

$$\bar{\Pi} = \frac{1}{2} \sum_c \{u\}^T \cdot [K] \cdot \{u\} - \{u\}^T \cdot \{F\}$$



Optimization of Laminated Composites – Overcoming Challenges in Design

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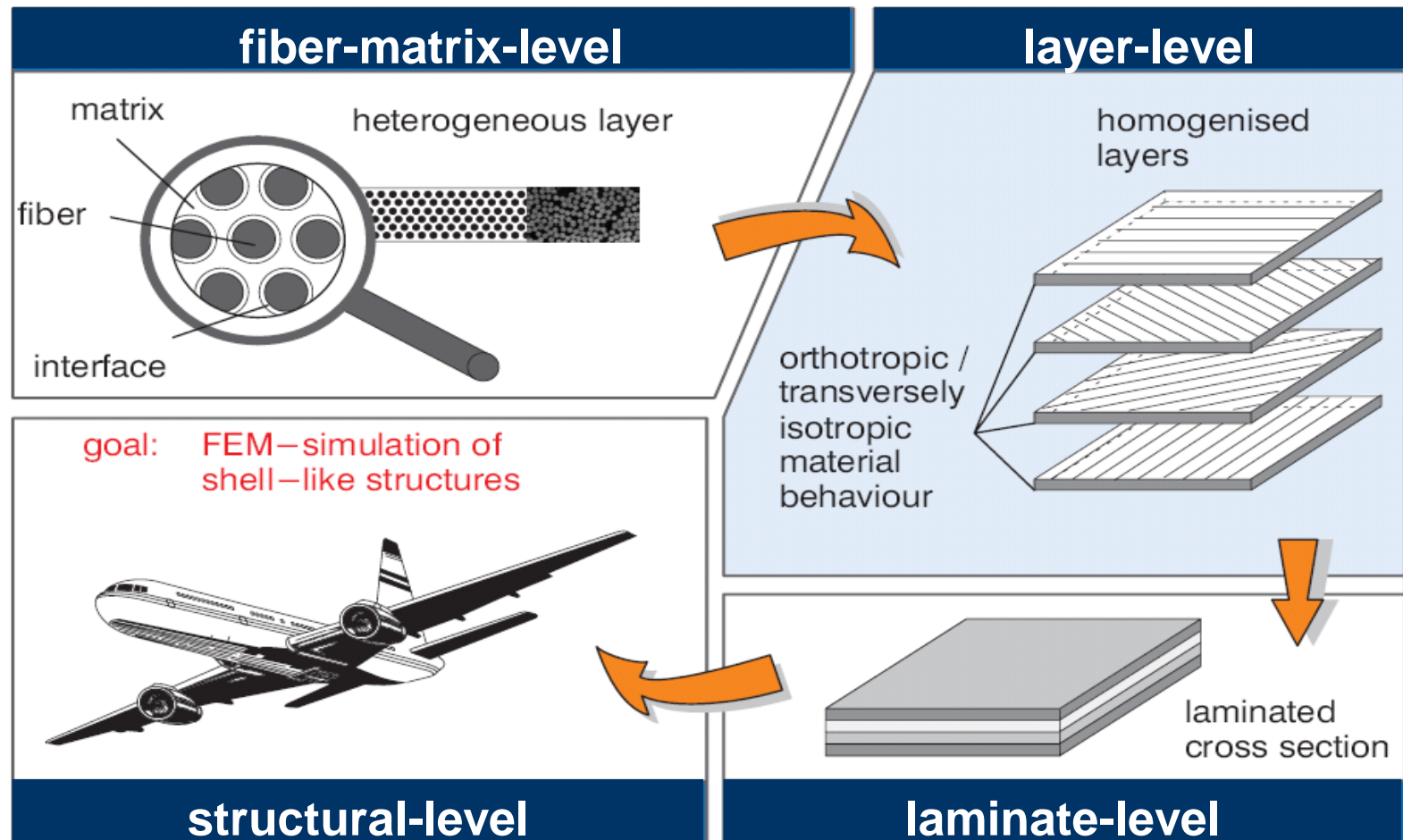
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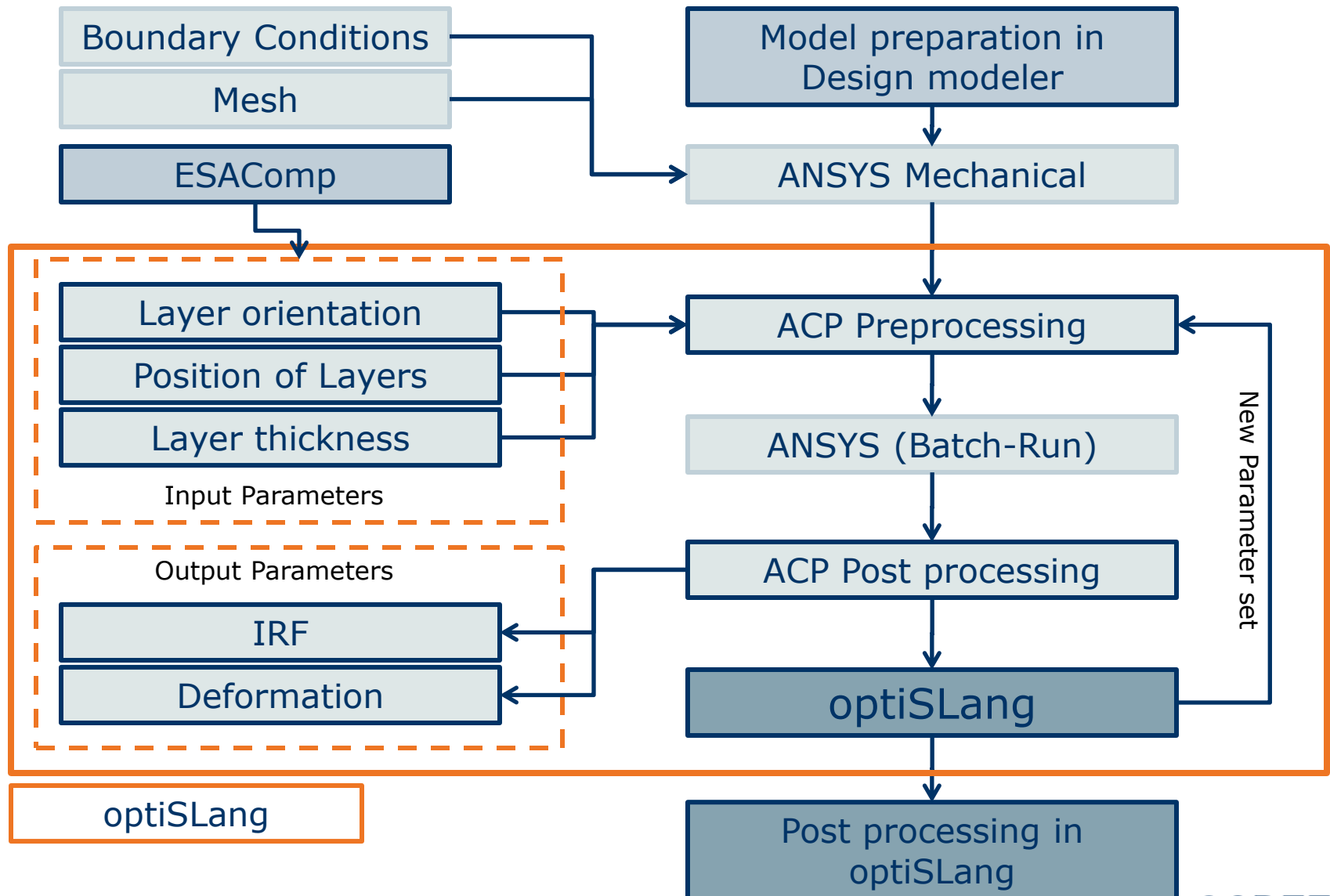
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Motivation

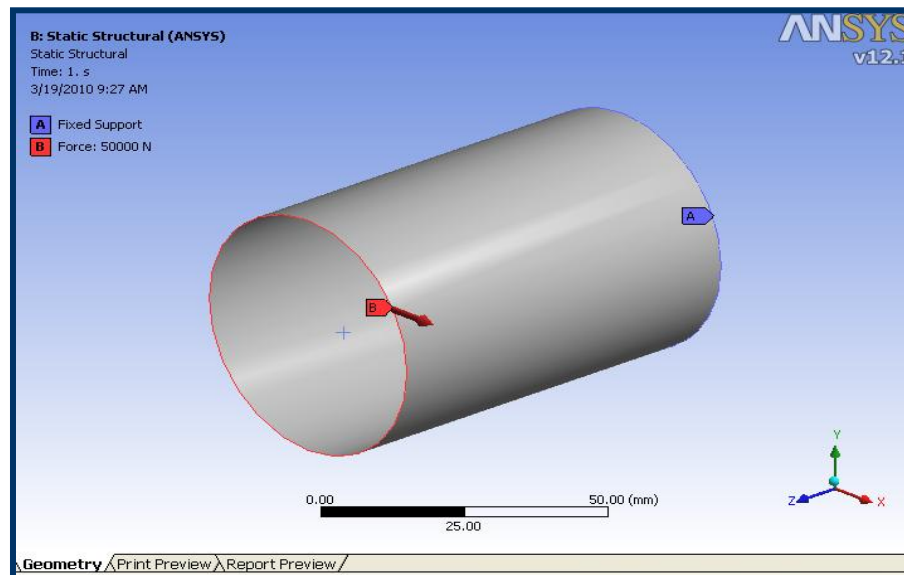
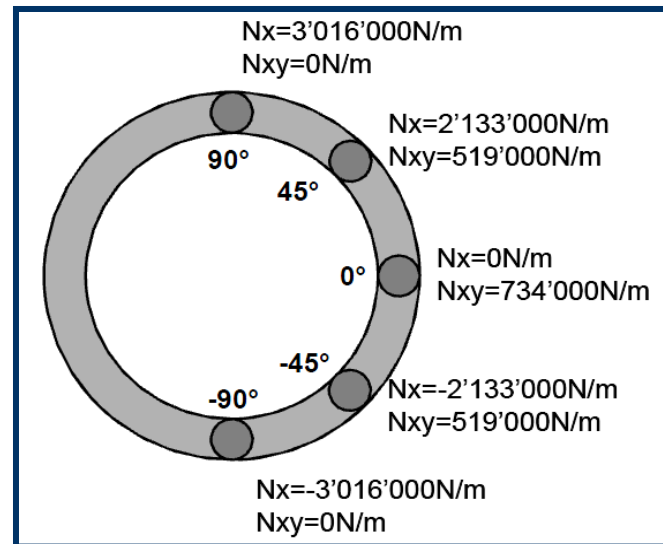
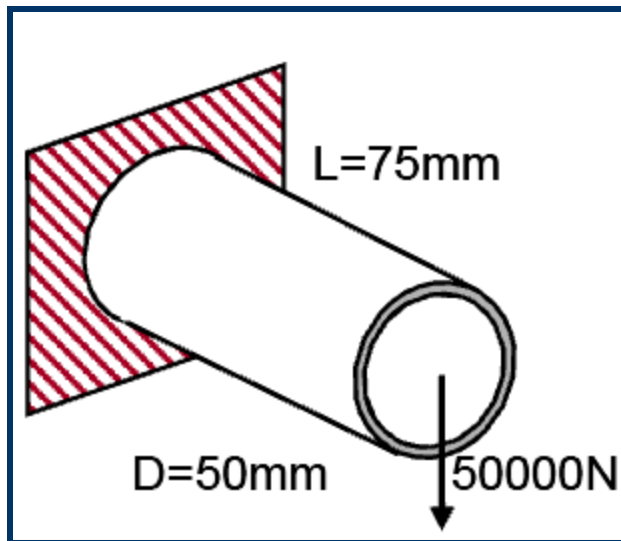
To propose a simple workflow for optimizing laminated composite properties (particularly layer orientations, position of layers, and layer thickness) using ESAComp, ANSYS Composite Prep-Post(ACP) and optiSLang.



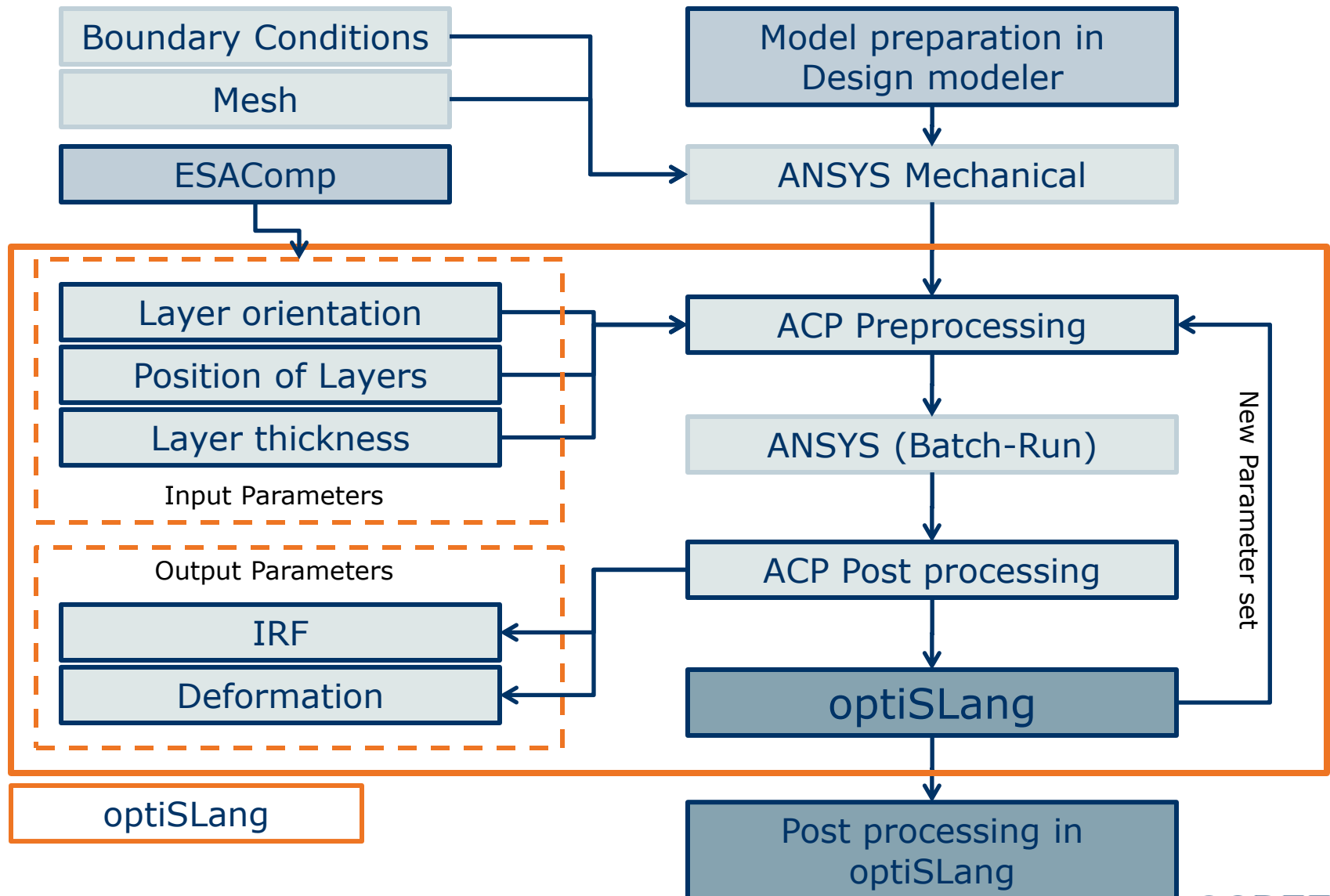
Workflow



Simulation Model



Workflow



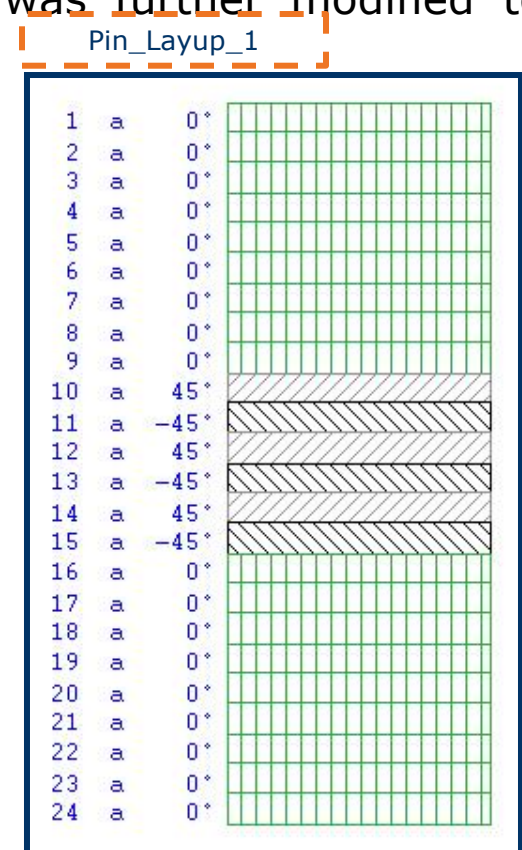
Composite Material Analysis in ESAComp

- A simple laminate was considered (Refer table below for layer properties)
- This laminate (shown below) was checked for load carrying capability using Load response (with First Ply Failure) in ESAComp
- Using the results at this stage, laminate layup was further modified to withstand failure

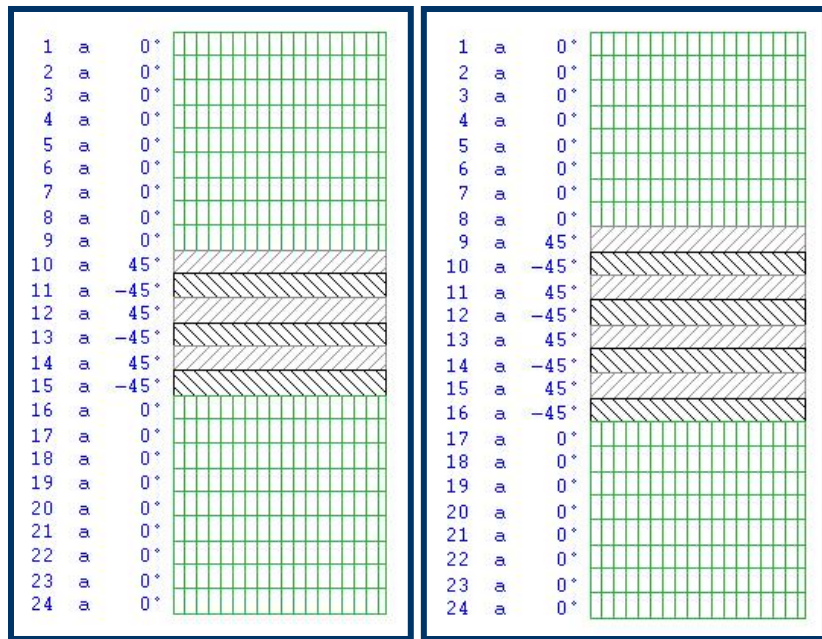
S.No	Engineering Constants	Units	Property
1	Each Layer thickness	mm	0.3
2	Density	Kg/m3	1600
3	Longitudinal Elastic modulus (Ex)	MPa	115000
4	Transverse Elastic modulus (Ey)	MPa	6500
5	Shear modulus (Gxy) in XY plane	MPa	6000
6	Poisson's ratio (Nuxy) in XY plane		0.28
7	Poisson's ratio (Nuyz) in YZ plane		0.34
Failure stresses			
8	X_t	MPa	2200
9	X_c	MPa	810
10	Y_t	MPa	40
11	Y_c	MPa	190
12	S	MPa	50
13	Q	MPa	50

X_t – Tensile failure stress in x direction
Y_t – Tensile failure stress in Y direction
S – In plain shear failure stress in XY plain

X_c – Compressive failure stress in X direction
Y_c – Compressive failure stress in Y direction
Q – Out of plane failure stress in YZ plain

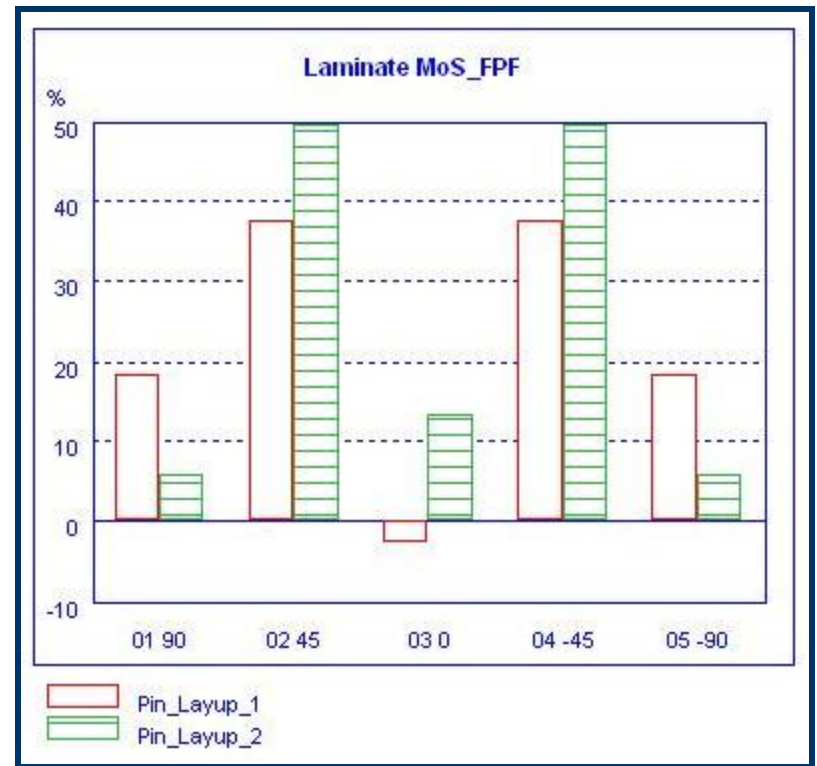


Laminate Level – Load response / failure



Pin_Layup_1

Pin_Layup_2

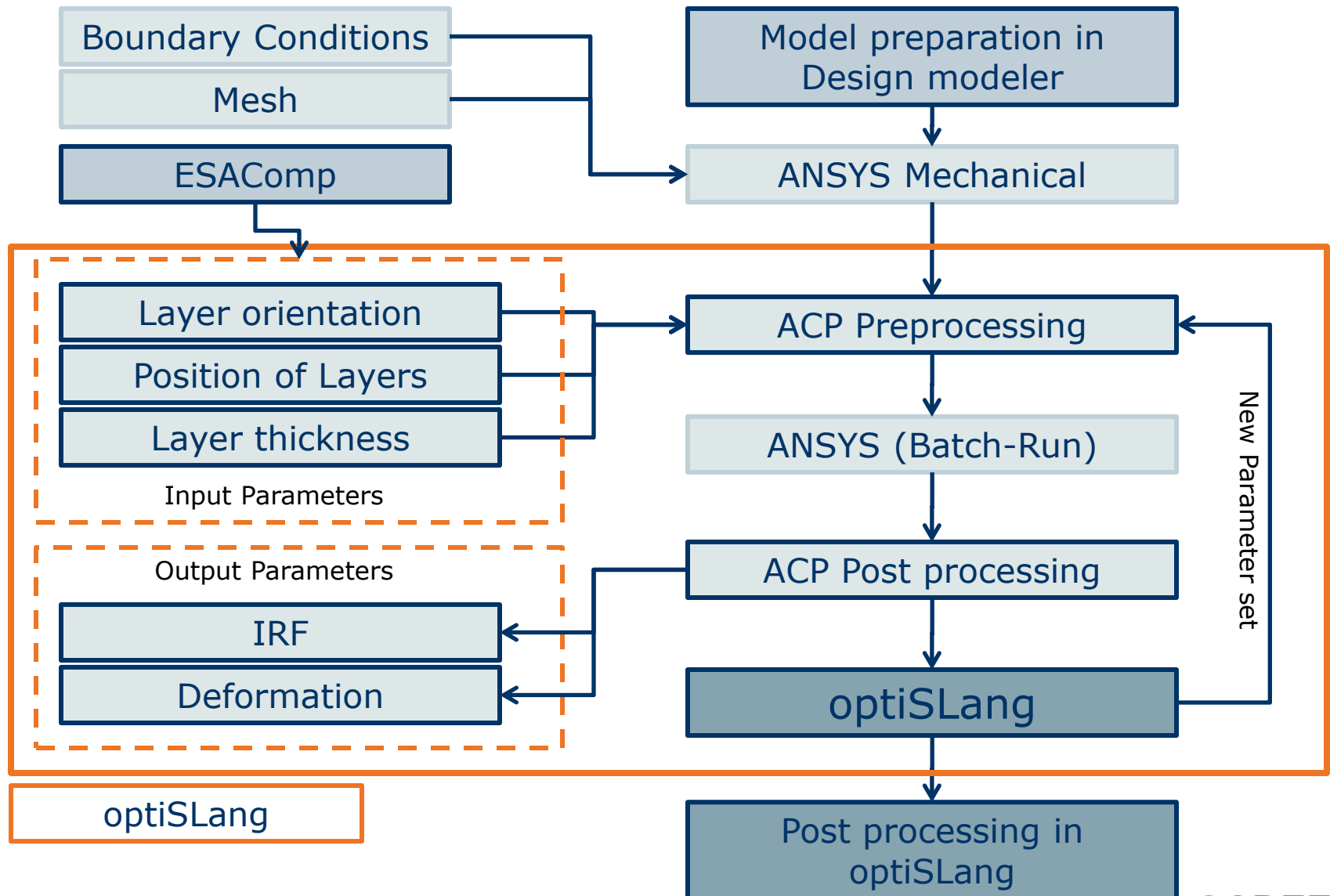


MOS_FPF			
S.No	Load	MoS_FPF (%)	
		Pin_layup_1	Pin_layup_2
1	90	18.424	5.901
2	45	37.5612	49.742
3	0	-2.732	13.3414
4	-45	37.5612	49.742
5	-90	18.424	5.901

Laminate was found to be safe with modified layup, i.e., Pin_Layup_2

Factor of safety : $FoS^w = 1$
 Failure criterion : Max stress 3D; Max strain; Von Mises; Out-of-plane shear; Out-of-plane shear; None (UD; non-UD; homogeneous; honeyc. core; foam/other core; adhesive)
 Stress/strain recovery : layer top/bottom

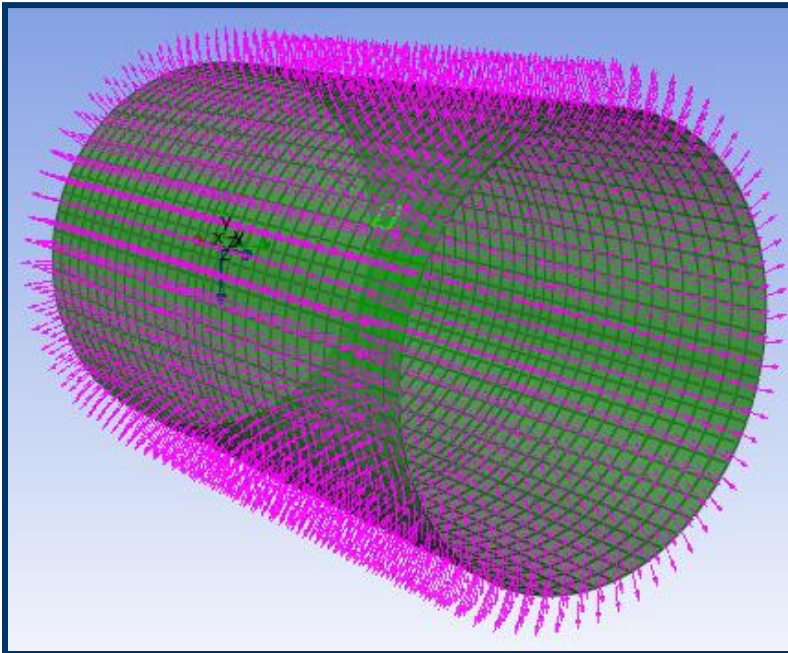
Workflow



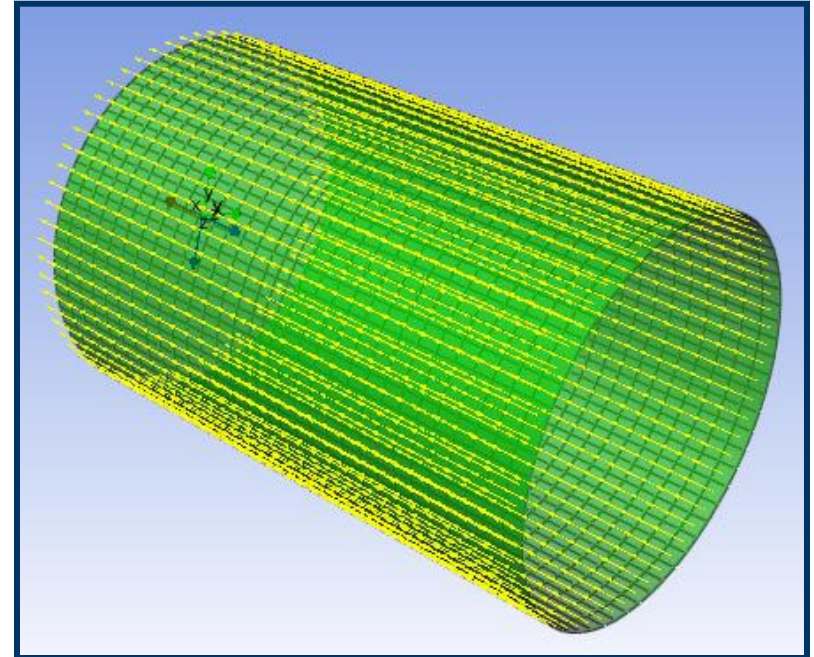
Structural Analysis in ACP

- Finalized material properties is exported into ACP.
- Before the solving the model in ACP using ANSYS, it is to be ensured that, all element sets have proper orientation
- All element normal's should be on the same side (to be aligned to the local Z axis)

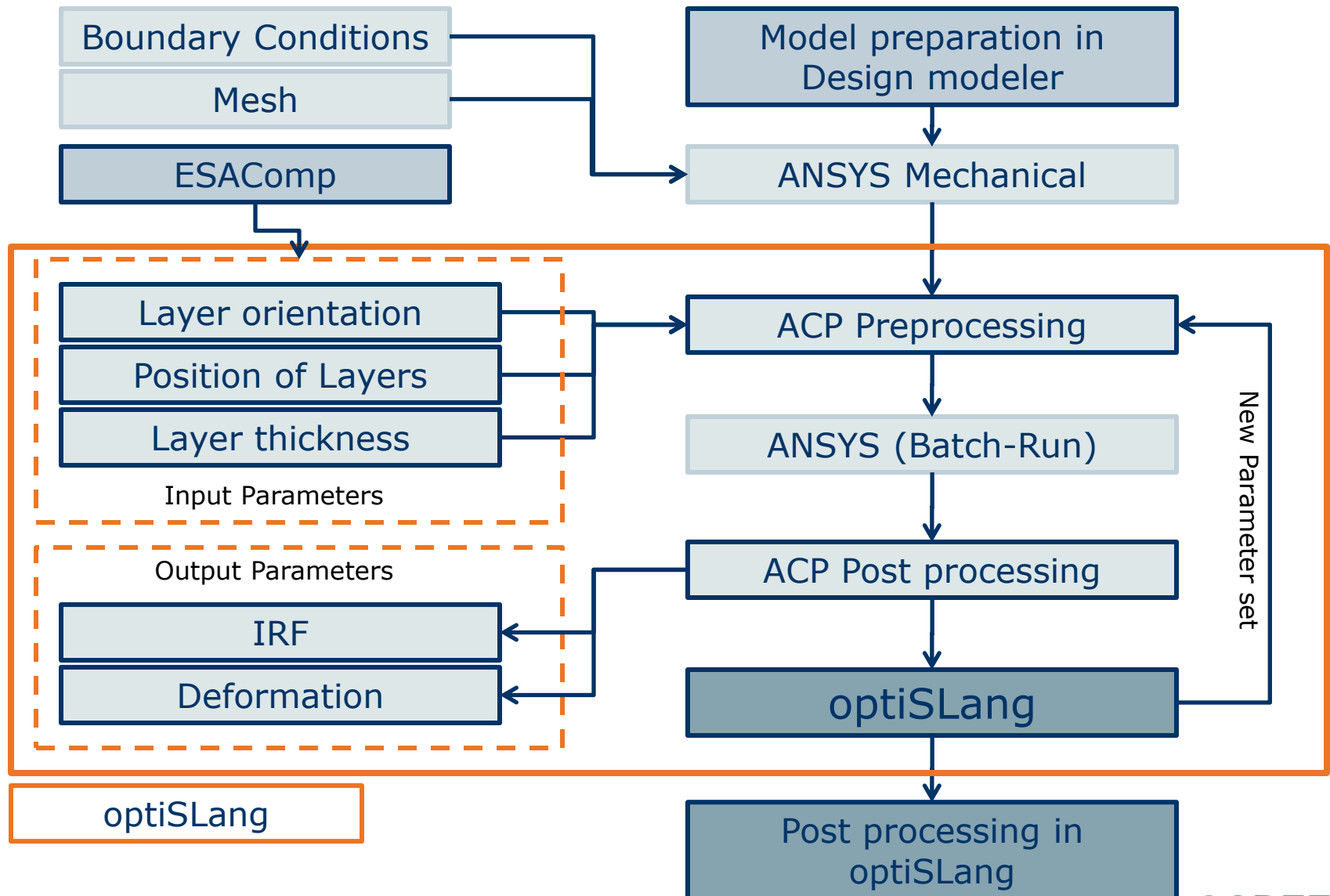
Z axis of each element being aligned to the element normals and shown in pink



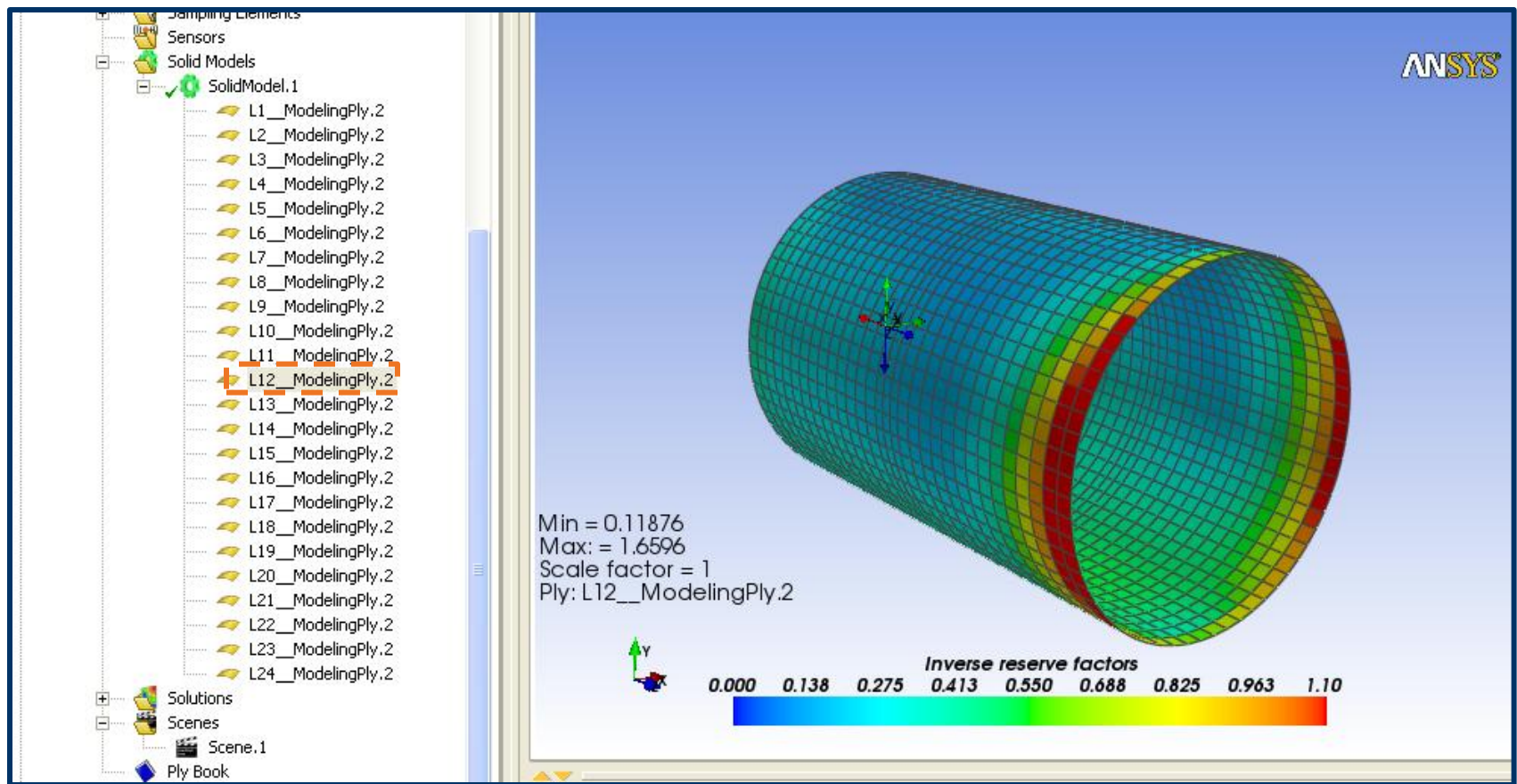
X-axis of each element being aligned to global X-axis and is shown in yellow.



Workflow

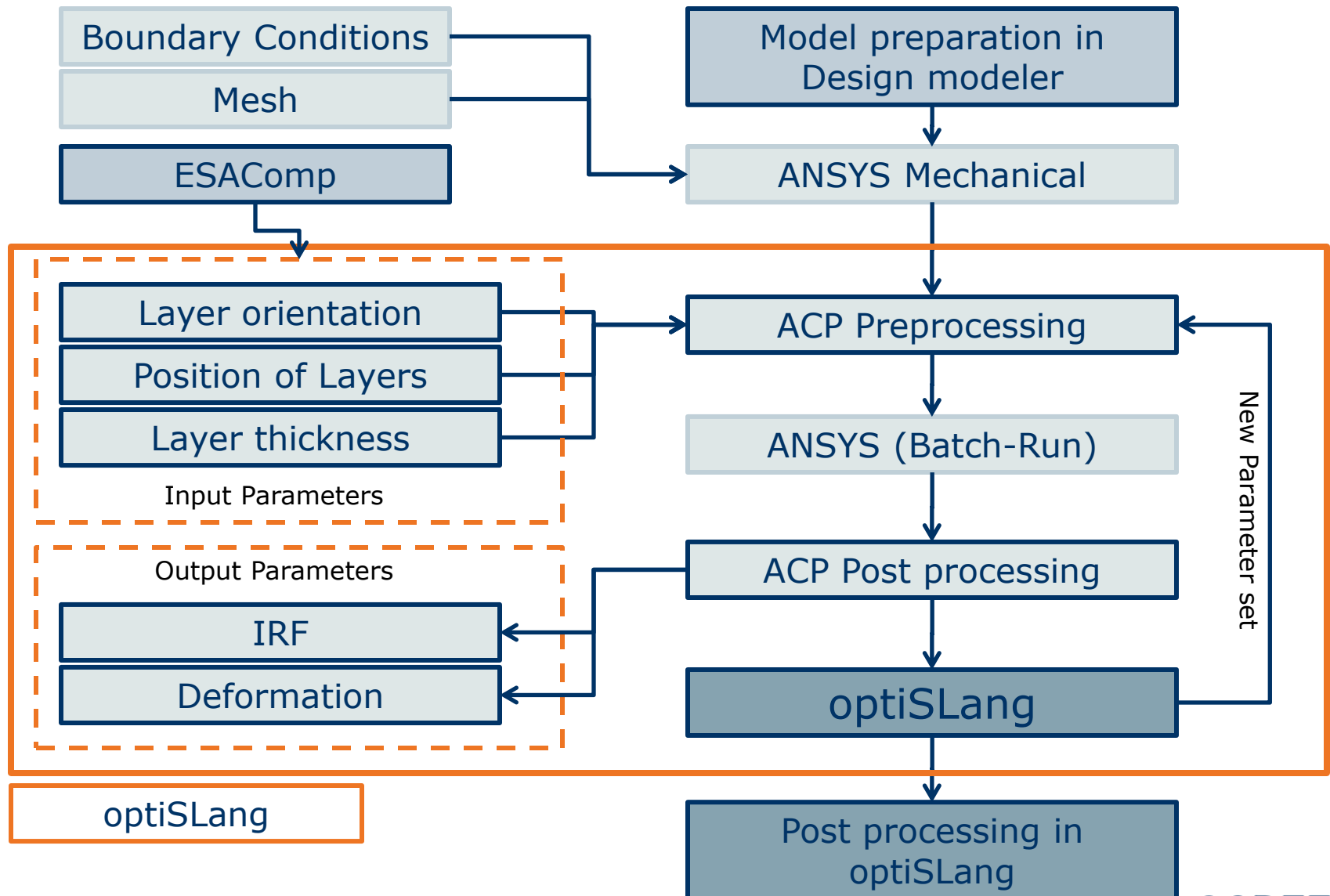


Post Processing using ACP: IRF



Layer wise failure can be visualized i.e., failure mode in 12th layer was shown above. Maximum value of IRF being higher than 1, the above laminate failed

Workflow



Problem Overview

First whole process is completely automated

Input Parameters

25 Input/Design parameters

- 1 continuous variables – Thickness of whole structure
- 24 discrete variables – Angles of each Ply with variation between – 90 to 90 with 5° increment

Response Parameters

26 Response parameters

- 2 Displacements → Max x disp. and Max y disp.
- 24 Inverse Reserve Factor(IRF) → IRF of each ply

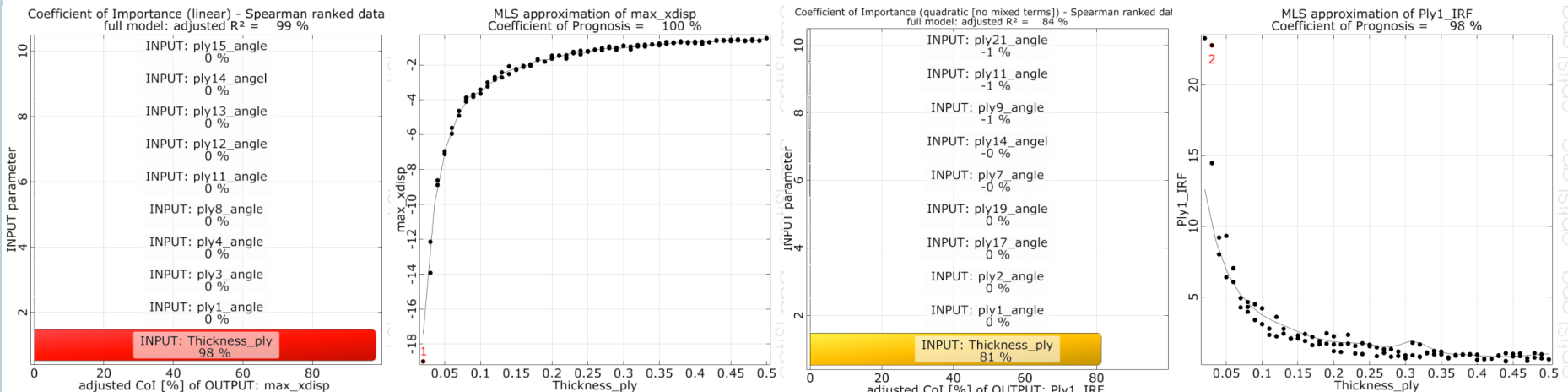
Objective and Constraint

- Minimize the mass and max displacement
- IRF value of each ply less than 1 as constraints.

Sensitivity Analysis

Design of Experiment (DoE) is carried out using 100 Latin Hypercube samples

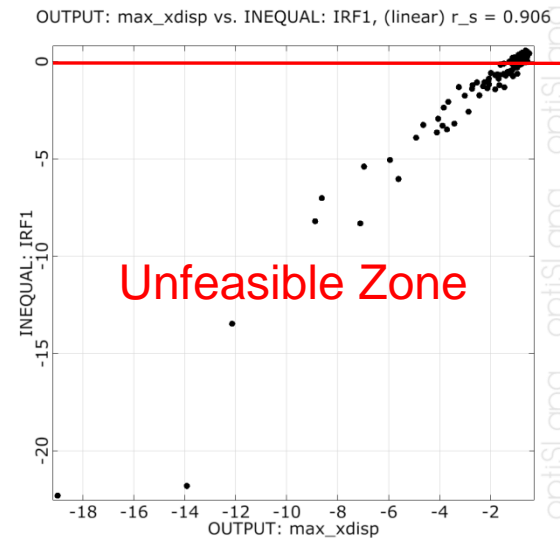
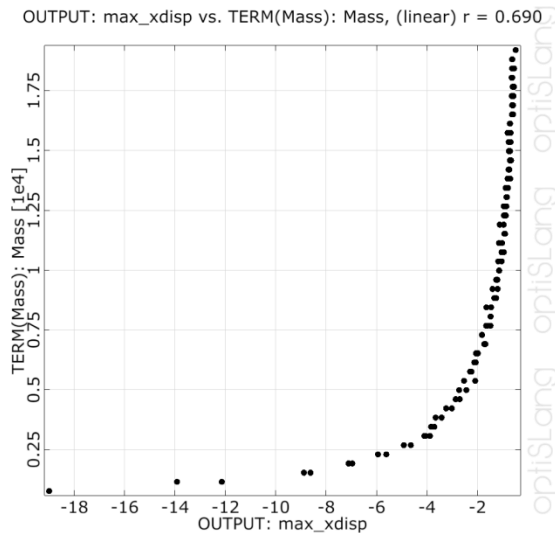
Result Evaluation - Responses



- Maximum Coefficient of Importance (CoI) more than 80% for both the Max_xdisp and Ply1_IRF
- Only Thickness_ply has influence on responses
- Responses vary non linearly with the variation of the input variable.

Sensitivity Analysis

Result Evaluation – Objective



- Two objectives are conflicting -> Pareto optimization
- Mass increase non linearly with the decrease in displacement
- Constraint of $IRF < 1$ curtails the displacement
- Due to above reason only mass can be chosen as objective
- Objectives are reduced from 2 to 1 -> No Pareto Optimization
- Global optimum design from sensitivity analysis is chosen as a starting point for optimization, to reduce computation time

Optimization

Overview

- All input parameters are considered for optimization
- Mass is considered as the only objective. It depends only on ply thickness
- To choose best design with less displacement among the designs with same mass, max displacement in x and y direction terms are added to the objective

#	Name	Formula	Type	Active
1	Mass	Thickness ply*1600*24	term	<input type="checkbox"/>
2	xdisp1	fabs(max xdisp)	term	<input type="checkbox"/>
3	ydisp1	fabs(max ydisp)	term	<input type="checkbox"/>
4	Mass	10.0*Mass+1.0*xdisp1+1.0*ydisp1	objective	<input checked="" type="checkbox"/>

- 24 constraints -> IRF of each ply < 1
- More than 15 discrete input parameters -> Evolutionary algorithm for optimization

Optimization

Initial vs. Optimized Design

- 25 input variables
- $N = 100 + 400 = 500$ No. of design evaluations
- Total mass of the composite structure as well as the displacement of best design are less compared to initial design

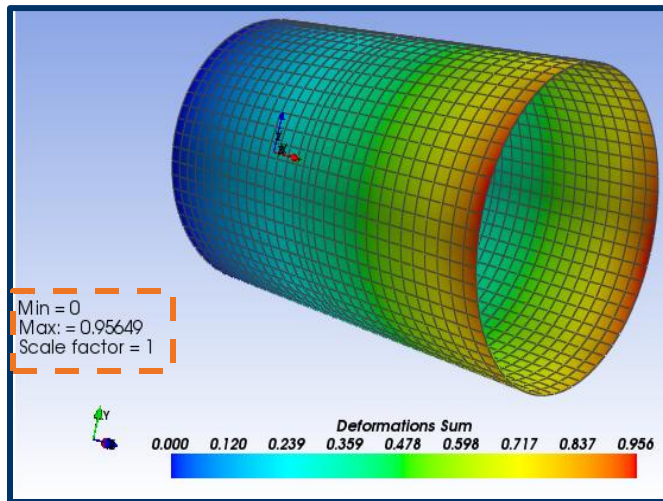
Output	Initial	SA	EA	EA – Improvement
Mass	11520	13824	11136 (3.5%)	10752 (7%)
Displacement Sum	0.96	0.80	0.86 (10%)	0.90(6.3%)

SA – Sensitivity Analysis

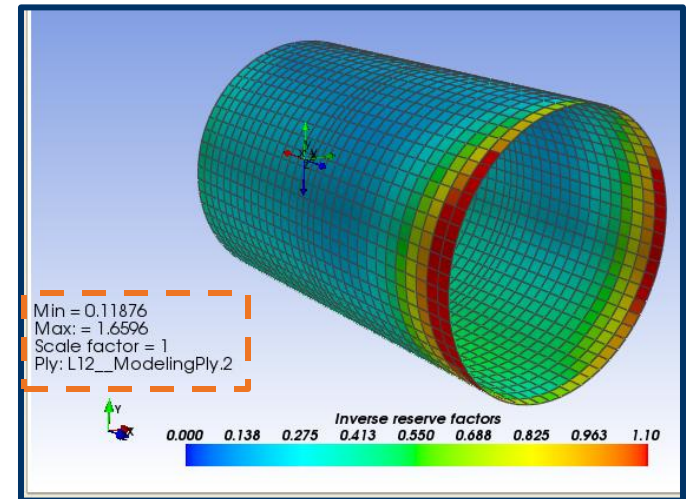
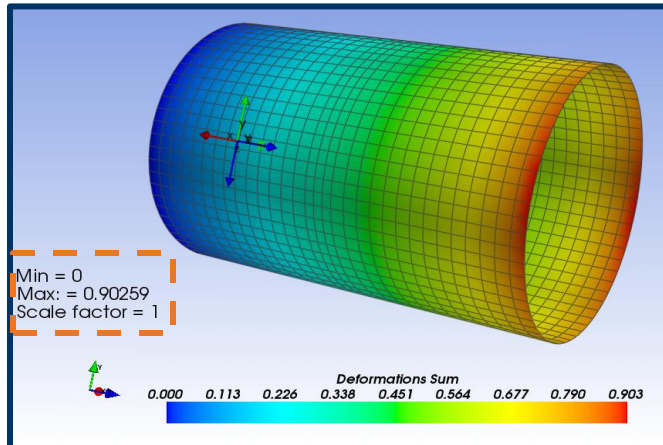
EA – Evolutionary Analysis

Optimization

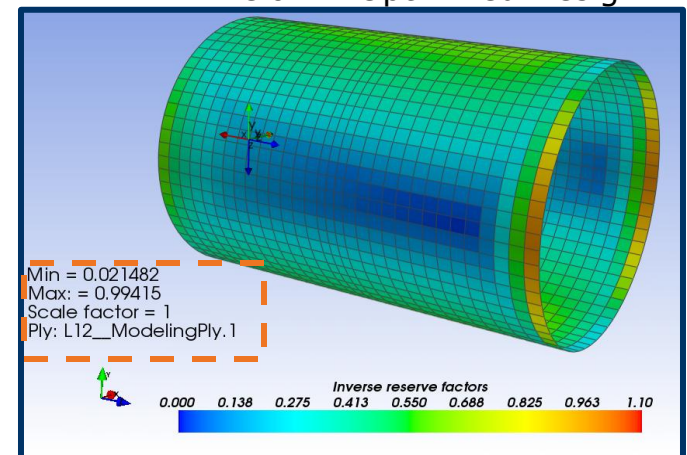
Initial vs. Optimized Design



Deformation : Above – Initial Design;
Below – Optimized Design



IRF : Above – Initial Design;
Below – Optimized Design



Summary

- **Behavior of laminates** is **studied without using FE analysis** (using Classical Laminate Theory), by an industrial approved software solution called **ESAComp** -> **Avoid FE simulation**
- **Second composite material** is designed based on the **suggestion from ESAComp** -> **Better performance** compared to the initial material
- Second composite material is **applied and investigated on model** using FE Analysis
- **Model setup** using composite material and the **post processing of the results** is carried out by a software tool called **ACP**
- **Structural failure occurred** for given load condition -> **optimization** has to **carried with failure constraints**
- Complete **optimization process** is **automated** using a tool called **optiSLang**

Summary

- **Sensitivity analysis** is using 100 Latin Hypercube sampling due to following advantages:
 1. **Better understanding** of design space to **define objective and constraints** -> **Save's computation time**
 2. **Global optimum design** as **start up** for optimization -> **Less computation time**
 3. To choose **important design parameters** for optimization -> **Save's computation time**
- **Optimization** is carried out using **Evolutionary / Genetic algorithm**
- **7% and 6.3% of reduction in mass and deformation** was achieved for the best design
- Goal of optimizing the laminate was achieved

$$\bar{\Pi} = \frac{1}{2} \sum_e \{u\}^T \cdot [K] \cdot \{u\} - \{u\}^T \cdot \{F\}$$



Thank You