

# Technische Hochschule Ulm



## Calibration of a material model for high-purity (OFHC) copper using classic and modern methods

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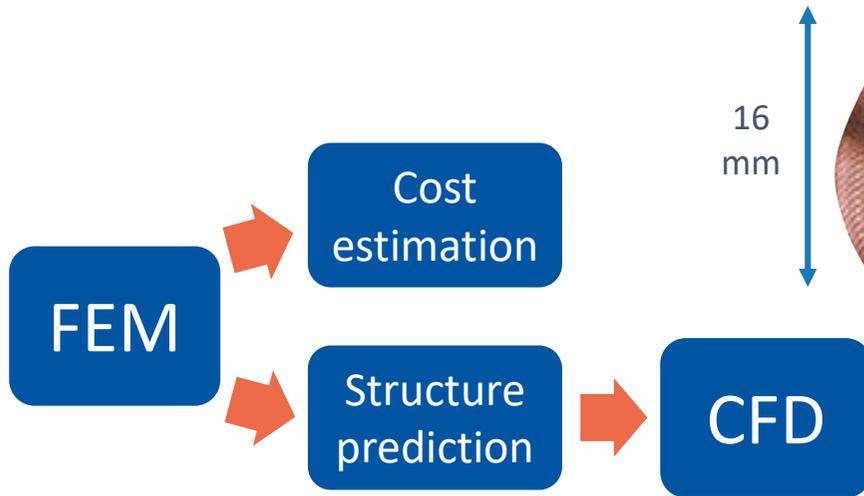
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## Agenda

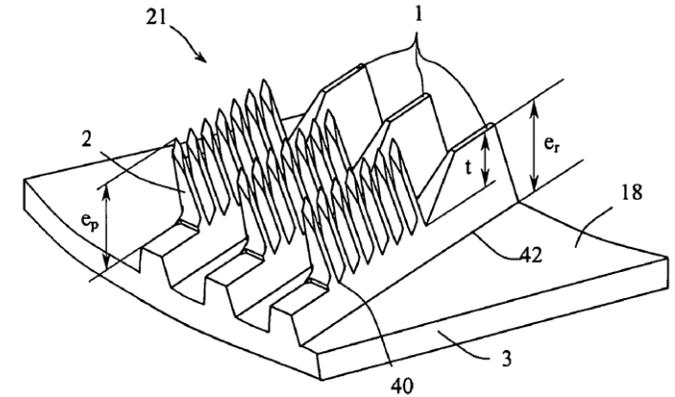
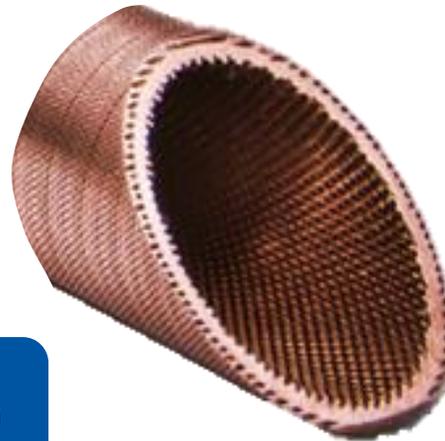
- Motivation
- Environment
- Important basics
- Global response fit
  - Root Mean Square Error (RMSE) approach
  - Dynamic Time Warping (DTW)
  - Statistics on Structures (SoS)
  - Comparison
- Summary



# wieland



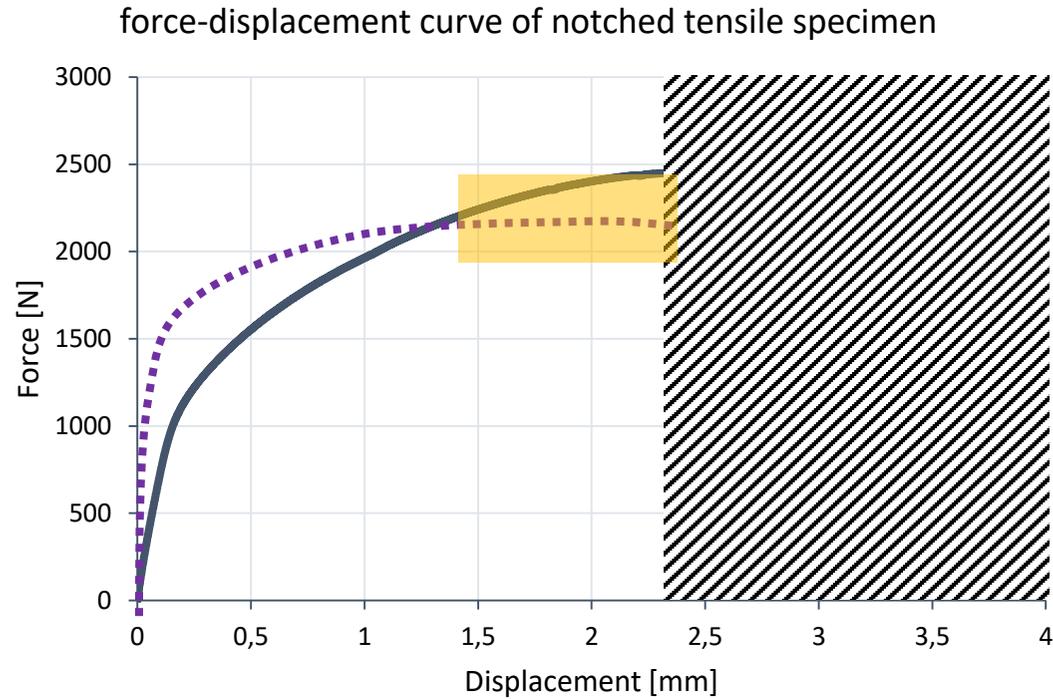
16 mm



United States Patent No. 7,509,828 B2

<https://www.wieland-thermalsolutions.com/de/rippenrohre/hochleistungsrohre>

# Motivation



- Experiment
- Johnson-Cook

Simulations based on material models from literature do not fit the experiments.  
A manufacturer-specific flow curve needs to be created to make predictions with FEM.



LS-DYNA R11, GISSMO specimen geometry



Optislang,  
Statistics on Structures



GOM Correlate  
Professional

## Engineering Curve

$$\sigma_{\text{Eng}} = \frac{\text{force}}{\text{area}_0}$$

$$\varepsilon_{\text{Eng}} = \frac{\text{disp.}}{\text{length}_0}$$

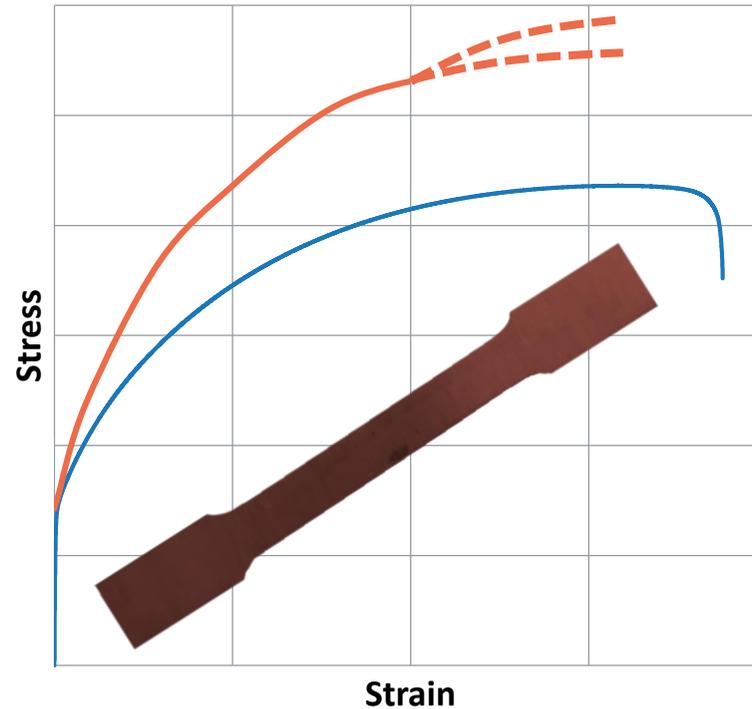
+

Easy

-

Global

## Difference between engineering and „true“ plastic curve



## True plastic Curve

$$\sigma_{\text{True}} = \sigma_{\text{Eng}} \cdot (1 + \varepsilon_{\text{Eng}})$$

$$\varepsilon_{\text{True}} = \ln(1 + \varepsilon_{\text{Eng}})$$

$$\varepsilon_{\text{True,pl}} = \varepsilon_{\text{True}} - \frac{\sigma_{\text{Eng}}}{E}$$

+

Universal

-

Extension  
necessary

# Important Basics

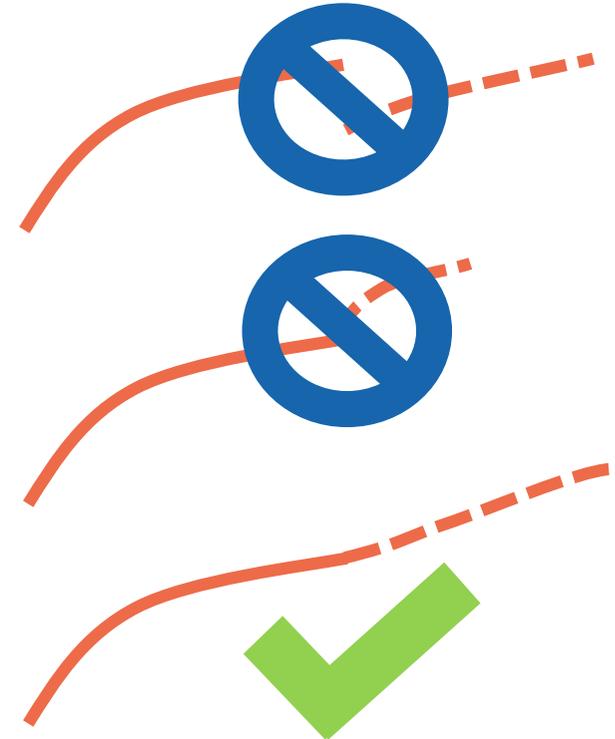
- Swift
- Voce
- Hockett-Sherby
- Johnson-Cook
- And many more!

$$\sigma_{True} = \cancel{K}(\epsilon_0 + \epsilon_{pl})^{\cancel{n}}$$

$$\sigma_{True} = \cancel{A} - \cancel{B} \cdot e^{-C \cdot \epsilon_{pl}}$$

$$\sigma_{True} = \cancel{A} - \cancel{B} \cdot e^{-C \cdot \epsilon_{pl}^n}$$

$$\sigma_{True} = \cancel{A} + \cancel{B} \cdot \epsilon_{pl}^n$$



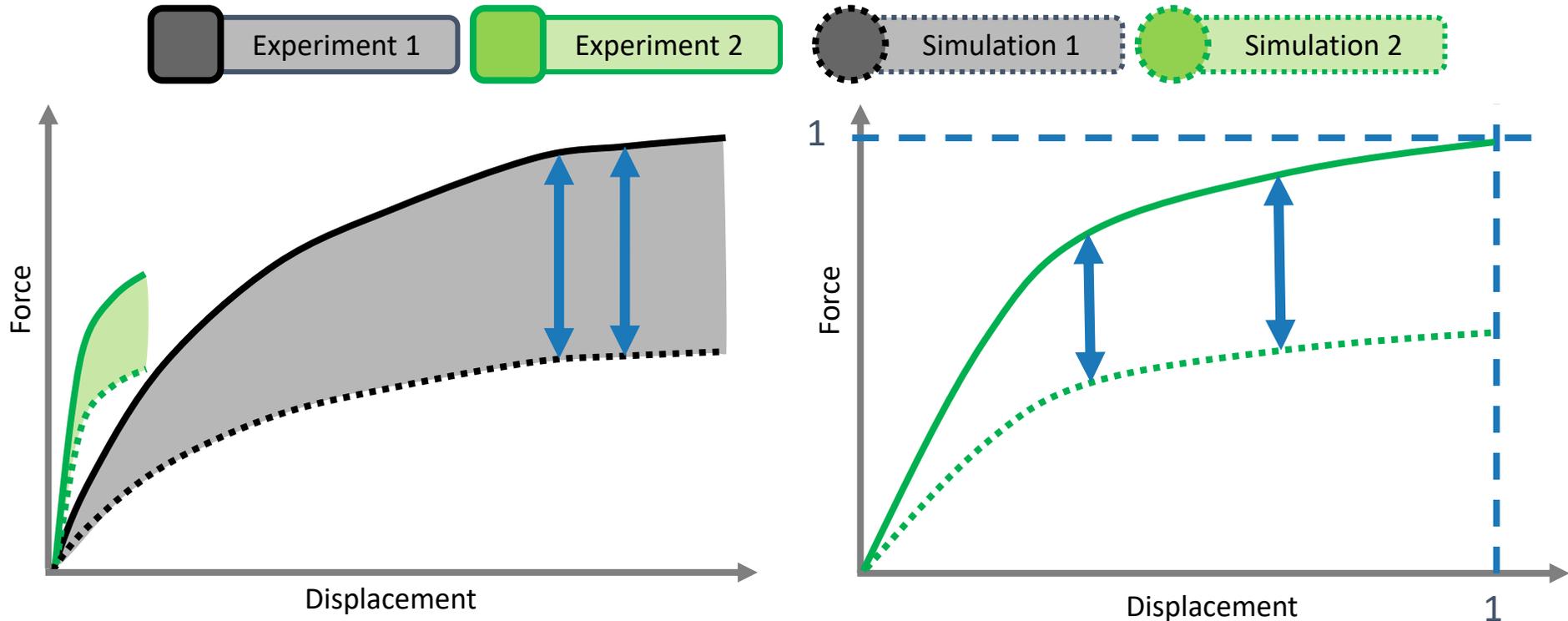
We eliminate two variables so c1 continuity is preserved.  
I prefer Hockett-Sherby because the two remaining variables offer great flexibility.



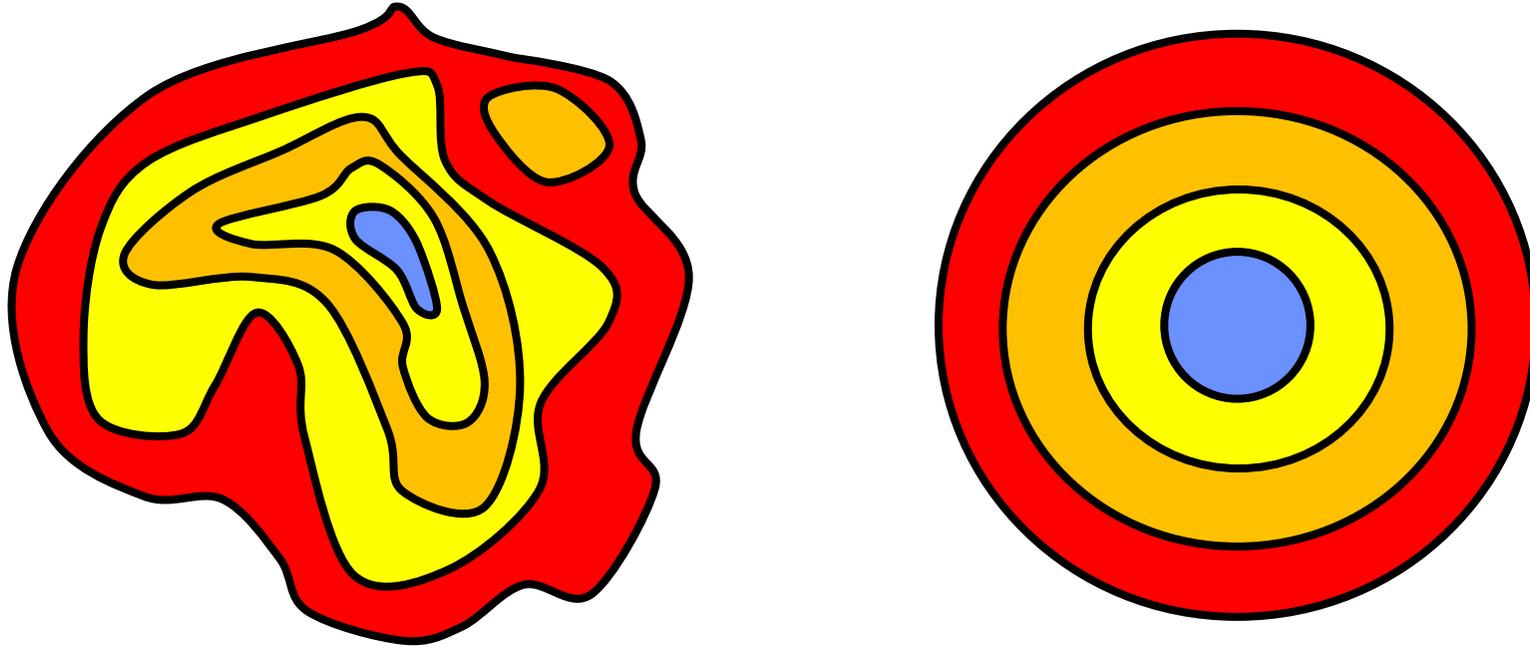
$$\text{Total Error} = \text{Error1} + \text{Error2} + \text{Error3} + \text{Error4}$$

Let us just define the total error as the sum of errors for each individual specimen.  
This is a simple approach but is a good description if no biasing occurs.

# Important Basics

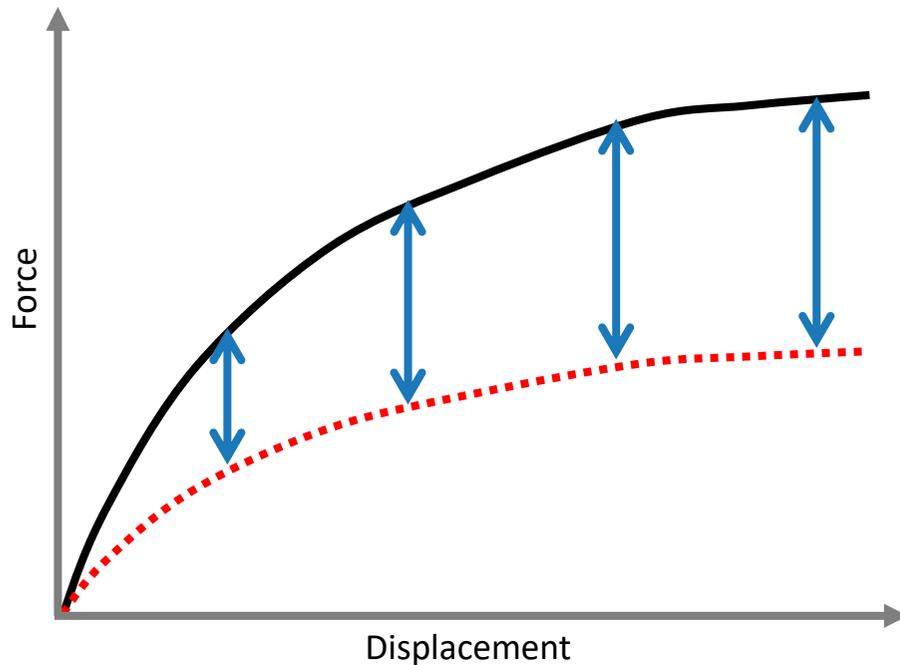


When undertaking a multi-objective optimization the data needs to be adjusted.  
We eliminate inherent data bias by scaling and resampling.



All of this data processing serves to make our cost-function well-behaved.  
Our way of measuring error should be robust so our MOP is accurate with few designs.

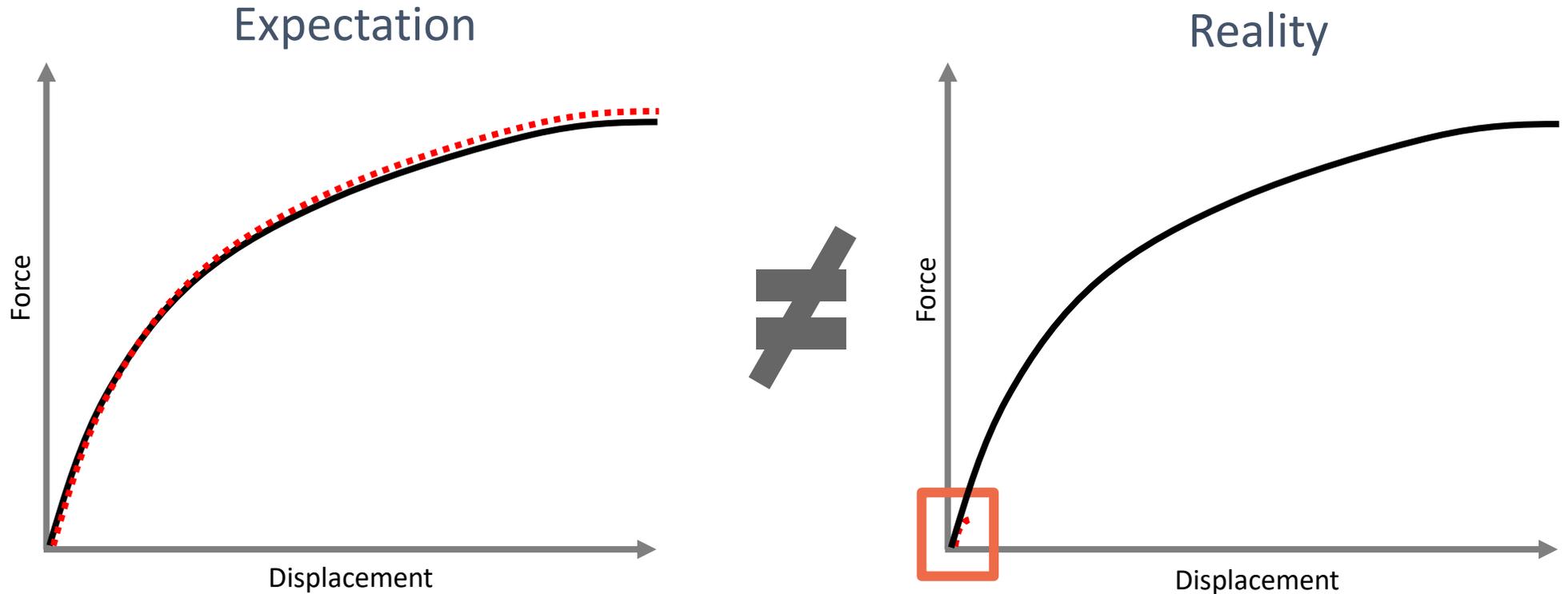
# Global Response fit – RMSE



$$Error_{RMSE} = \sqrt{\frac{1}{n} \sum_{i=1}^n \Delta y^2}$$

The easiest way to determine the difference between simulation and experiment is the root mean square error approach. Interpolation is required for this approach to work.

# Global Response fit – RMSE

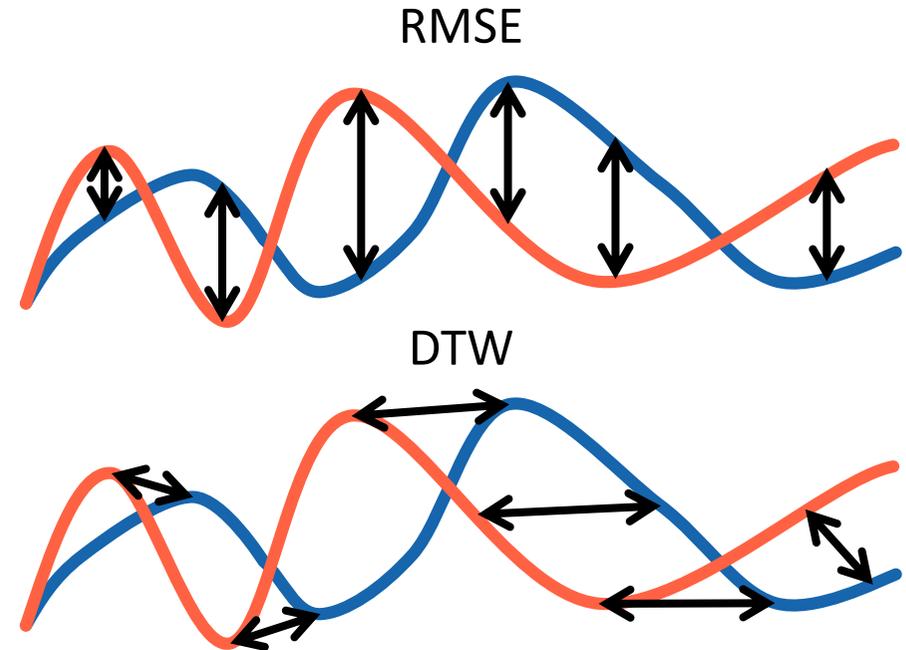


My error measure describes the optimum perfectly, however the behaviour is not robust and leads to many local minima which lead to a less than satisfactory optimization result.

# Global Response fit – Dynamic Time Warping



<https://www.cio.com/article/3239924/cios-listen-up-voice-recognition-meets-the-printer.html>



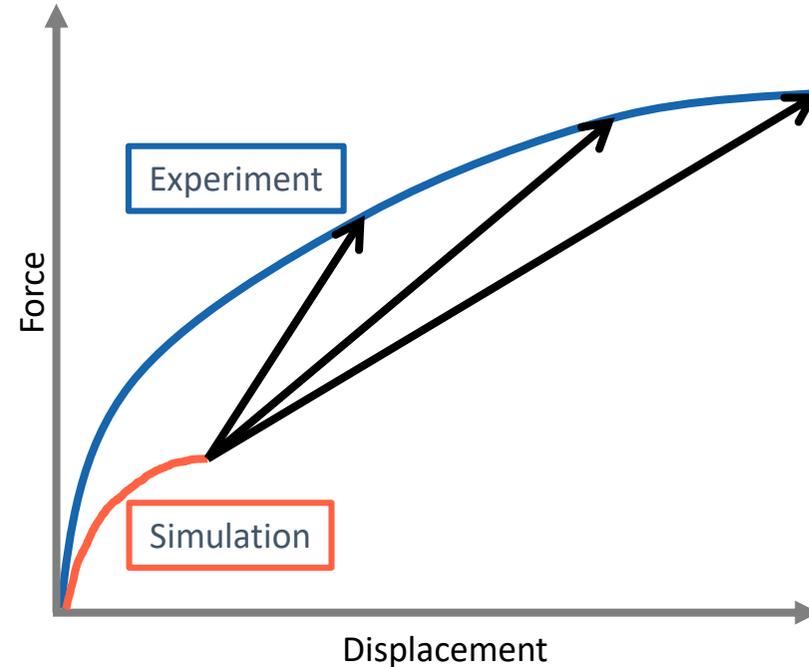
A great way of measuring the similarity between curves is dynamic time warping. Originally used in voice recognition it's applicable to material science as well.

# Global Response fit – Dynamic Time Warping



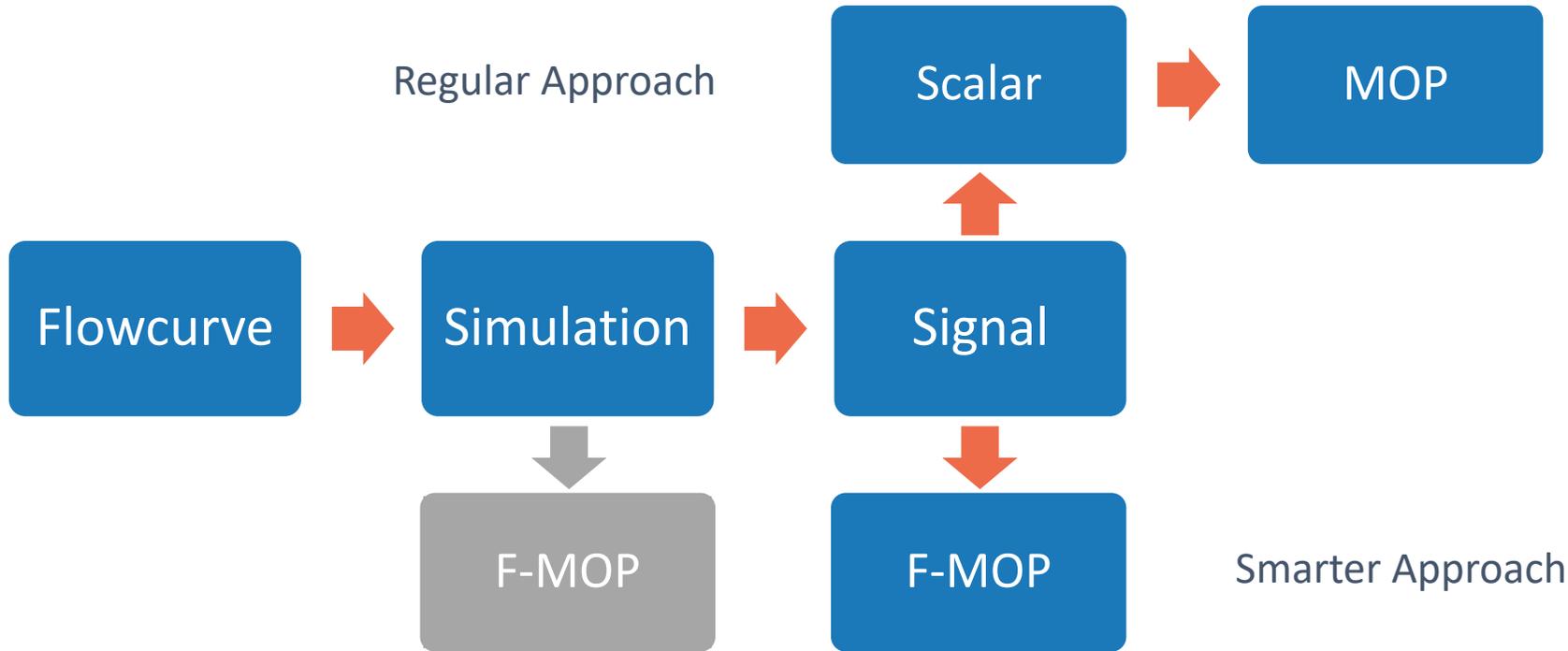
$a_{00}$	$a_{01}$	$a_{02}$	$a_{03}$	$a_{04}$	$a_{05}$	$a_{06}$	$a_{07}$
$a_{10}$	$a_{11}$	$a_{12}$	$a_{13}$	$a_{14}$	$a_{15}$	$a_{16}$	$a_{17}$
$a_{20}$	$a_{21}$	$a_{22}$	$a_{23}$	$a_{24}$	$a_{25}$	$a_{26}$	$a_{27}$
$a_{30}$	$a_{31}$	$a_{32}$	$a_{33}$	$a_{34}$	$a_{35}$	$a_{36}$	$a_{37}$
$a_{40}$	$a_{41}$	$a_{42}$	$a_{43}$	$a_{44}$	$a_{45}$	$a_{46}$	$a_{47}$
$a_{50}$	$a_{51}$	$a_{52}$	$a_{53}$	$a_{54}$	$a_{55}$	$a_{56}$	$a_{57}$
$a_{60}$	$a_{61}$	$a_{62}$	$a_{63}$	$a_{64}$	$a_{65}$	$a_{66}$	$a_{67}$
$a_{70}$	$a_{71}$	$a_{72}$	$a_{73}$	$a_{74}$	$a_{75}$	$a_{76}$	$a_{77}$
$a_{80}$	$a_{81}$	$a_{82}$	$a_{83}$	$a_{84}$	$a_{85}$	$a_{86}$	$a_{87}$
$a_{90}$	$a_{91}$	$a_{92}$	$a_{93}$	$a_{94}$	<del><math>a_{95}</math></del>	<del><math>a_{96}</math></del>	<del><math>a_{97}</math></del>

<https://www.quora.com/How-do-I-create-a-rm-LaTeX-macro-that-generates-an-m-times-n-matrix>



A matrix is produced by the DTW algorithm which pairs individual points of the signals. The distance (error) is easily quantified and agrees with my qualitative estimations.

# Global Response fit - SoS

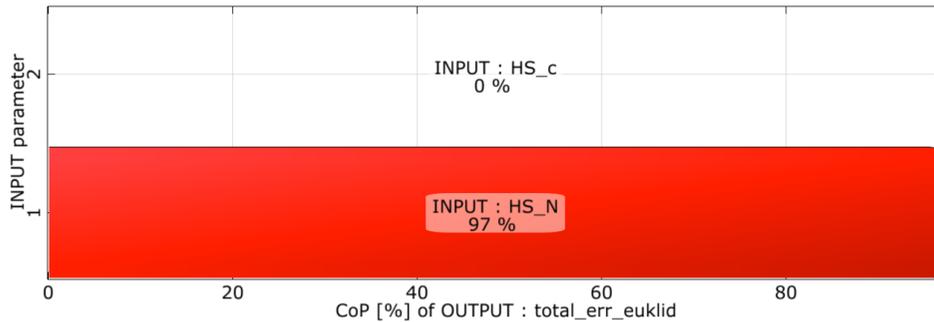


While the other approaches certainly work, using SoS is far more elegant and all the information we obtain in our signal can be used to gauge the sensitivity with a F-MOP.

# Global Response fit – Comparison

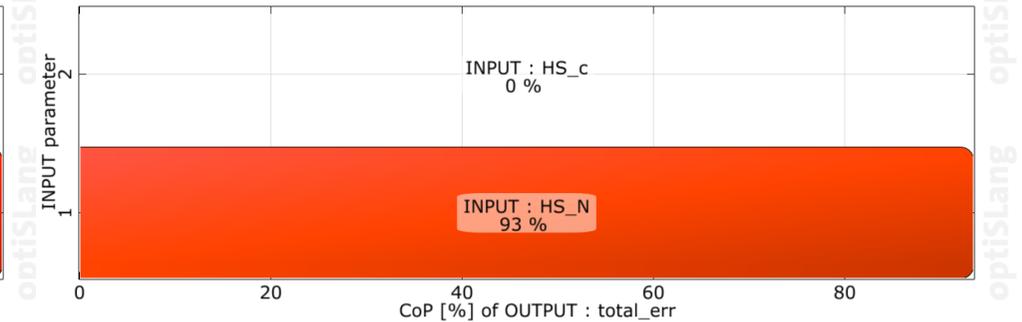
## RMSE

Coefficients of Prognosis (using MOP)  
full model: CoP = 98 %



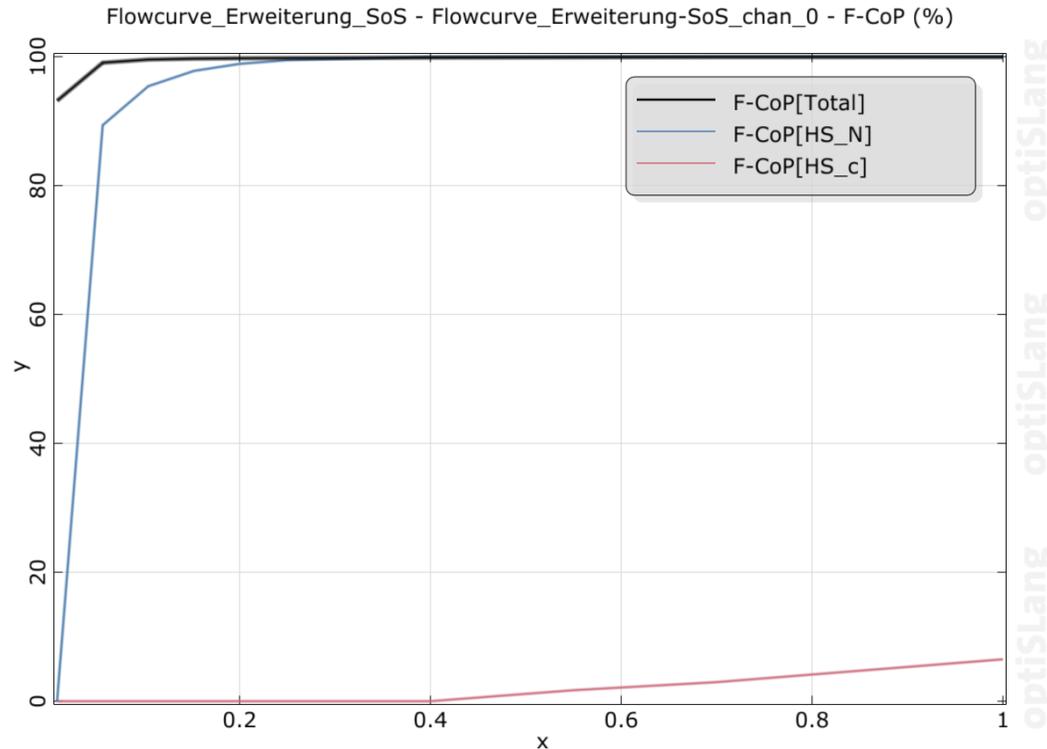
## DTW

Coefficients of Prognosis (using MOP)  
full model: CoP = 94 %



Judging from just the CoP you would think that RMSE is a better measure.  
This is deceptive and not the case, otherwise I would not give this presentation!

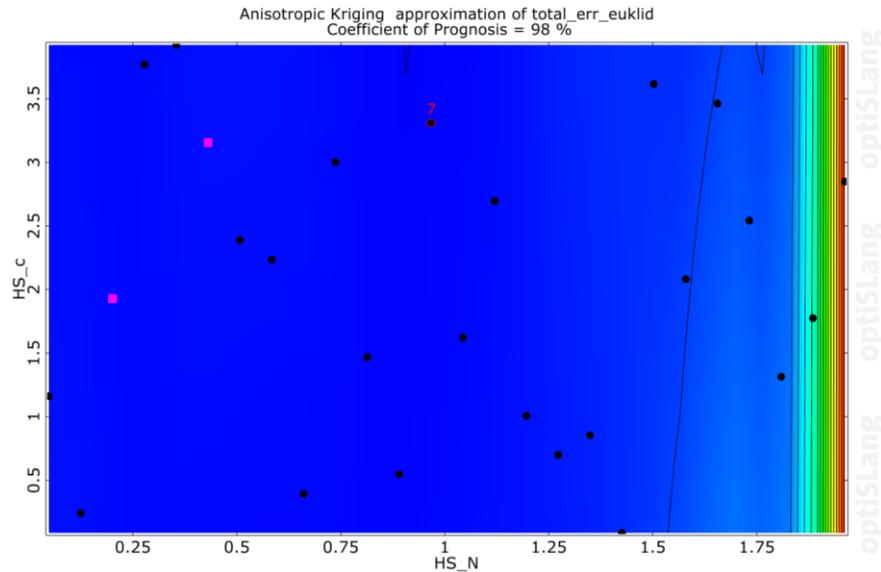
# Global Response fit – Comparison



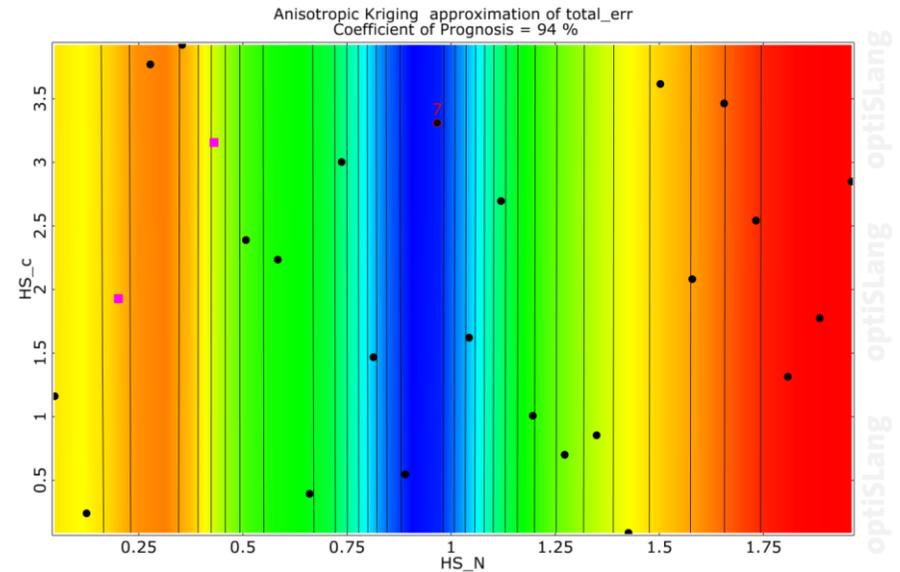
Of course, our variable C has a significant impact on the results but due to the large influence of N our MOP does not capture this. With SoS and its' F-MOP, the influence is easily shown.

# Global Response fit – Comparison

## RMSE

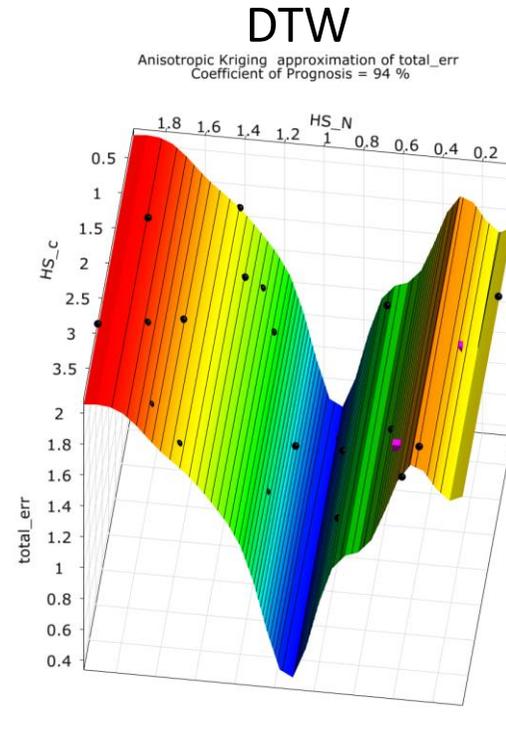
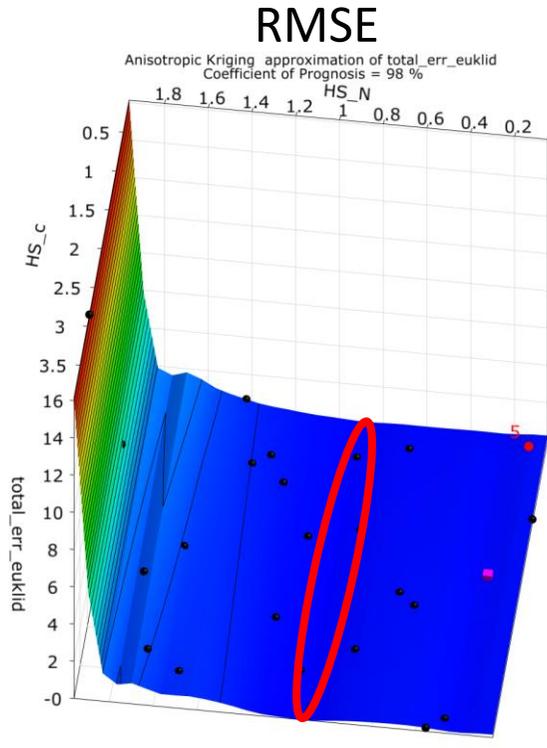


## DTW



The response surface however, tells a very different story. While most of the area with RMSE is quite flat and kind of useless. With DTW every design provides information.

# Global Response fit – Comparison

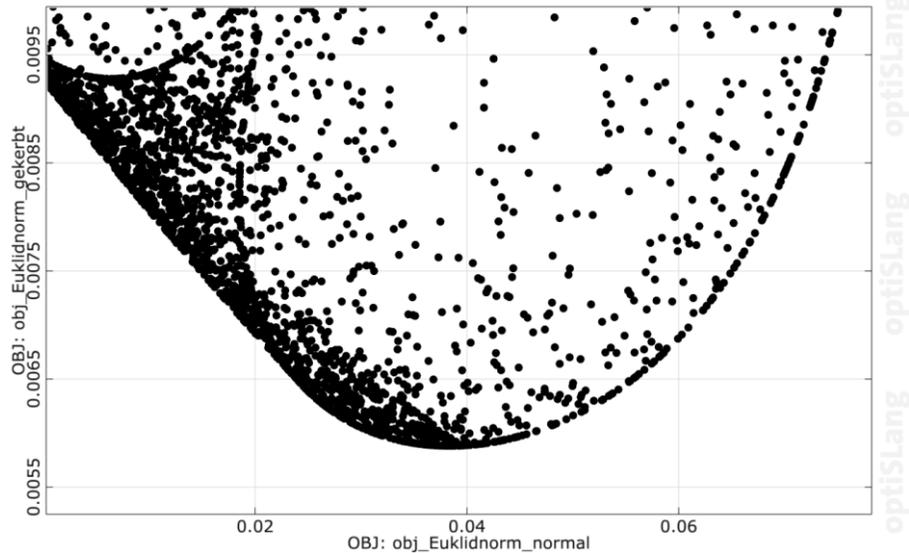


The response surface however, tells a very different story. While most of the area with RMSE is quite flat and kind of useless. With DTW every design provides information.

# Global Response fit – Comparison

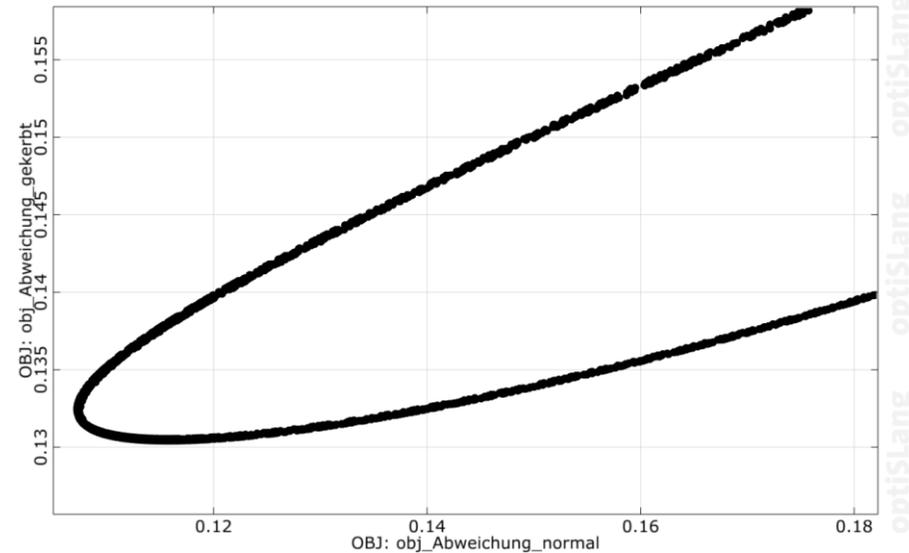
## RMSE

Objective Pareto Plot



## DTW

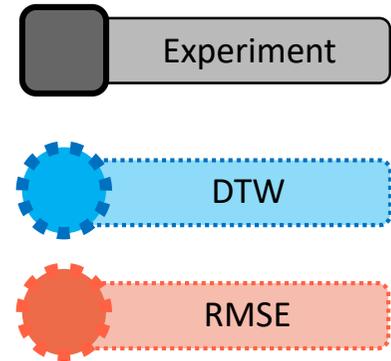
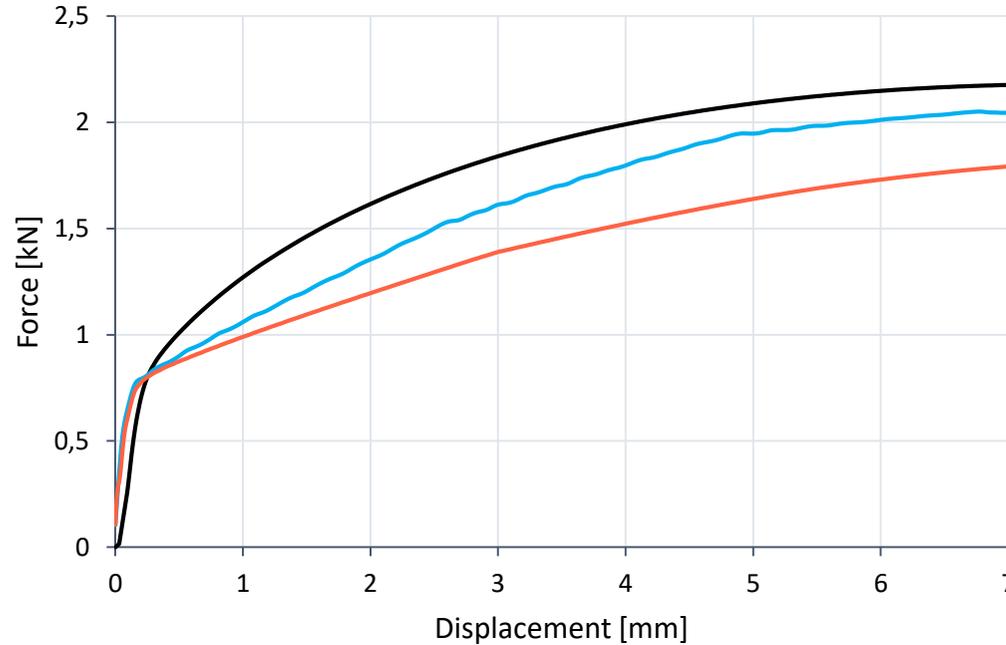
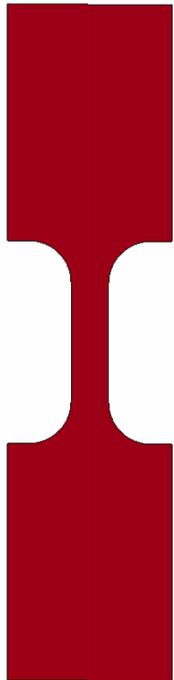
Objective Pareto Plot



The results become even more apparent if you look at the pareto set.

With DTW we are able to detect our best design easily.

# Global Response fit – Comparison

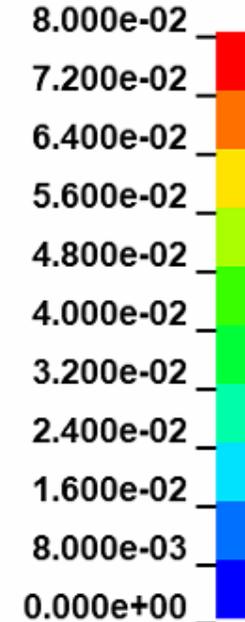


Both flowcurve parameters suggested by the MOPs do not fit the experiment exactly. However, the suggestion based on the data from DTW is a lot closer.

# Global Response fit - Outlook



Thickness Reduction- based on initial geometry



Thanks to Digital Image Correlation (DIC) we can take a closer look at our „black box“ experiment. In the future a fit based on the local response with SoS will reduce data loss.

Multiple adjustments to the data are necessary to remove bias:

- Normalize axes for all experiments and simulations
- Resample so every signal has the same amount of points

While a good CoP can be reached with these adjustments and RMSE, the MOP obtained is not suitable for an optimization.

Dynamic Time Warping is a better description of signal deviation and leads to a „well behaved“ MOP. The optimum in this MOP delivers acceptable results on another specimen.

- G. Johnson, W. Cook: A constitutive model and data for metals subjected to large strains, high strain rates and high temperatures  
  
Proceedings of the Seventh International Symposium on Ballistics, 1983
- F. Andrade, A. Haufe, M. Feucht, F. Neukamm: An incremental stress state dependent damage model for ductile failure prediction  
  
International Journal of Fracture, V200, 2016
- H. Sakoe, S. Chiba : Dynamic programming algorithm optimization for spoken word recognition  
  
IEEE Trans. Acoustic Speech and Signal Processing, V26, 1978



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