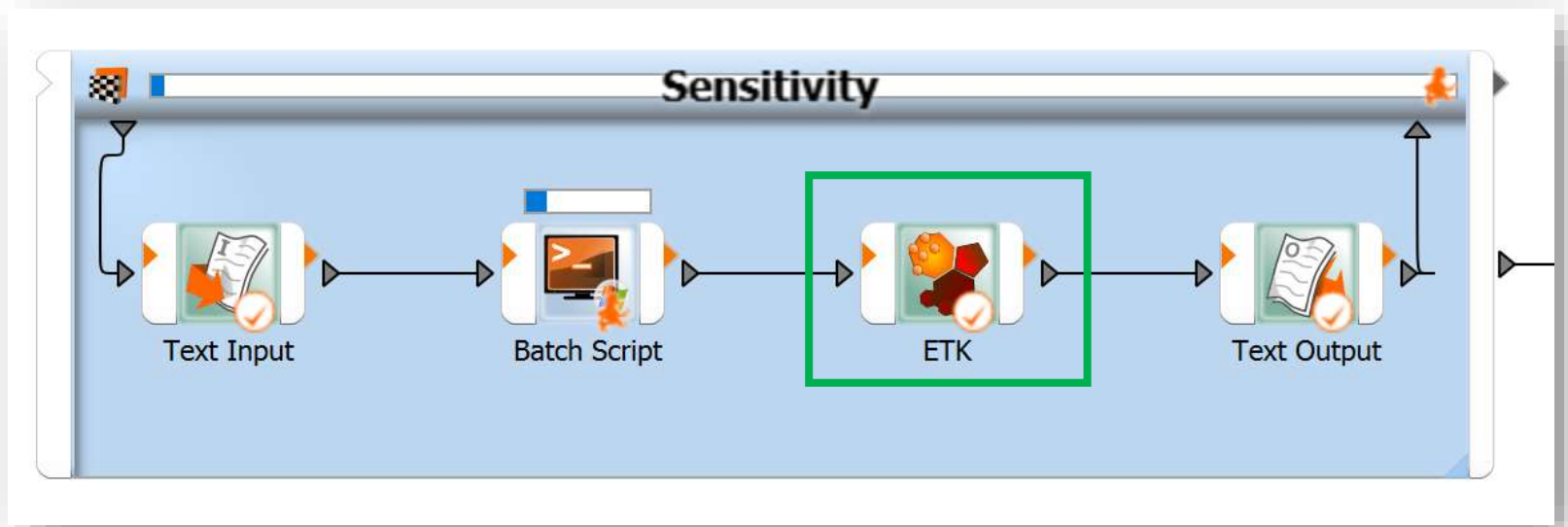
Workflow optiSLang CFX – Template – Solver



```
cfx_batch.bat - Notepad
File Edit Format View Help
copy D:\data\jeinzing\PreSales\WOST2020\GEKO_OLS\Backward_Facing_Step\CFX_REF\BFS.def .
copy D:\data\jeinzing\PreSales\WOST2020\GEKO_OLS\Backward_Facing_Step\CFX_REF\BFS.cst .
copy D:\data\jeinzing\PreSales\WOST2020\GEKO_OLS\Backward_Facing_Step\CFX_REF\cfxpost_varvector.cse .
"C:\Program Files\ANSYS Inc\v201\CFX\bin\cfx5solve.exe" -def BFS.def -ccl GEKO.ccl
"C:\Program Files\ANSYS Inc\v201\CFX\bin\cfx5post.exe" -batch cfxpost_varvector.cse
del BFS_001.res
```

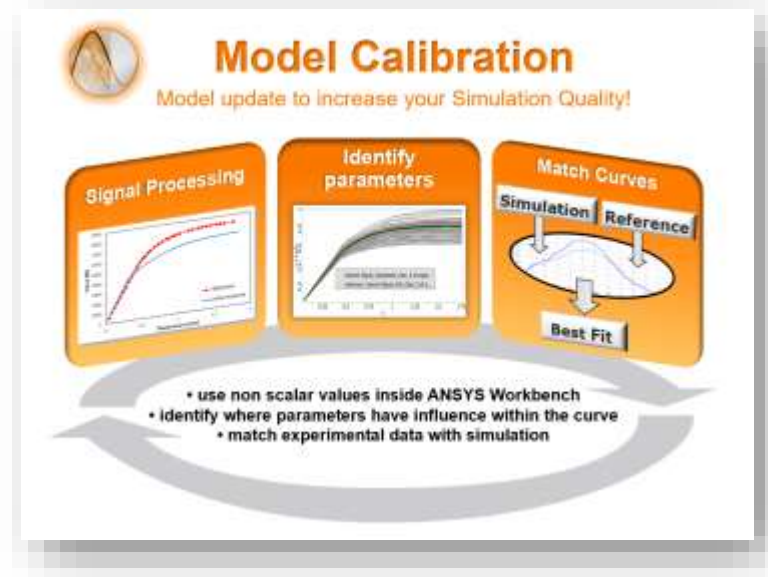
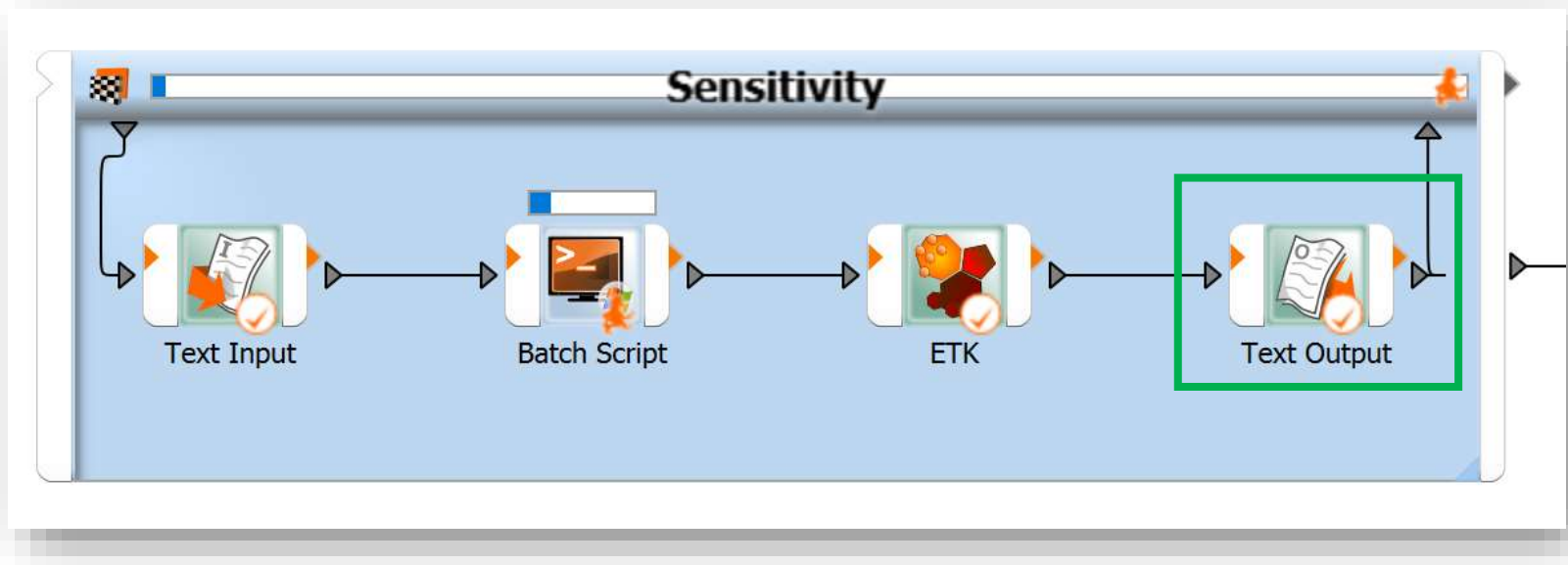
**Copy Reference Files,
CFX-Solver&Post Script
Start CFX-Solver
Start CFX-Post
Delete Result File**

Workflow optiSLang CFX – Template – Signals



Read Signals:
Velocity Distributions
Friction Coefficient
Stanton Number
CFD Simulation and
Experiment
Calculate Difference of
Curves

Workflow optiSLang CFX – Template – Output



The screenshot shows the 'Text Output' window with a file named 'BFS.txt' open. The text content is as follows:

```
1 Postprocessing of BFS
2
3 Accumulated Time Step = ..... 1.08000000e+02 [.]
4 my_max_res = ..... 1.73530054e-07 [.]
5
```

On the right side of the window, under the 'Responses' tab, two parameters are listed: 'MaxResidual' with a value of 1.7353 and 'Numiteration' with a value of 108.

**Parse Scaler Output
Parameter
Maximum Residual and
Iteration Number, to
check convergence for all
Design Points**

Test Case: Backward Facing Step

2D Test Case with Recirculation

Inlet:

- Velocity Profile
- $k-\omega$ Profile
- constant Temperature

Outlet:

- constant Pressure

Fluid:

- incompressible

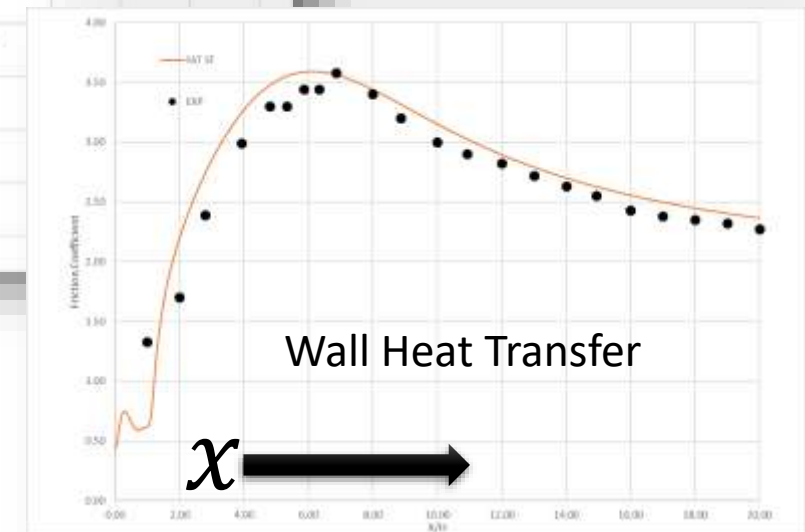
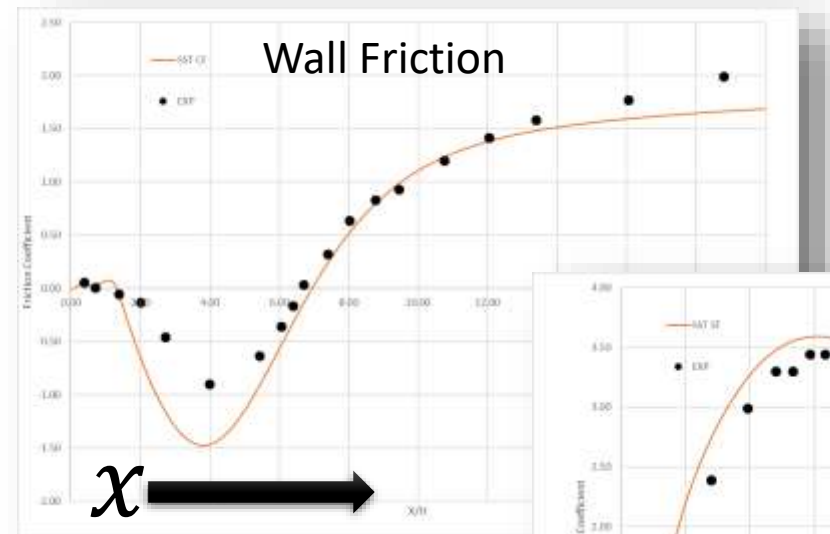
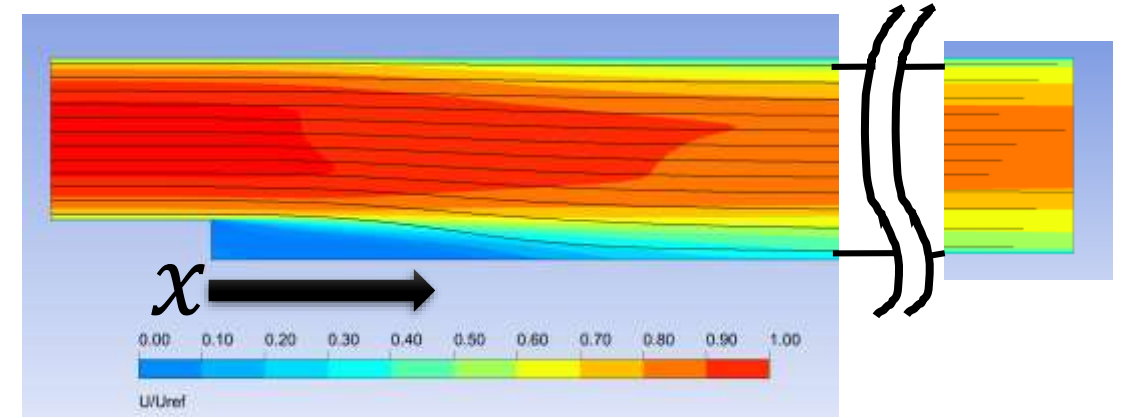
Reynolds Number = 10^5

Reference Turbulence Modell

- SST

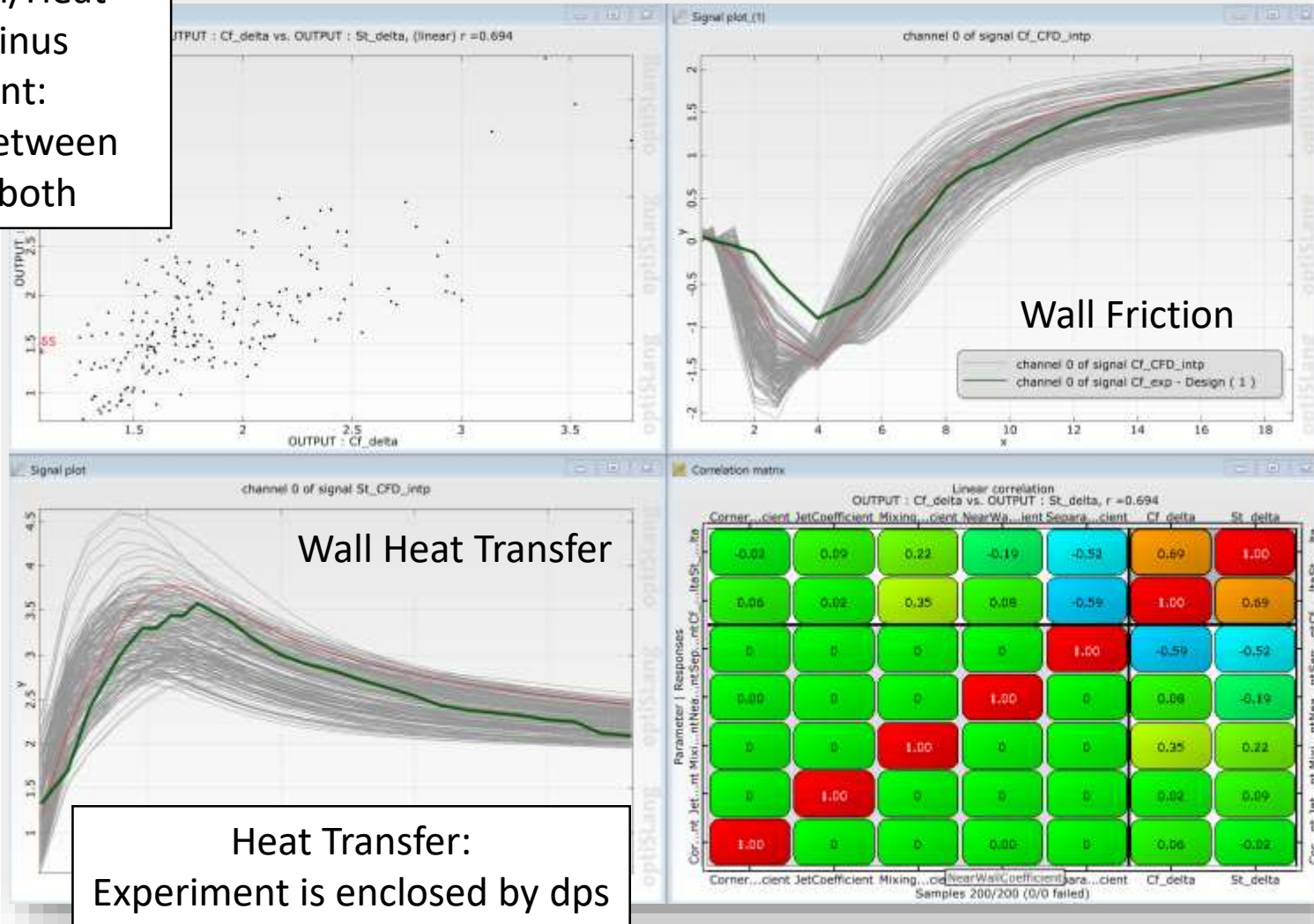
Output:

- Wall Friction Coefficient
- Wall Heat Transfer Coefficient



Sensitivity Study – 200 Samples

Delta Friction/Heat Transfer minus Experiment:
No Conflict between best fit for both



Wall Friction:
Experiment is not fully enclosed by dps

Heat Transfer:
Experiment is enclosed by dps

GEKO Parameter	min	max
Separation Coefficient	0.9	2.3
Mixing Coefficient	0.15	0.95
Near Wall Coefficient	-1.25	1.25
Jet Coefficient	0.0	1.0
Corner Coefficient	0.0	1.5

Meta Model of Optimal Prognosis

Good CoP for both Delta Sim vs Exp

Input Parameter:

C-Separation: dominating Parameter

C-Mixing: important

C-Near-Wall: important

C-Jet: filtered out

C-Corner: filtered out

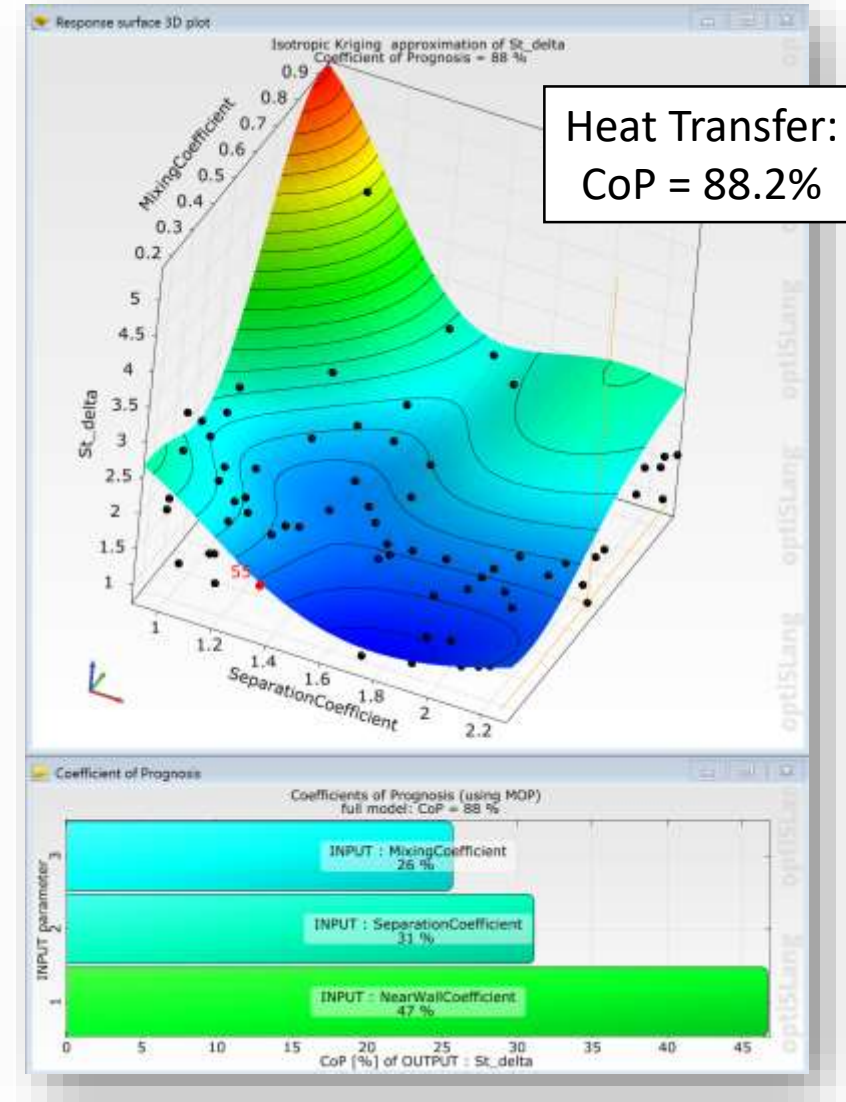
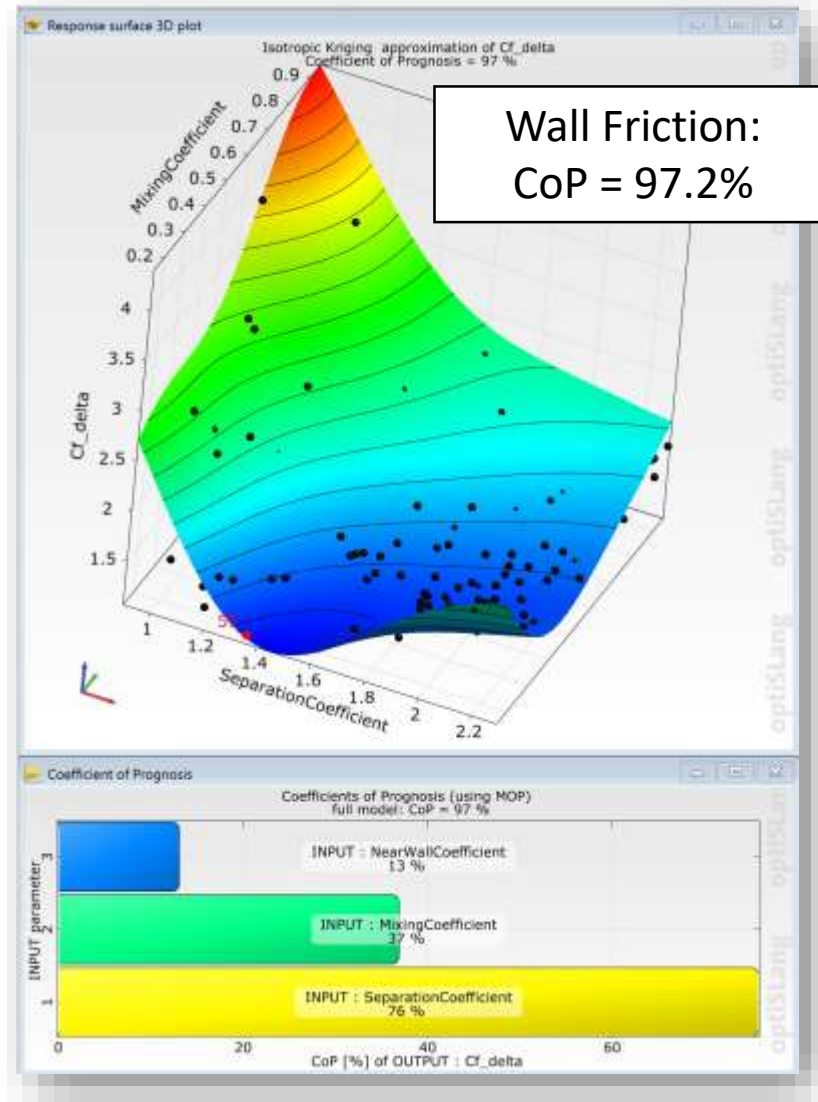
Next Step:

Optimization on Meta-Model

CFX Calculation for Optimum

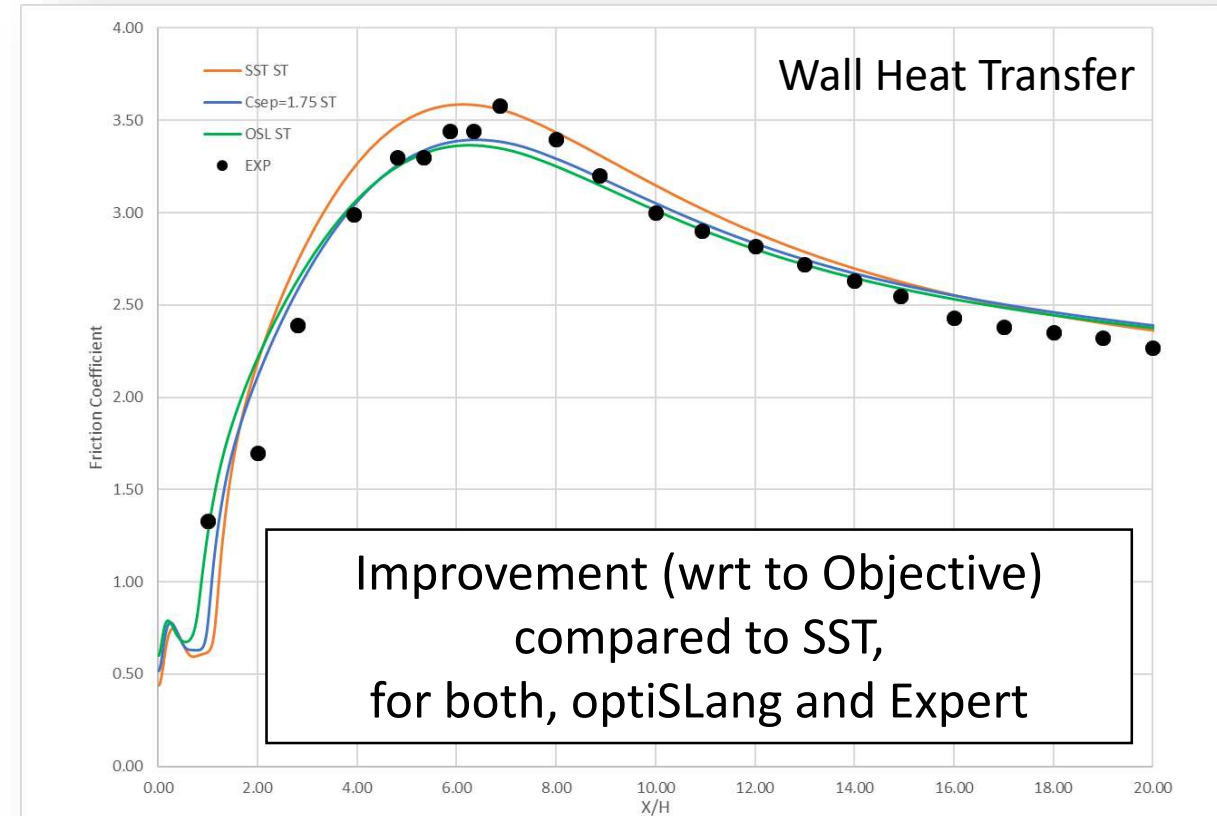
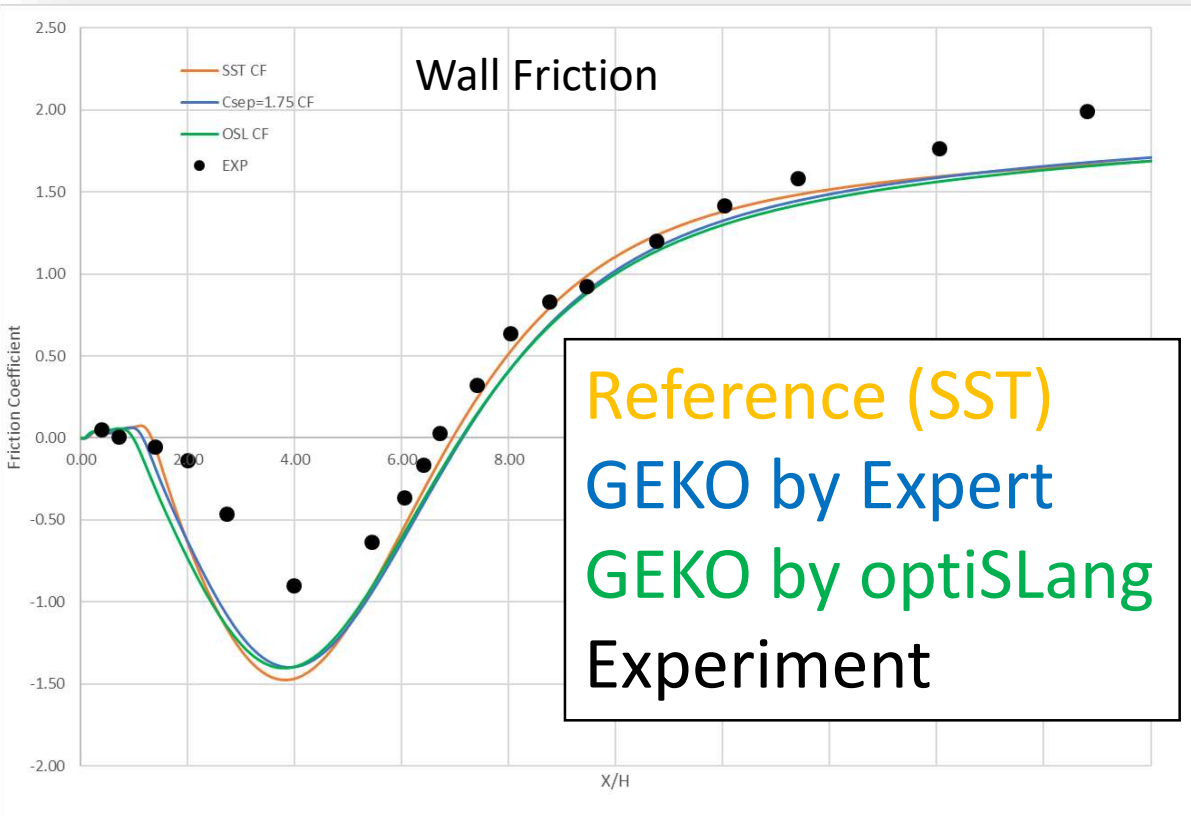
Objective Function:

$$\min(\Delta C_f + \Delta S_t)$$

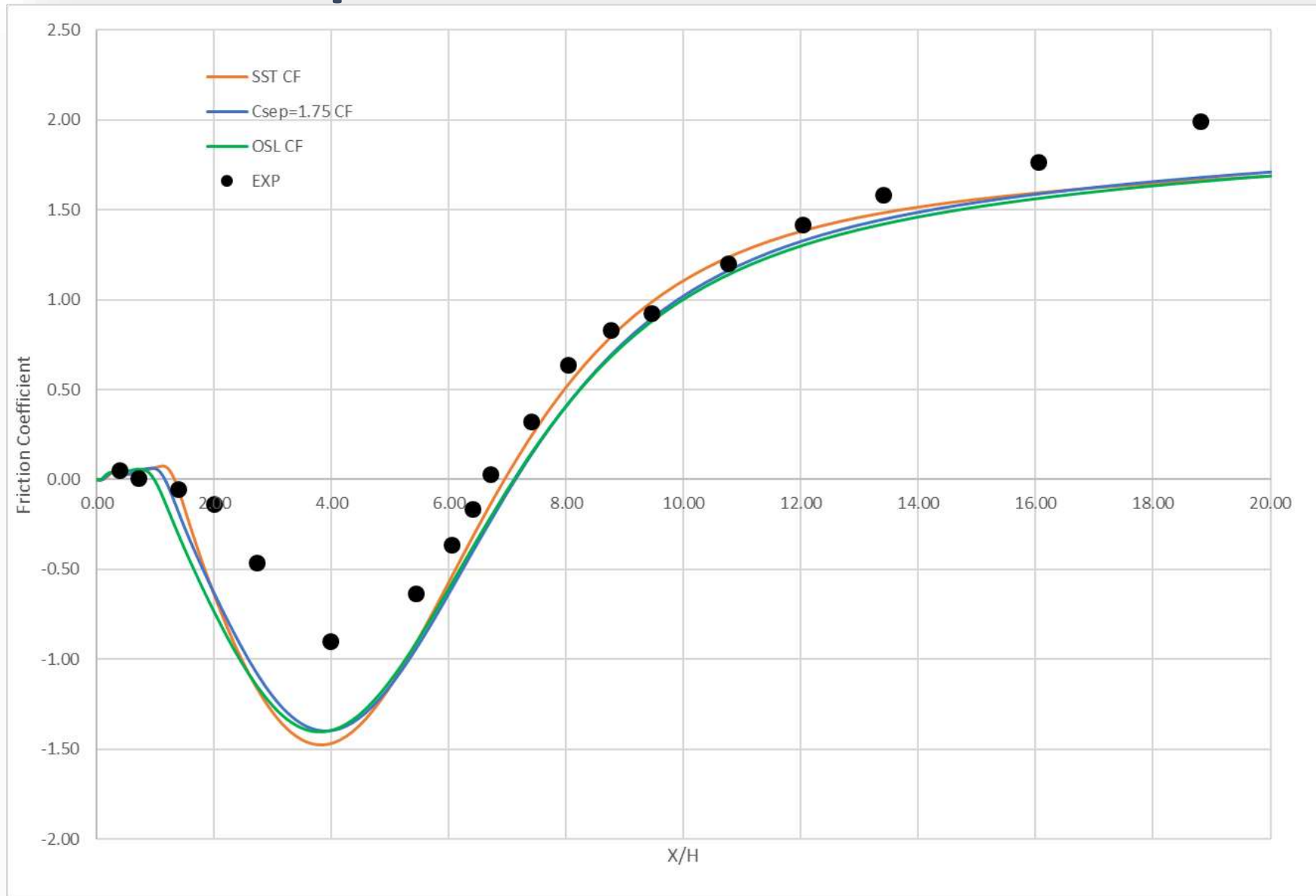


Optimization on Meta Model

	CoP [%]	Reference	Expert	MoP Prediction	CFX Simulation	Rel. Error [%]
Cf-Delta	97.2	1.228	1.221	1.303	1.293	0.54
St-Delta	88.2	0.969	0.713	0.782	0.754	3.71
OBJ: (Cf+St) = min	-	2.197	1.934	2.082	2.047	1.71

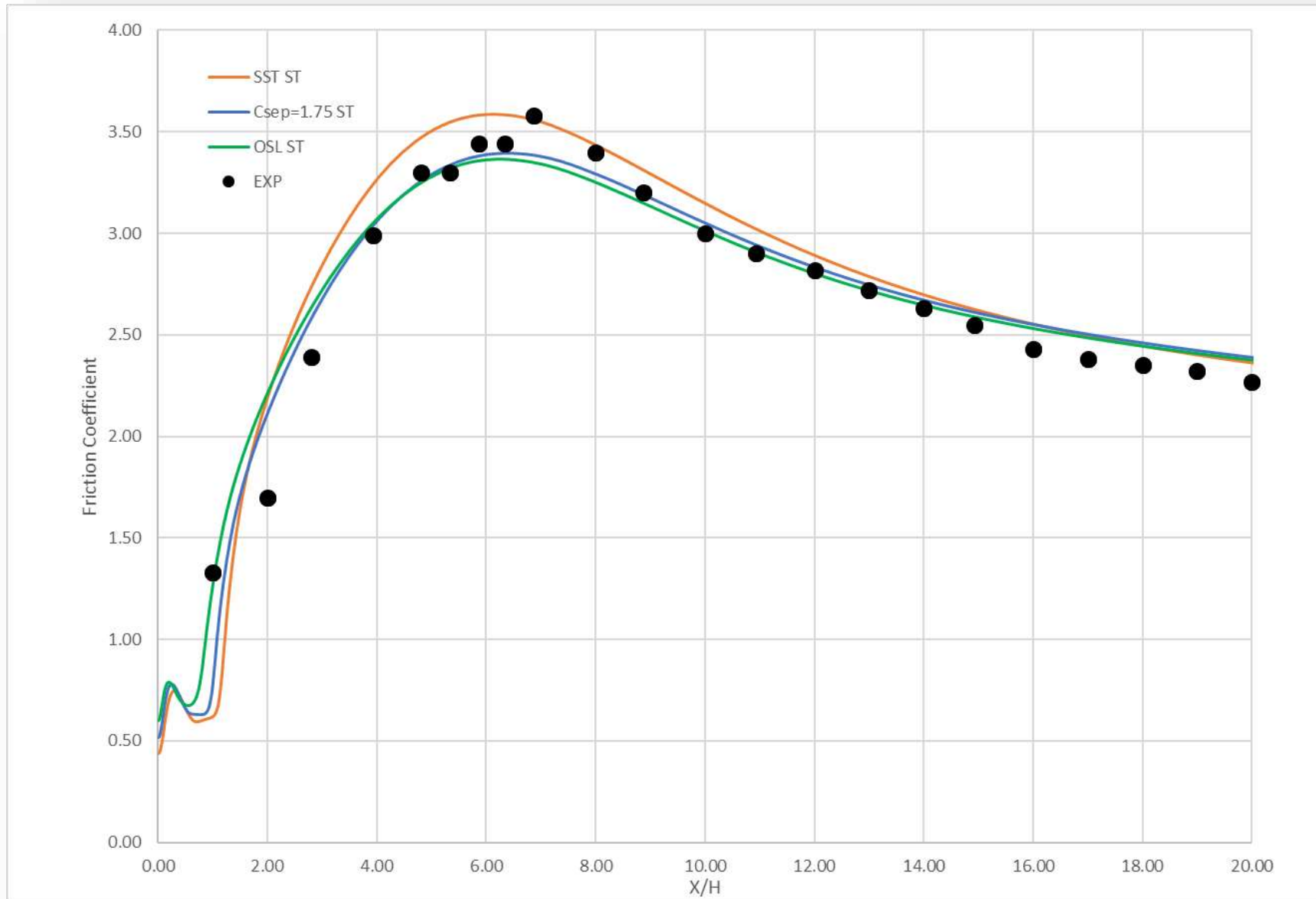


Result Comparison – Wall Friction



Reference
GEKO by Expert
GEKO by optiSLang
Experiment

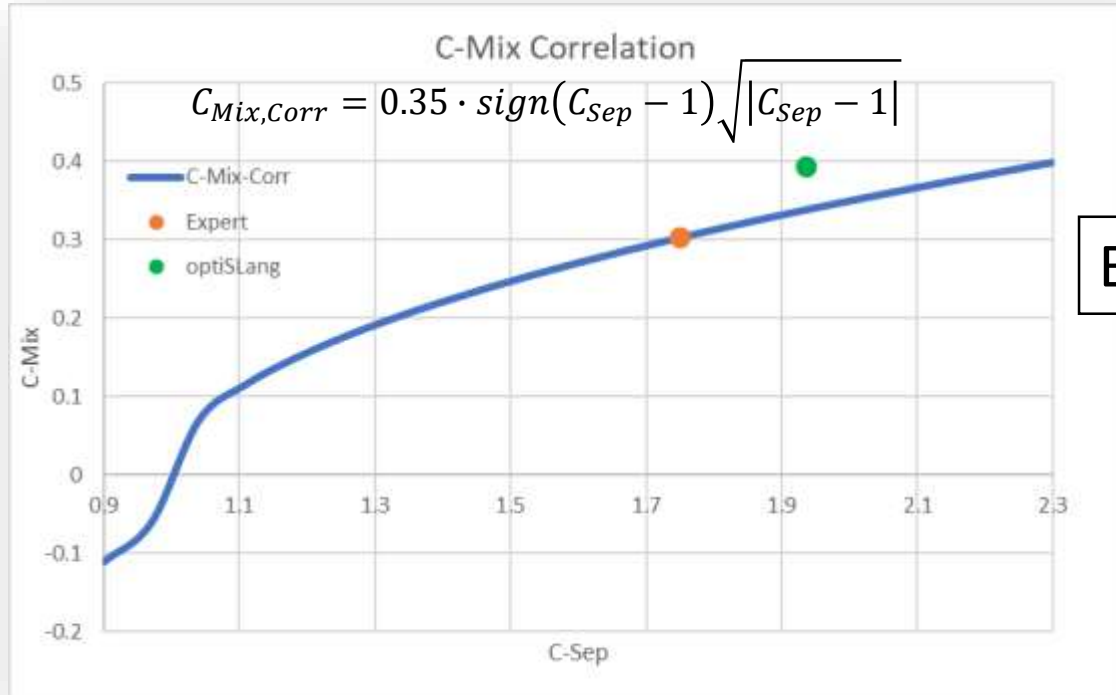
Result Comparison – Wall Heat Transfer



Reference
GEKO by Expert
GEKO by optiSLang
Experiment

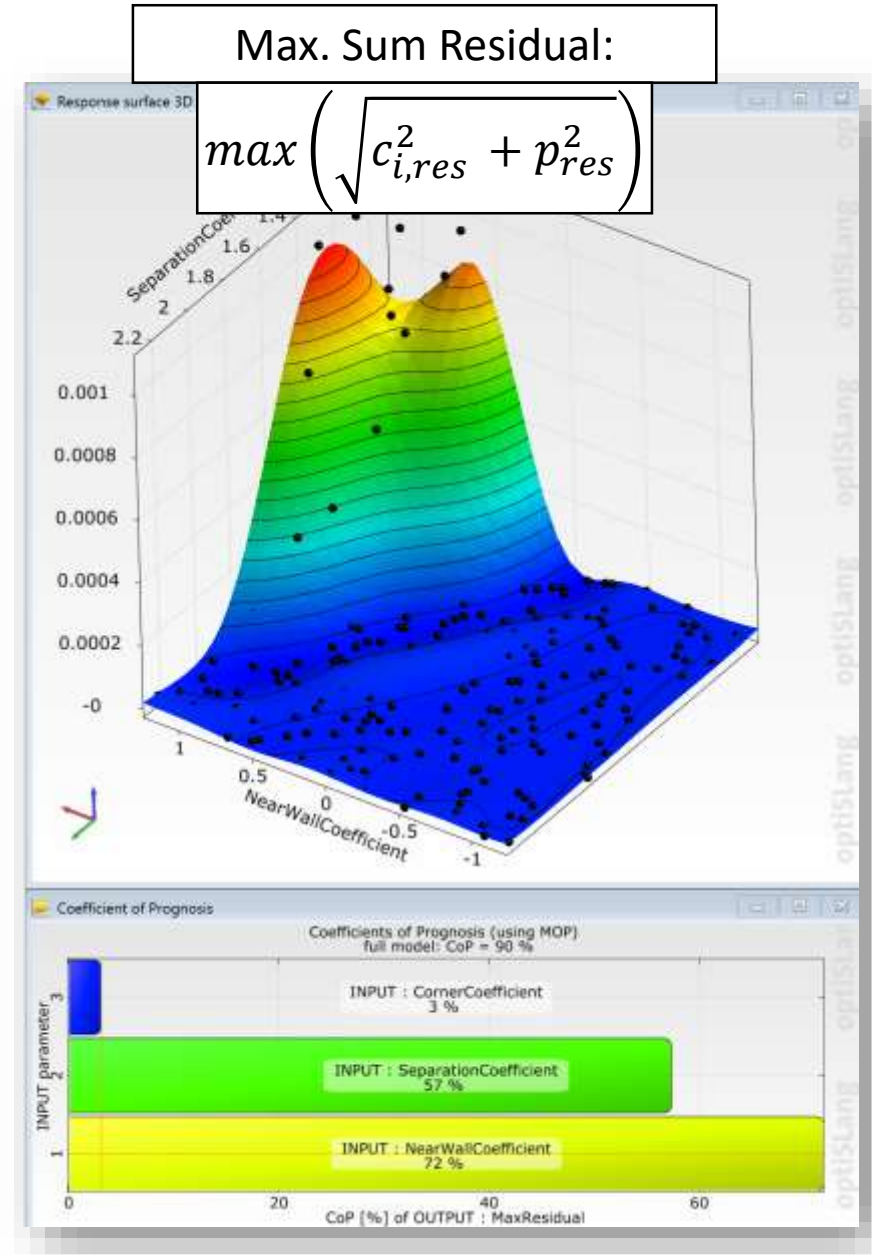
Result Comparison – GEKO Parameter

GEKO Parameter	Expert	optiSLang	min	max
Separation Coefficient	1.75	1.937	0.9	2.3
Mixing Coefficient	0.3	0.3925	0.15	0.95
Near Wall Coefficient	0.5	0.3603	-1.25	1.25
Jet Coefficient	0.9	0.9	0.0	1.0
Corner Coefficient	1.0	0.0	0.0	1.5



Bad Residuals for

$$C_{sep} < 2C_{NW}$$



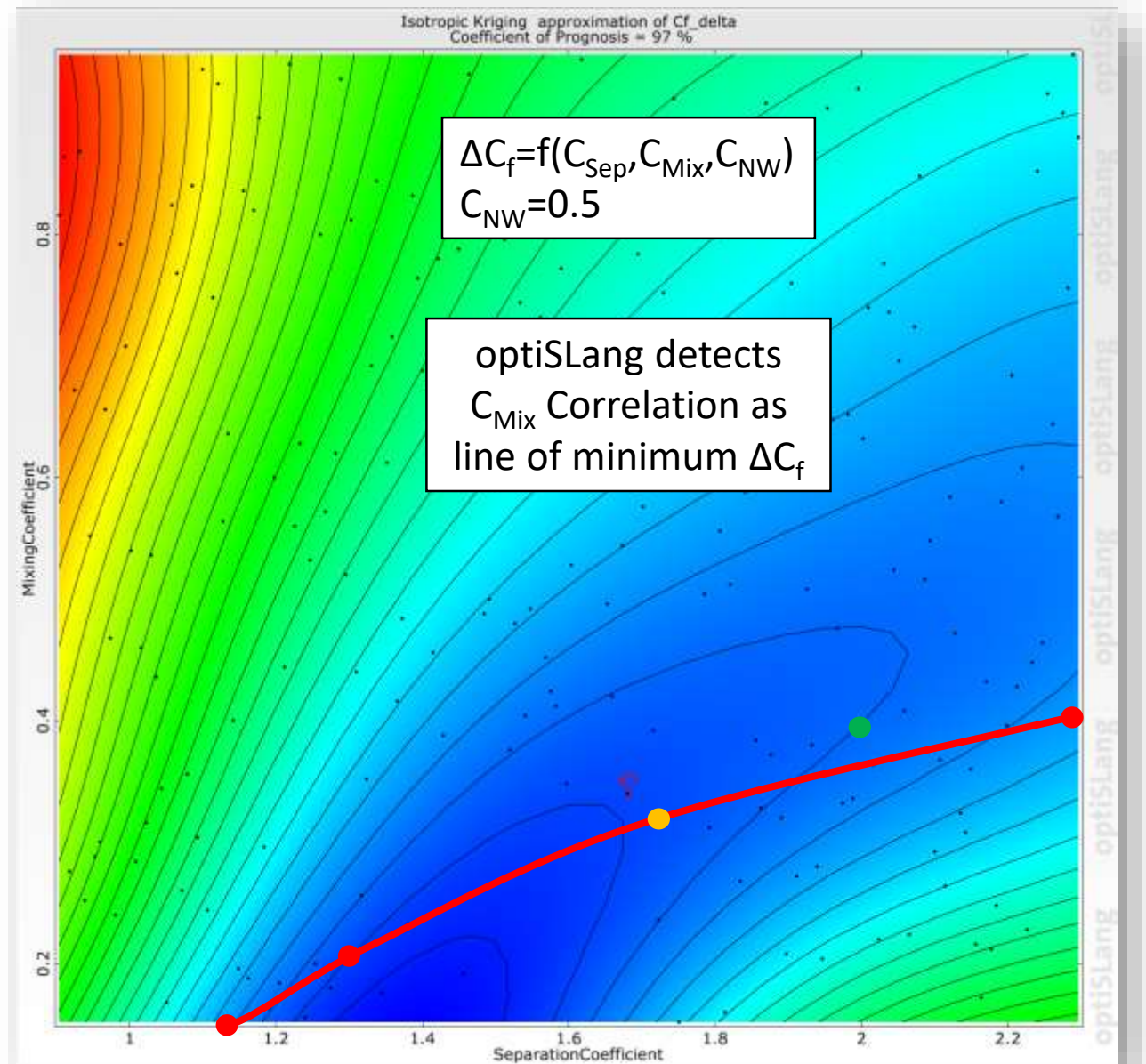
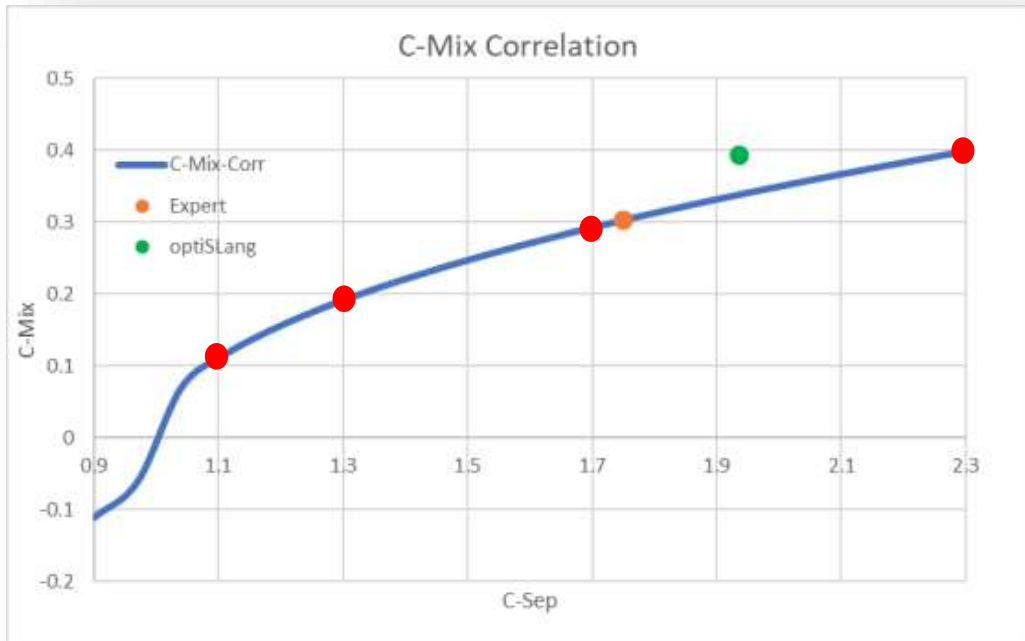
Result Comparison – C_{Mix} Correlation

GEKO_Model_Best_Practice_V1.0.pdf:

For each value of C_{SEP} an optimal value of C_{MIX} exists, which maintains optimal free shear flows.

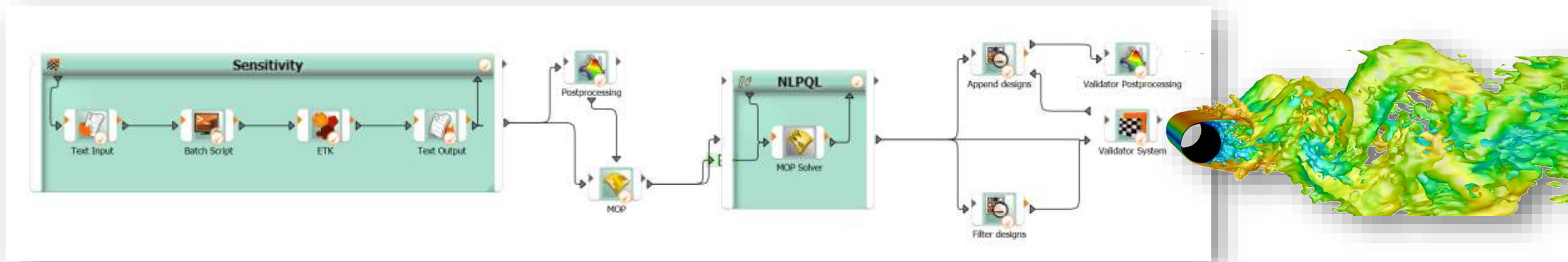
This value is given by the correlation:

$$C_{Mix,Corr} = 0.35 \cdot \text{sign}(C_{Sep} - 1) \sqrt{|C_{Sep} - 1|}$$



Summary

Generic GEKO Parameter Calibration Template for CFX is generated



Result for Backward Facing Step:

- Calibration by Expert
 - Calibration by optiSLang
- deliver comparable Results, both improved compared to SST, wrt to Objective Function



Benefit from optiSLang, if no Expert is available!

Note: other Objective Functions are possible!